

Complementary aspects of MuSR and other experimental methods

Tomo Uemura, Columbia University

Spin Glasses AuFe and CuMn

$\text{La}_2\text{CuO}_{4.12}$, $(\text{La},\text{Nd},\text{Sr})_2\text{CuO}_4$

$\text{Sr}_4\text{V}_2\text{O}_6\text{Fe}_2\text{As}_2$, $\text{Sr}_4\text{Sc}_2\text{O}_6\text{Fe}_2\text{As}_2$

MnSi under applied pressure

Muon-spin relaxation in *AuFe* and *CuMn* spin glasses

Y. J. Uemura

Brookhaven National Laboratory, Upton, New York 11973

and Department of Physics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo, Japan

T. Yamazaki

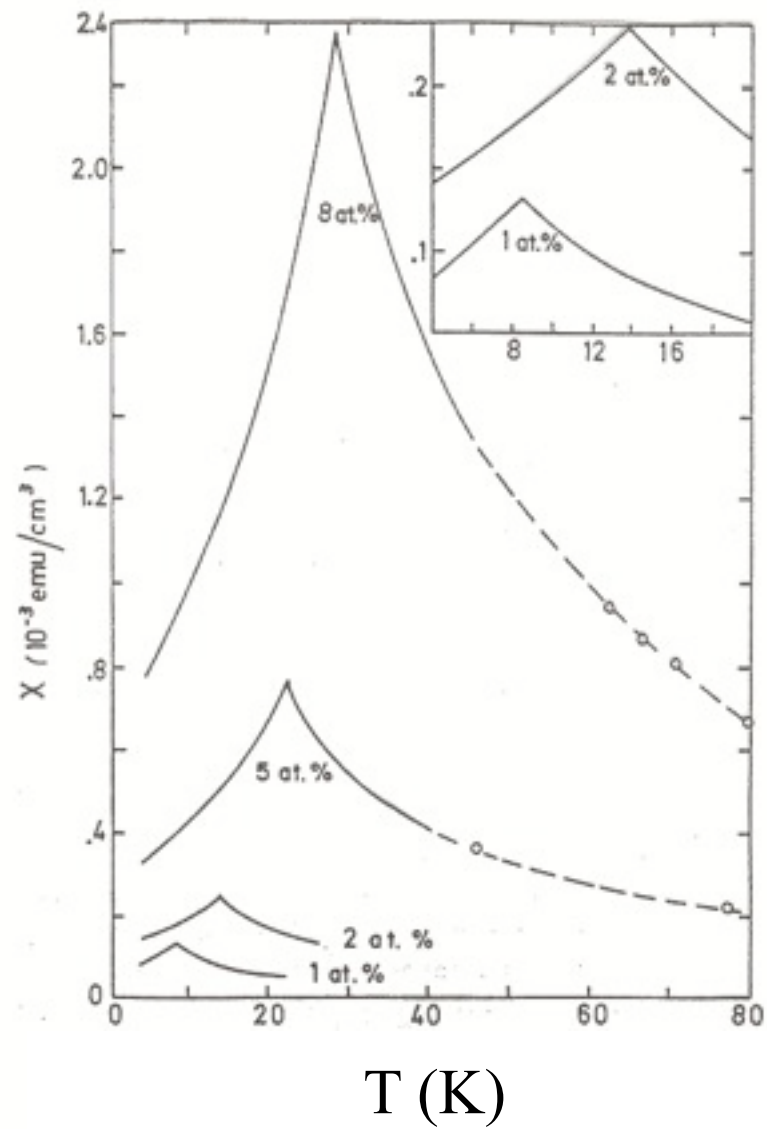
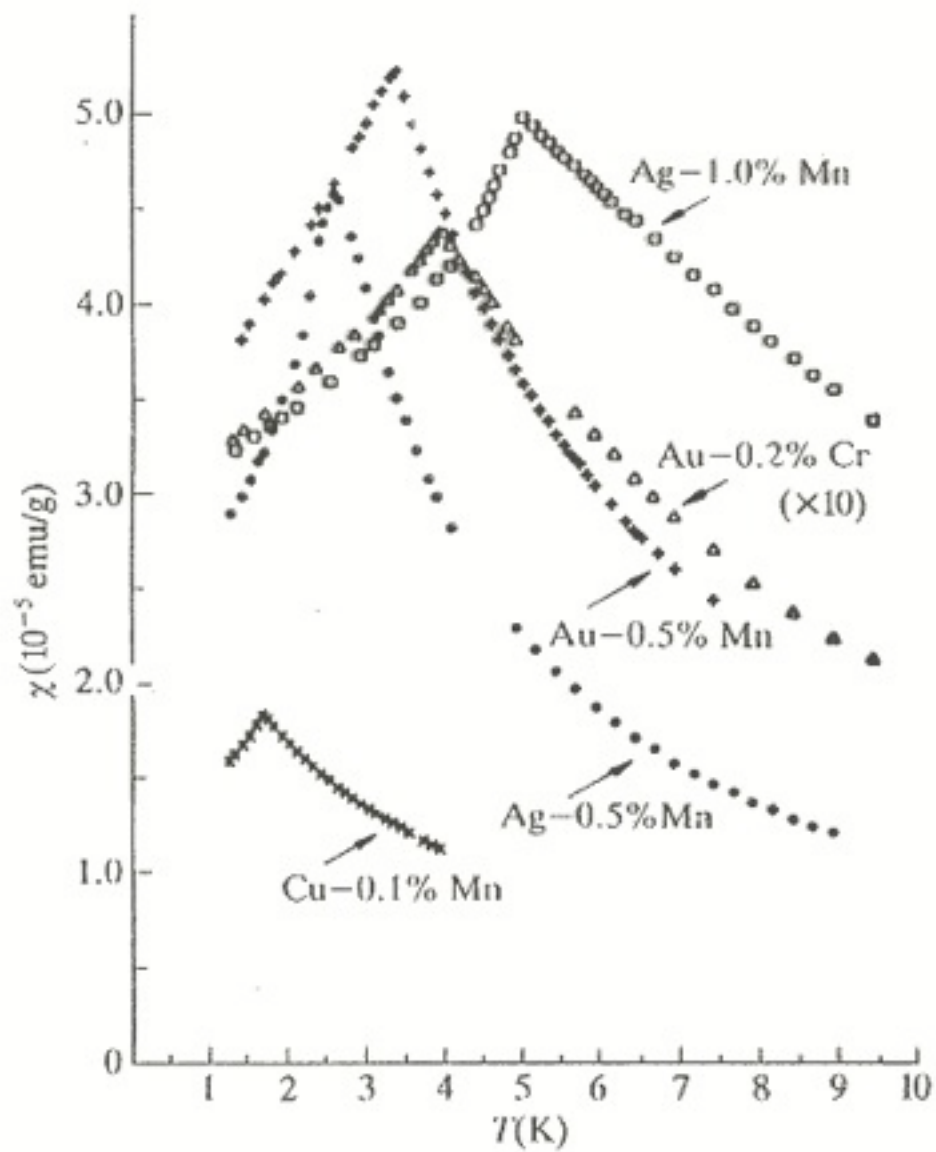
Department of Physics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo, Japan

D. R. Harshman, M. Senba, and E. J. Ansaldo*

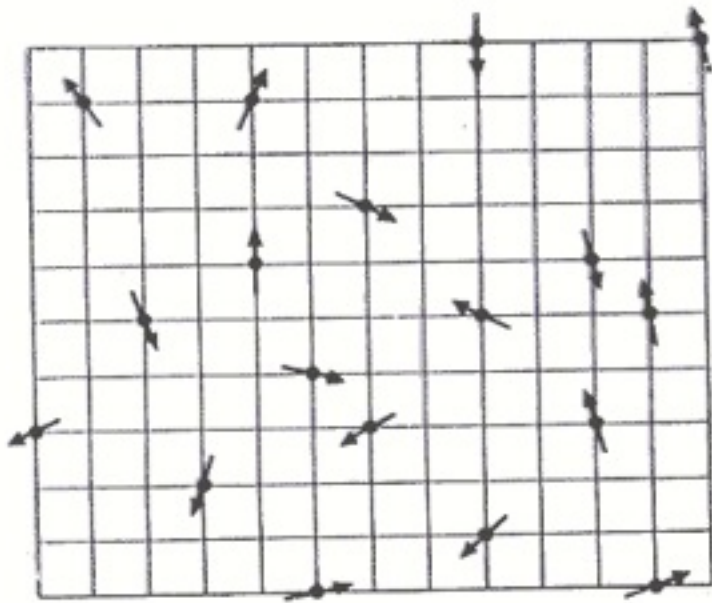
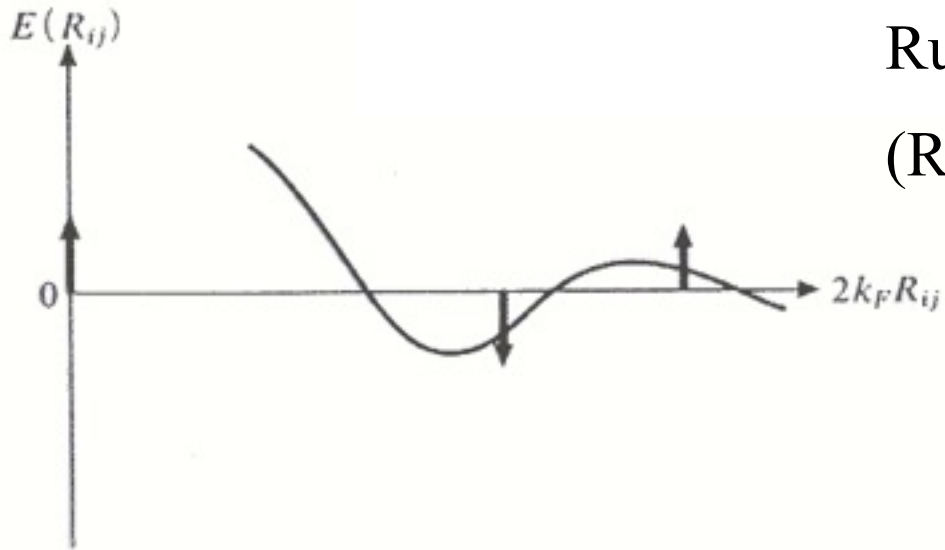
TRIUMF, University of British Columbia, Vancouver, British Columbia, Canada

(Received 22 June 1984)

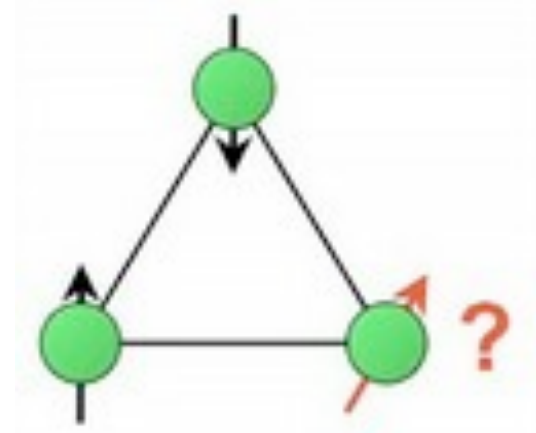
Phys. Rev. B31 (1985) 546 - 563



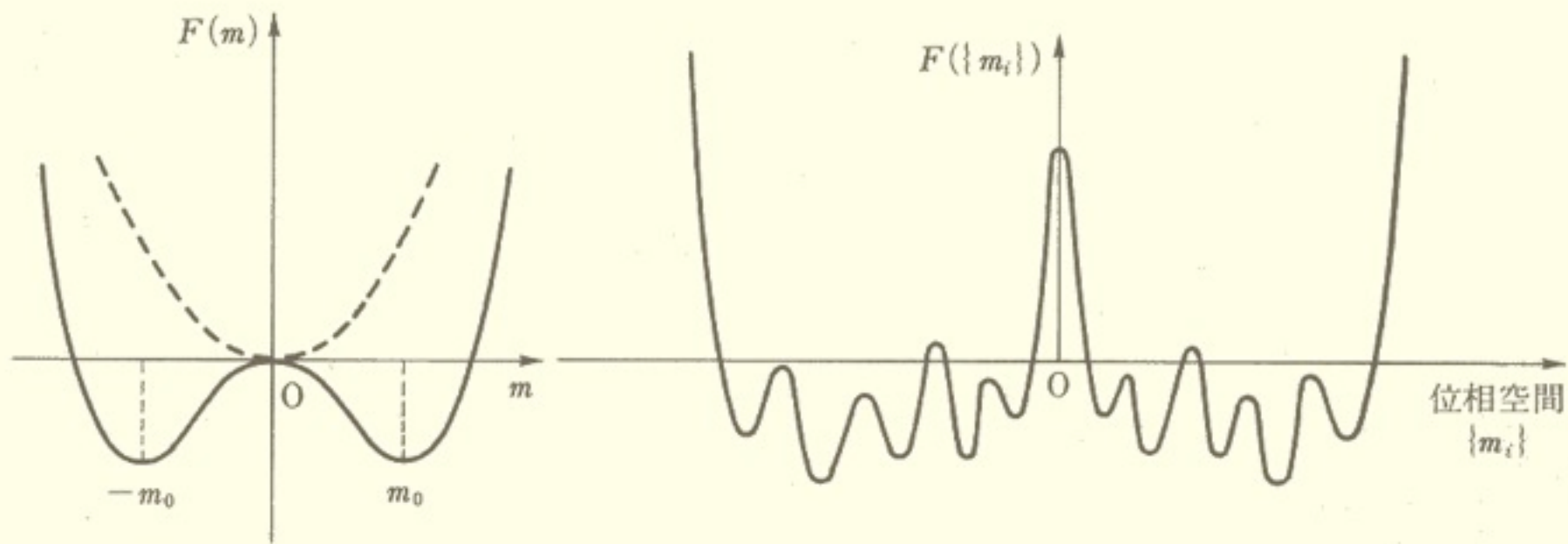
Ruderman-Kittel-Kasuya-Yoshida (RKKY) interaction



randomness in geometry



frustration



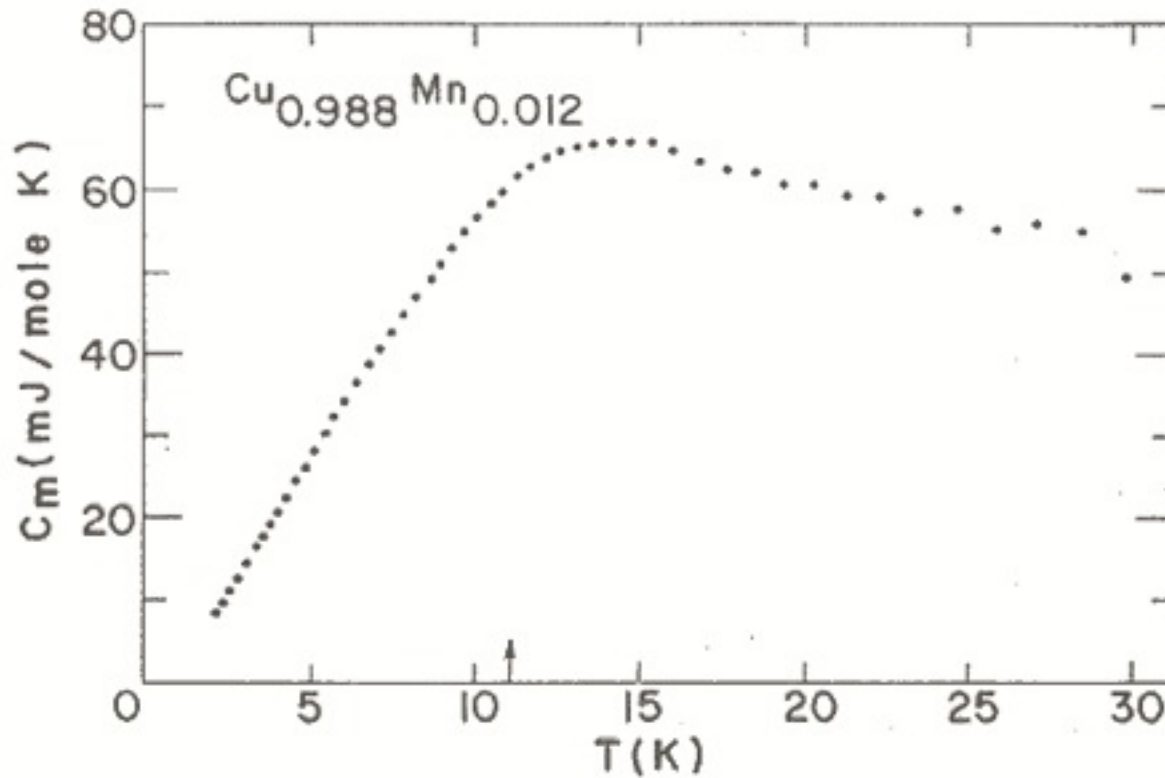
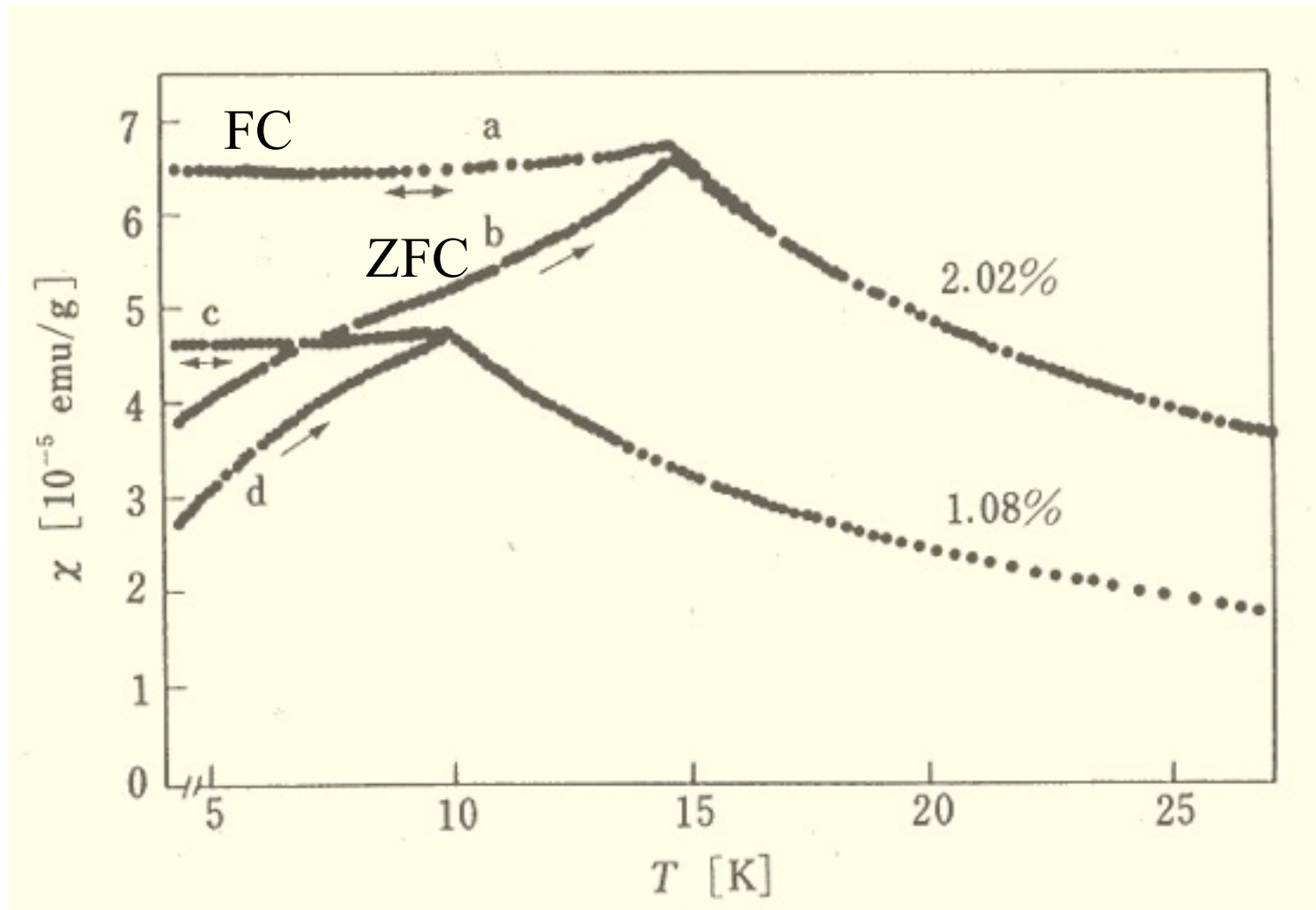


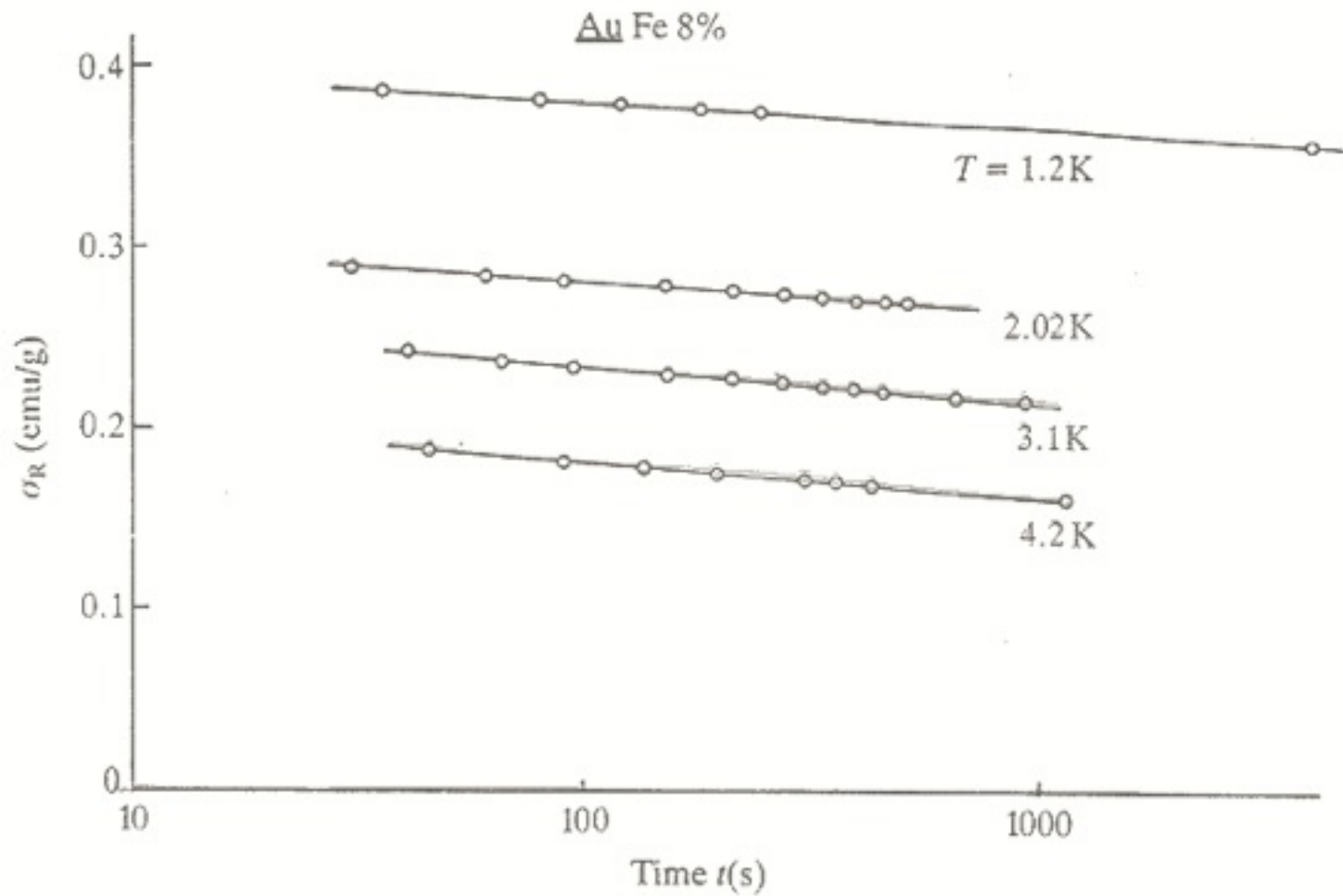
FIG. 3. Magnetic specific heat of $\text{Cu}_{0.988}\text{Mn}_{0.012}$ in the temperature range 2–30 K. The arrow indicates the ordering temperature T_0 .

no sharp feature in the specific heat

dc susceptibility of CuMn



Field-Cooling (FC) vs Zero-Field-Cooling (ZFC)



Time-dependent isothermal remanent magnetization

ac susceptibility depending on measuring frequency

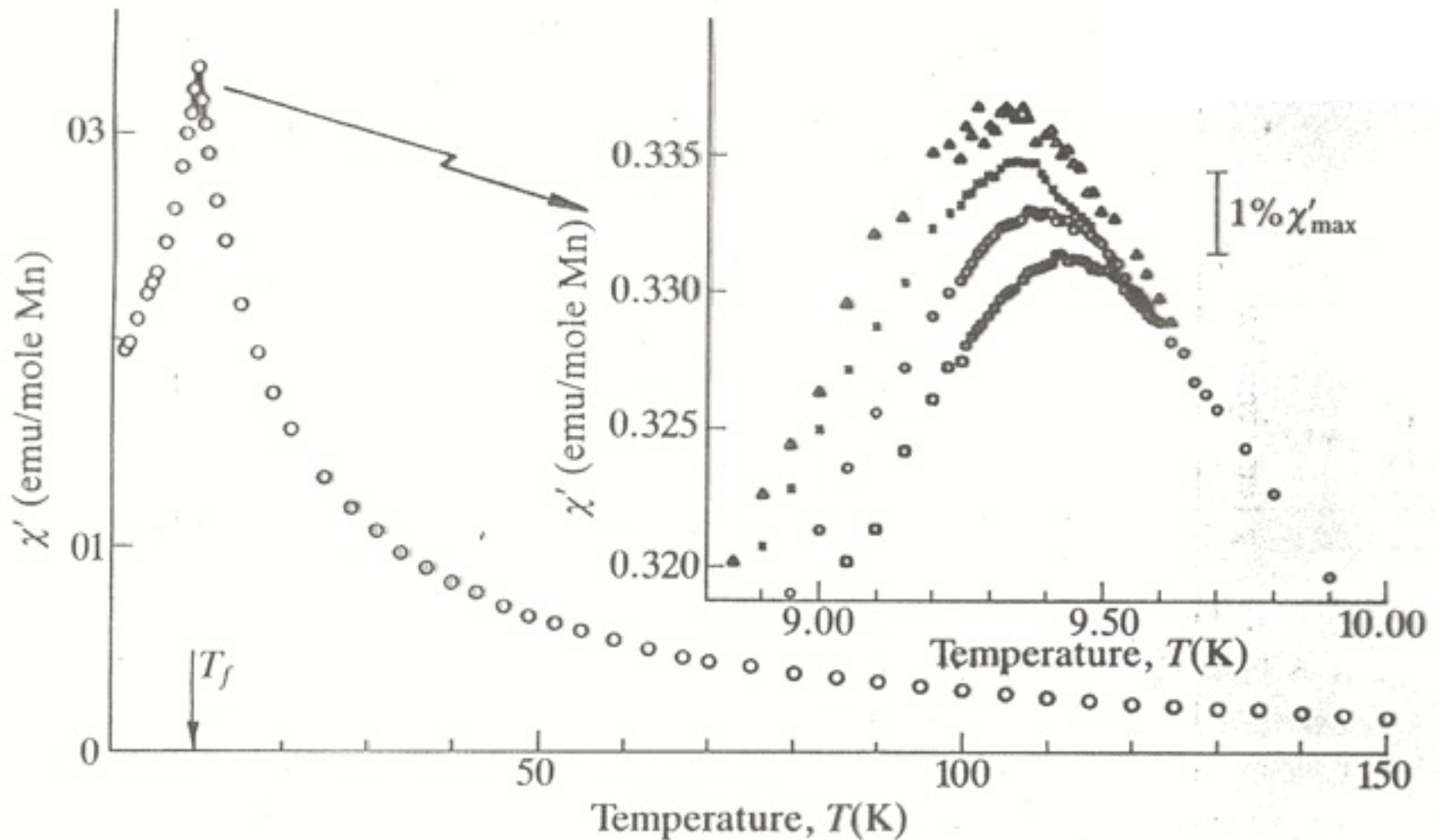
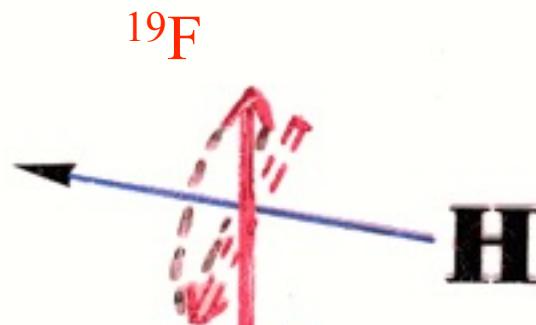
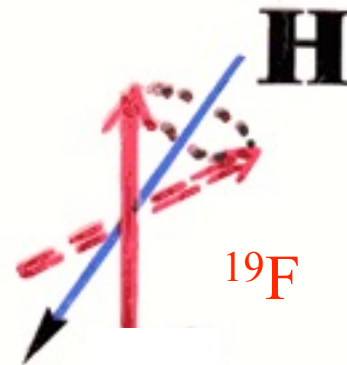
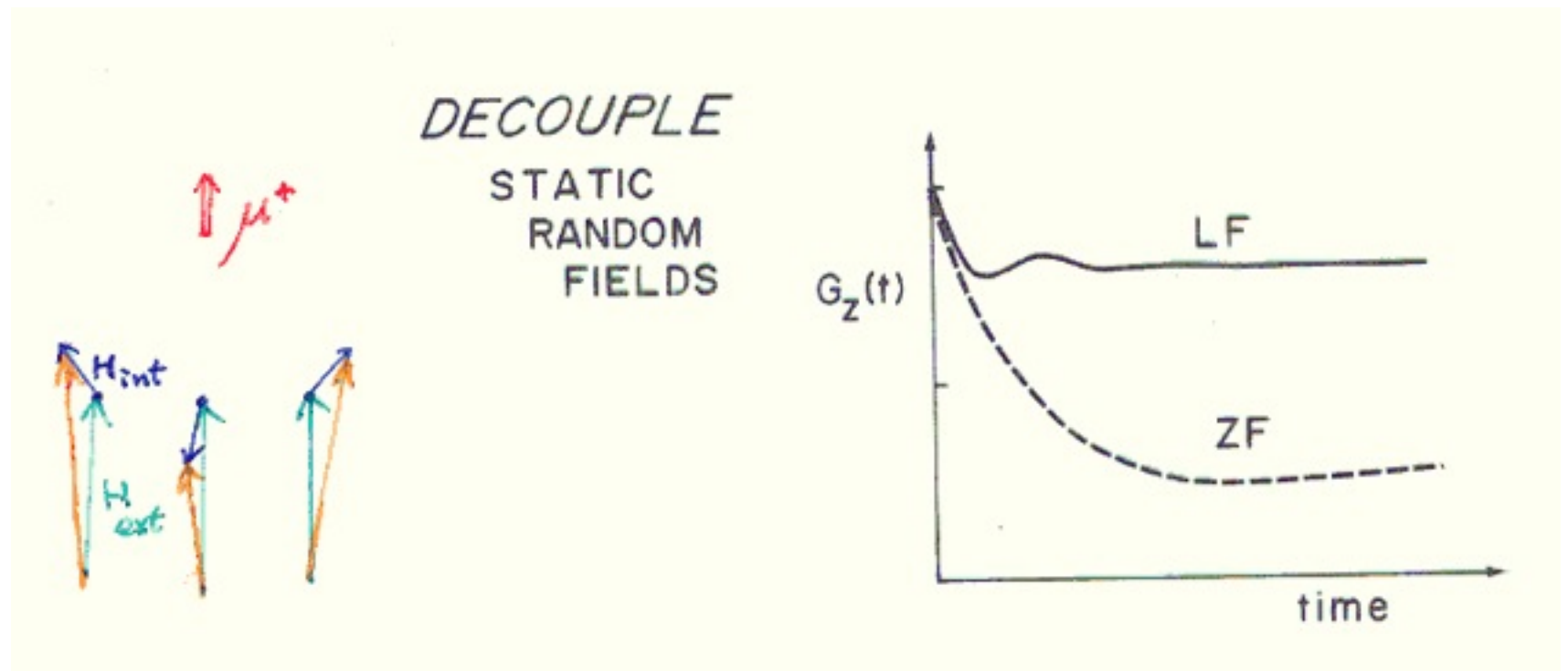


Figure 1.2: The ac susceptibility as a function of temperature for Cu-0.9% Mn for the frequencies 1.33 kHz ($\square$), 234 Hz ($\circ$), 10.4 Hz ($\times$), and 2.6 Hz ($\triangle$) (from Mulder et al, 1981, 1982).

RANDOM LOCAL FIELD H

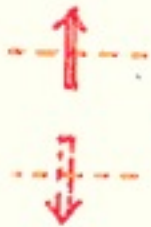


Distinguishing static versus dynamic effects

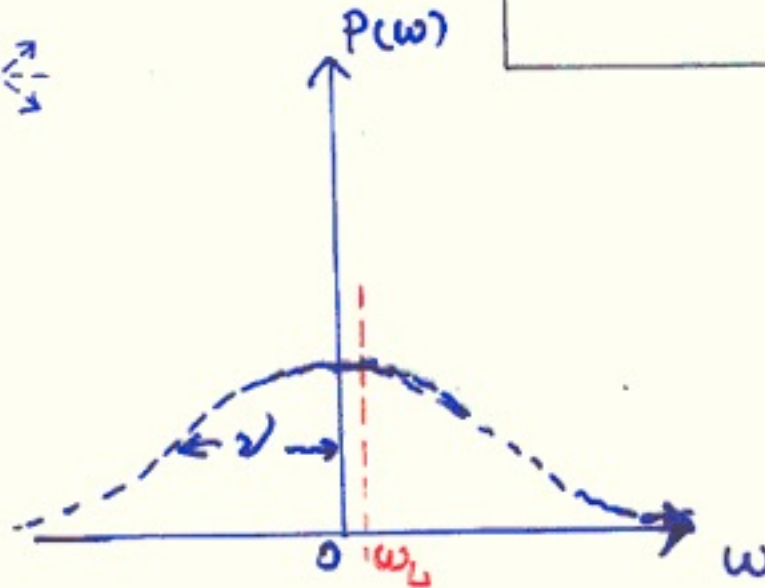
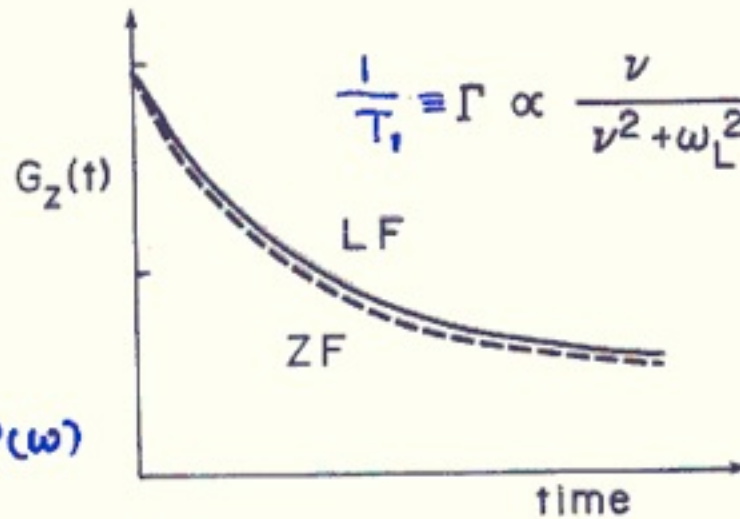


fluctuation rate ν

NO CHANGE
FAST
DYNAMIC
FIELDS



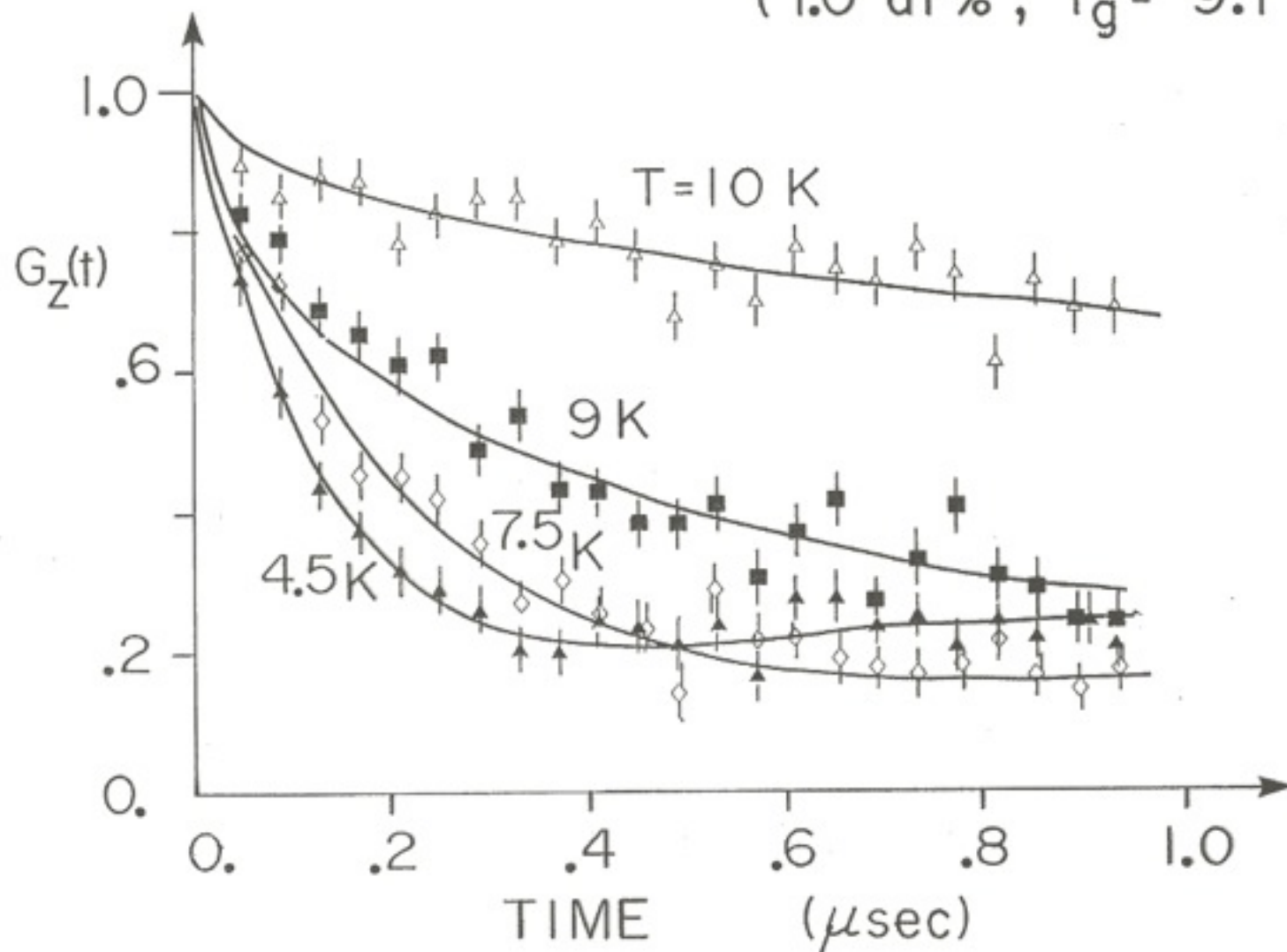
$$\omega_L = \gamma \mu H_{\text{ext}}$$



Noise power
spectrum $P(\omega)$

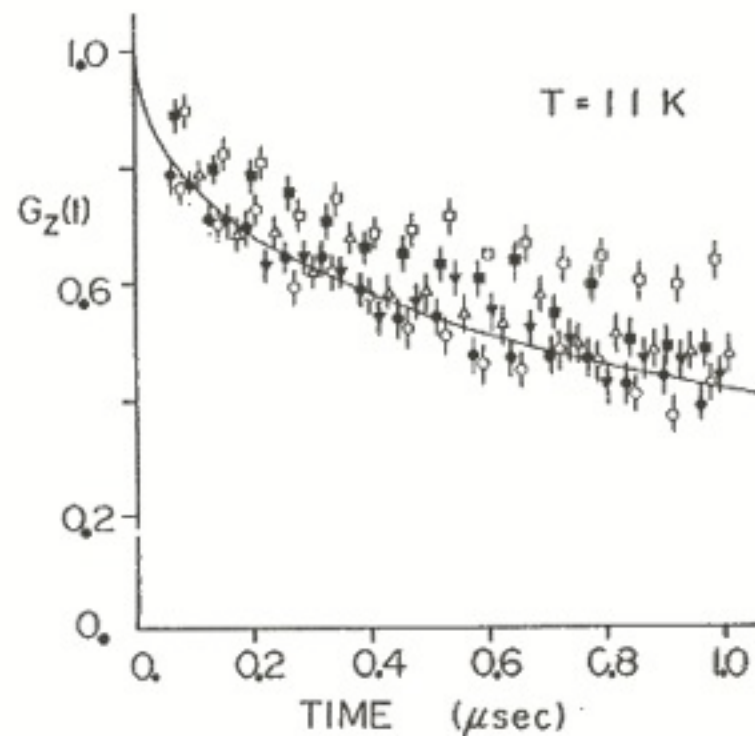
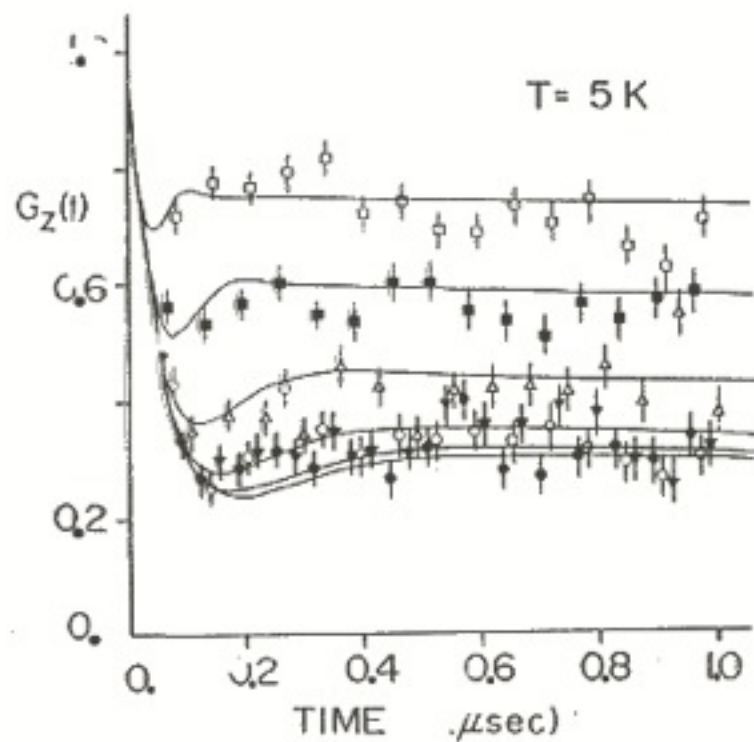
ZF- μ SR in AuFe

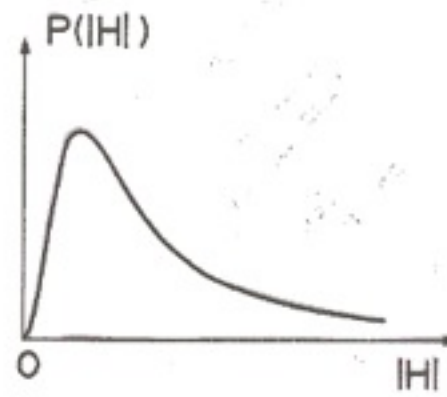
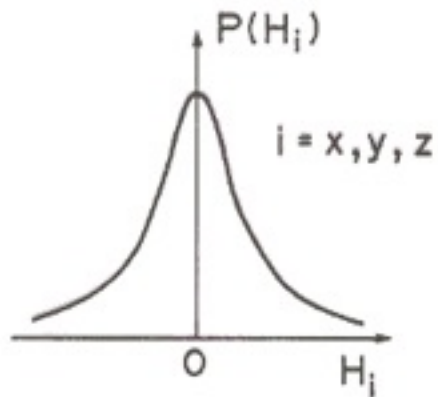
(1.0 at % , $T_g = 9.1$ K)



CuMn (1.1 at%) $T_g = 10.8 \text{ K}$

H_L (Oe) = • 0 ◊ 40 ▼ 80 ▲ 160 ■ 320 ◻ 640

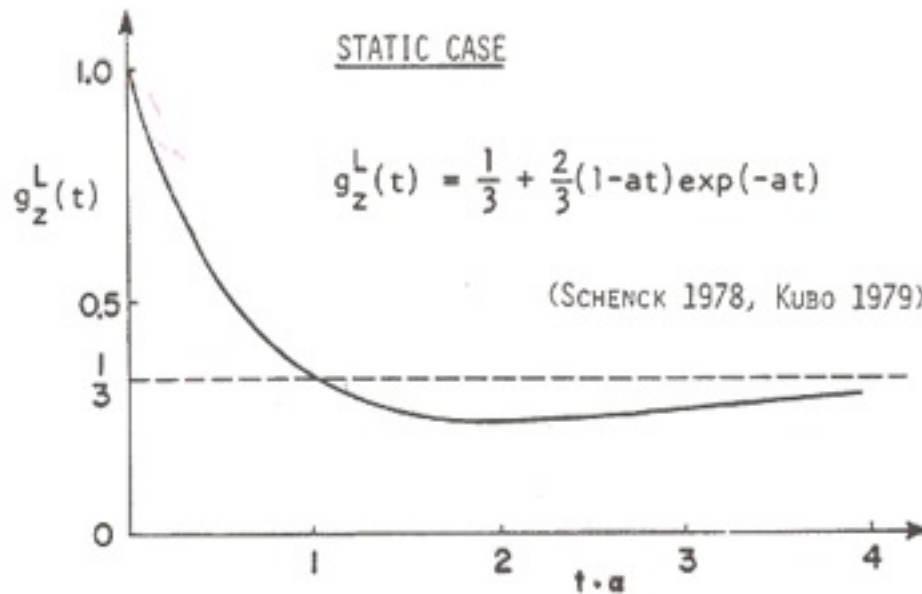




Lorentzian

$$P^L(H_i) = \frac{\gamma_\mu}{\pi} \cdot \frac{a}{(a^2 + \gamma_\mu^2 H_i^2)}$$

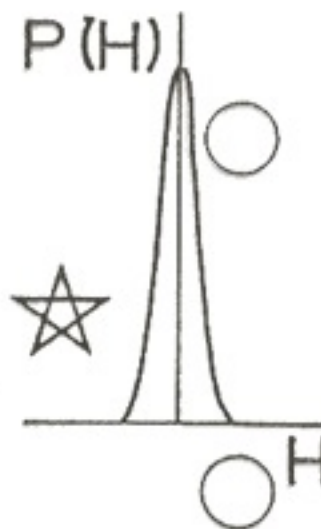
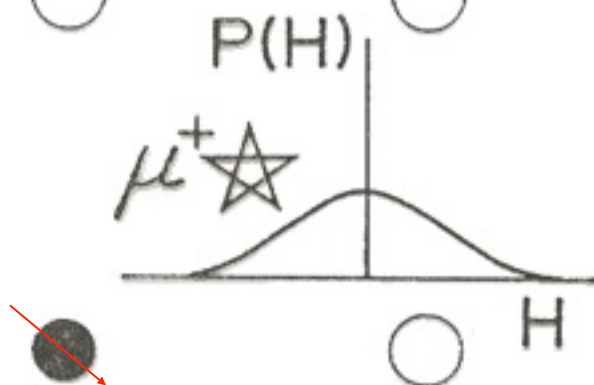
(WALSTEDT & WALKER, 1974)

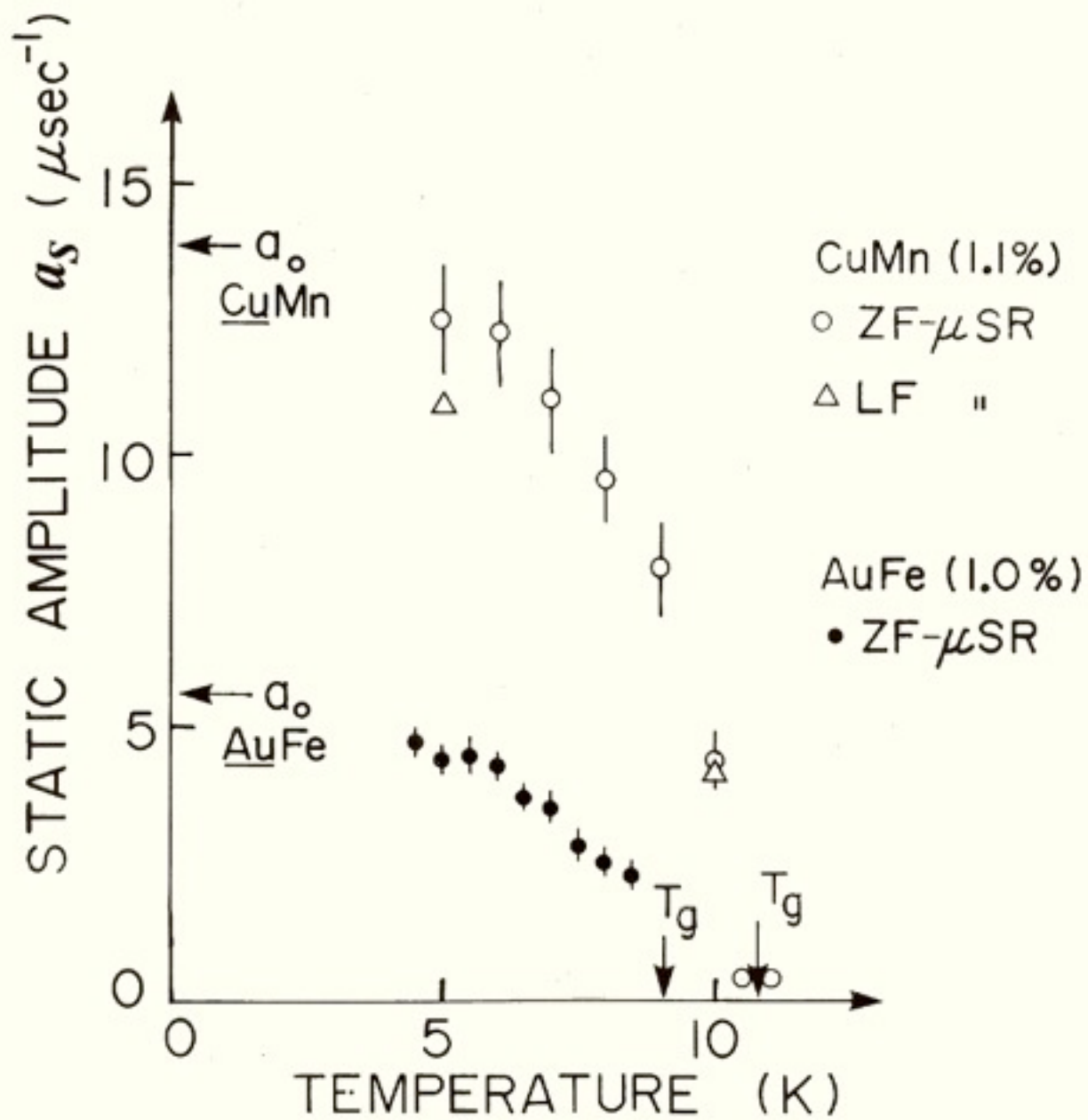


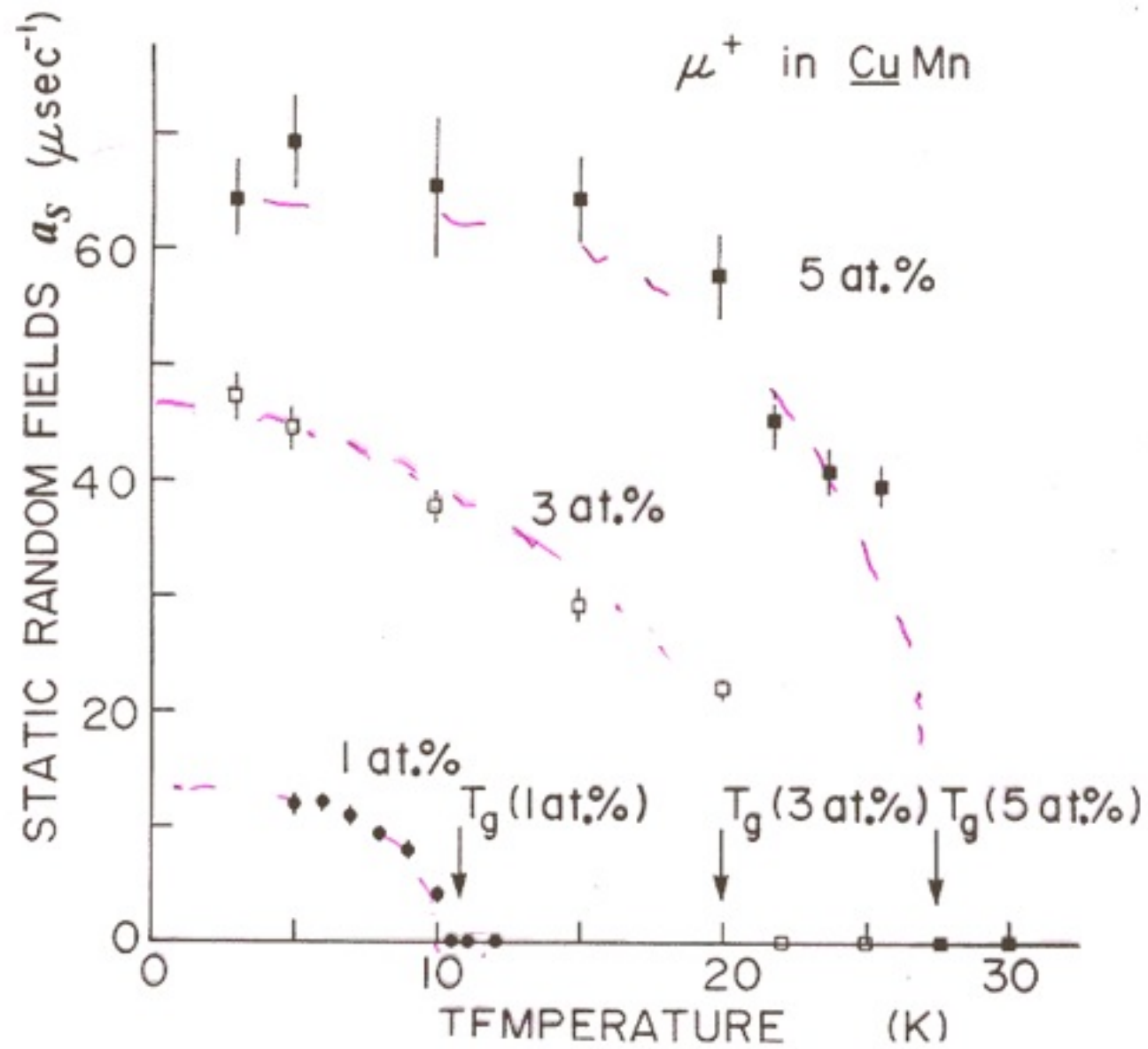
Au

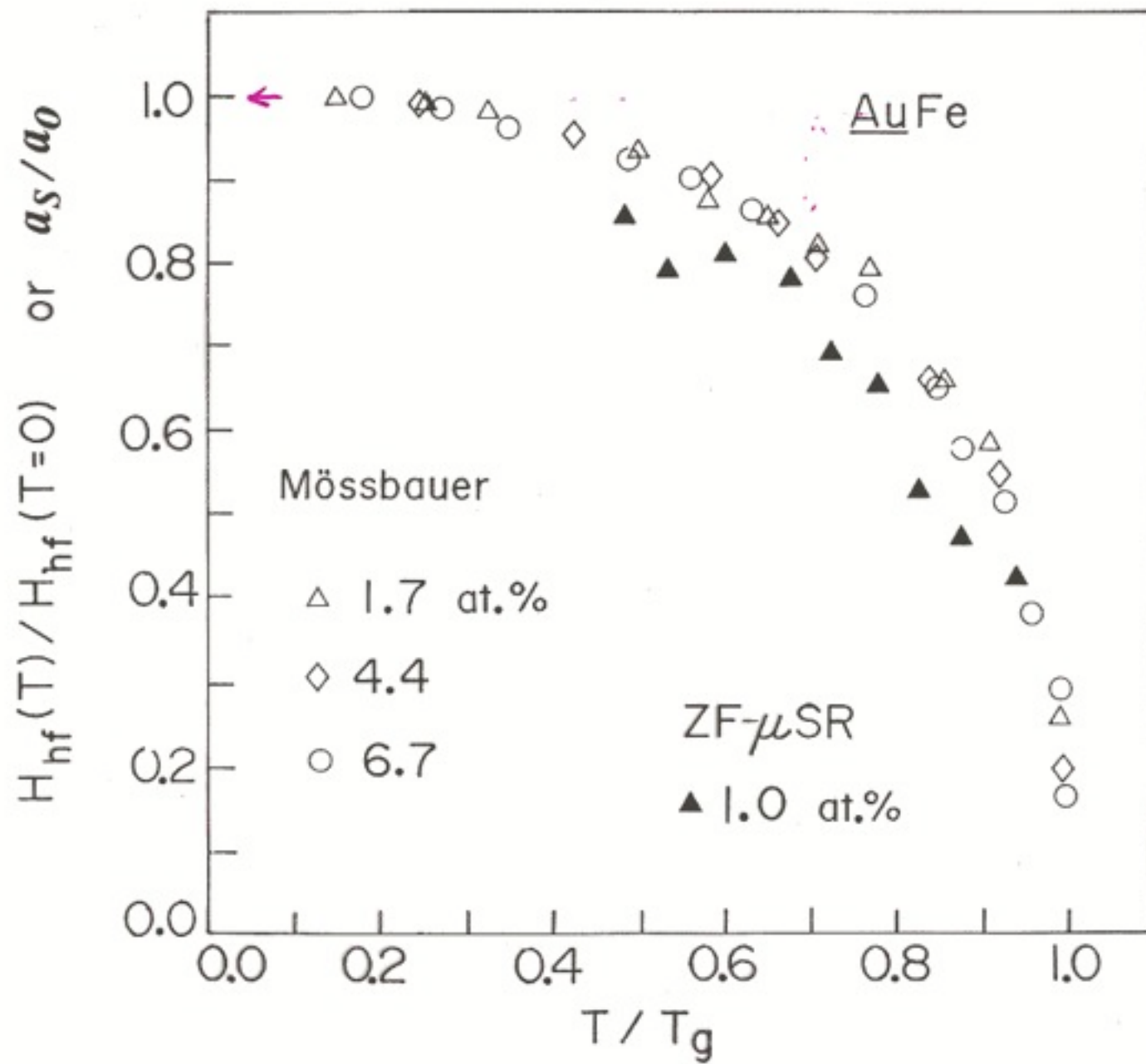


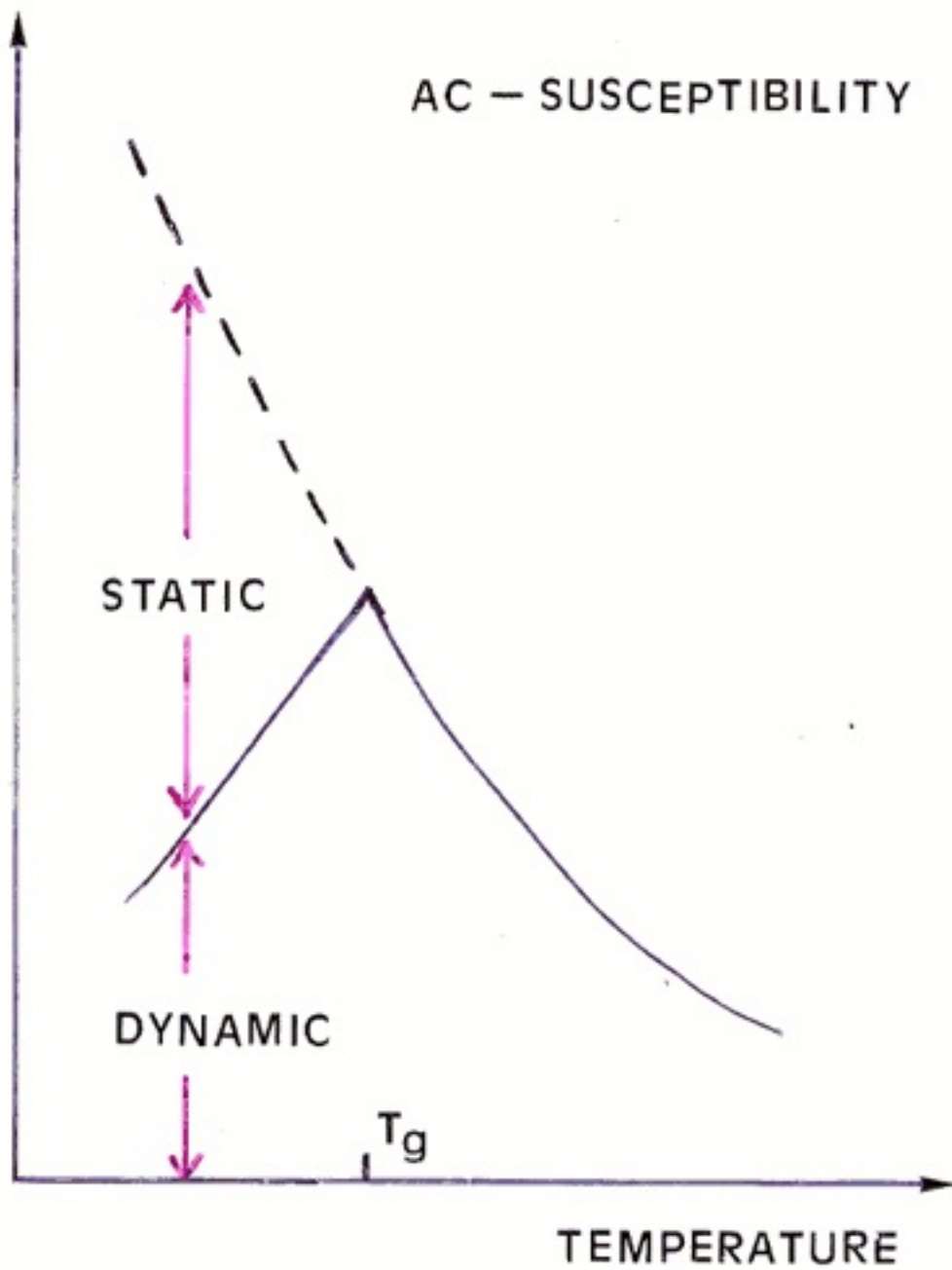
Fe







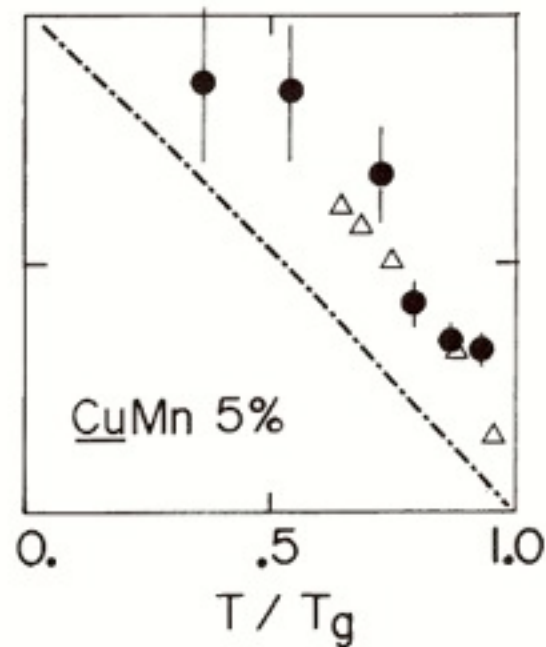
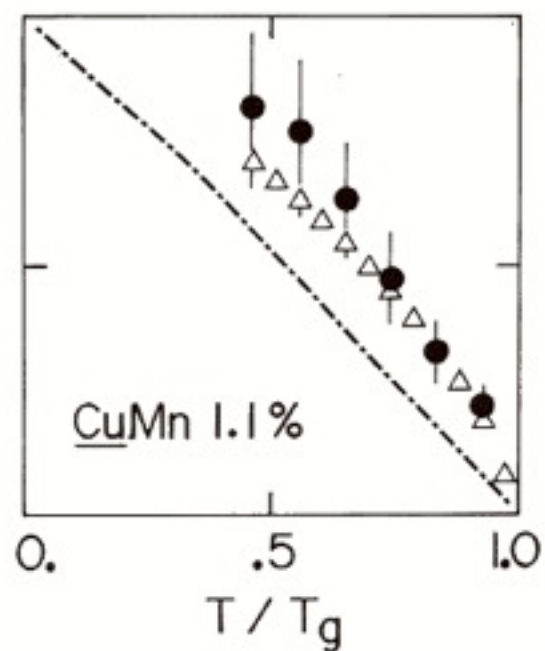
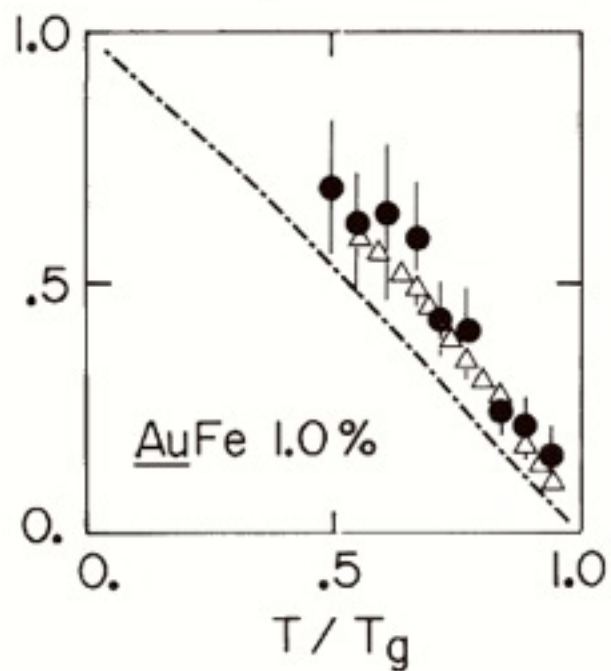




● ZF- μ SR $(a_s/a_o)^2$

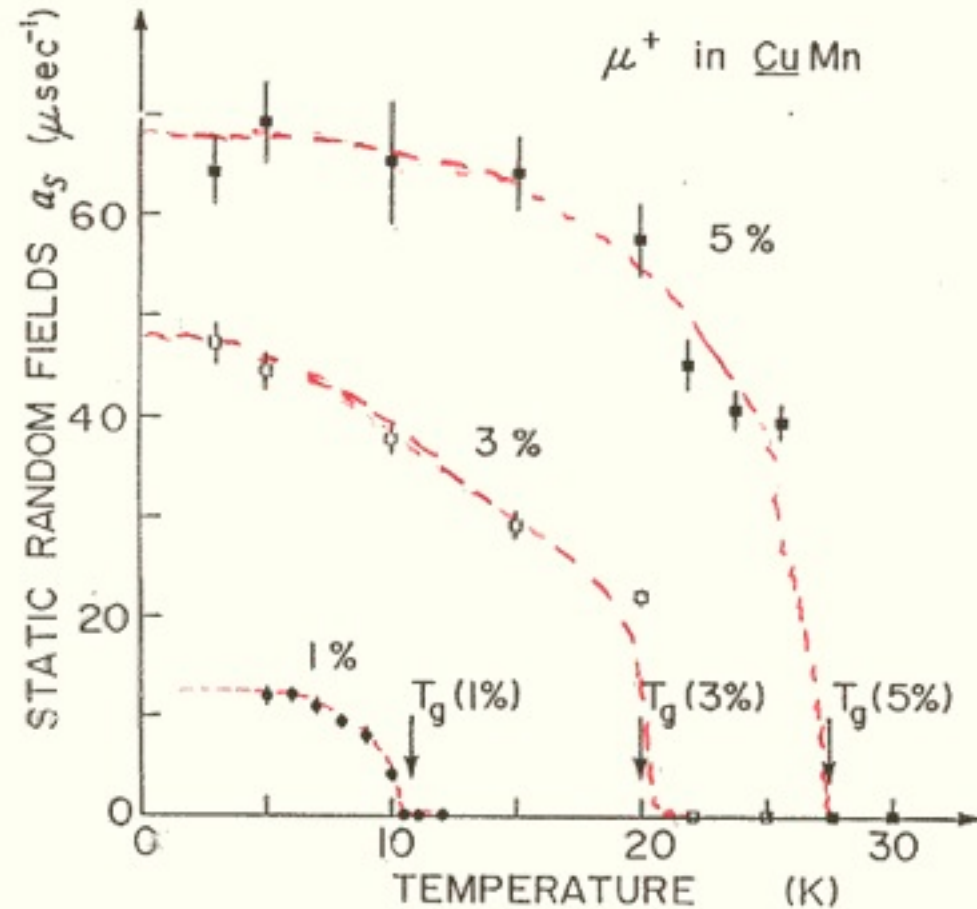
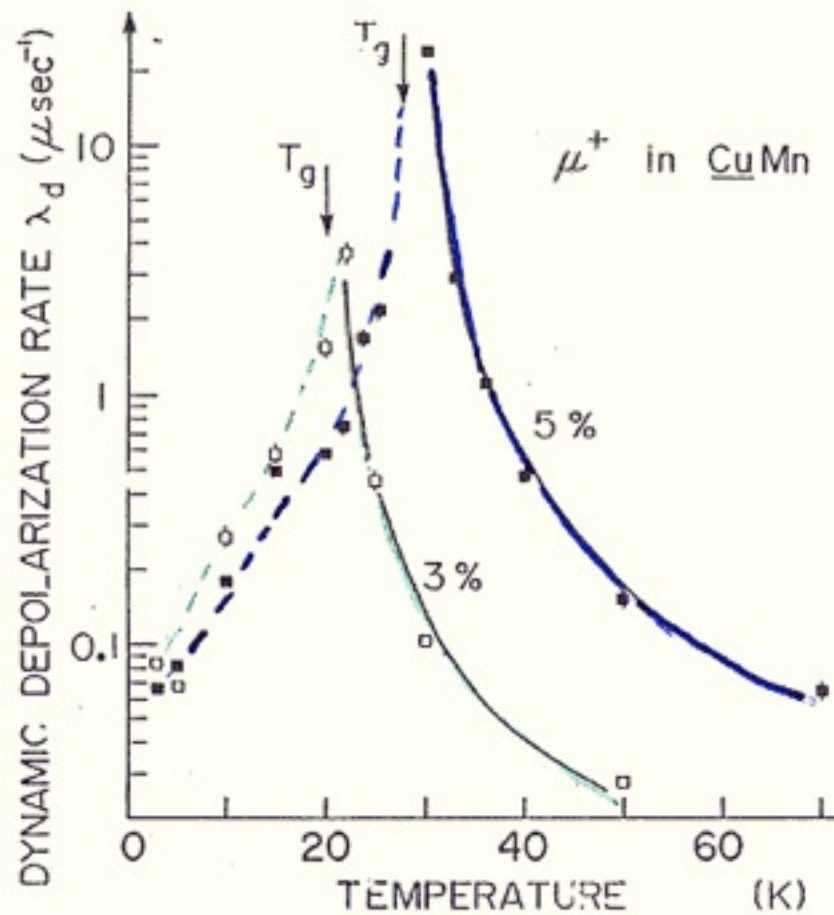
△ ac-Sus $(1-x/x_{\text{Curie}})$

----- S-K Model $Q(T)$



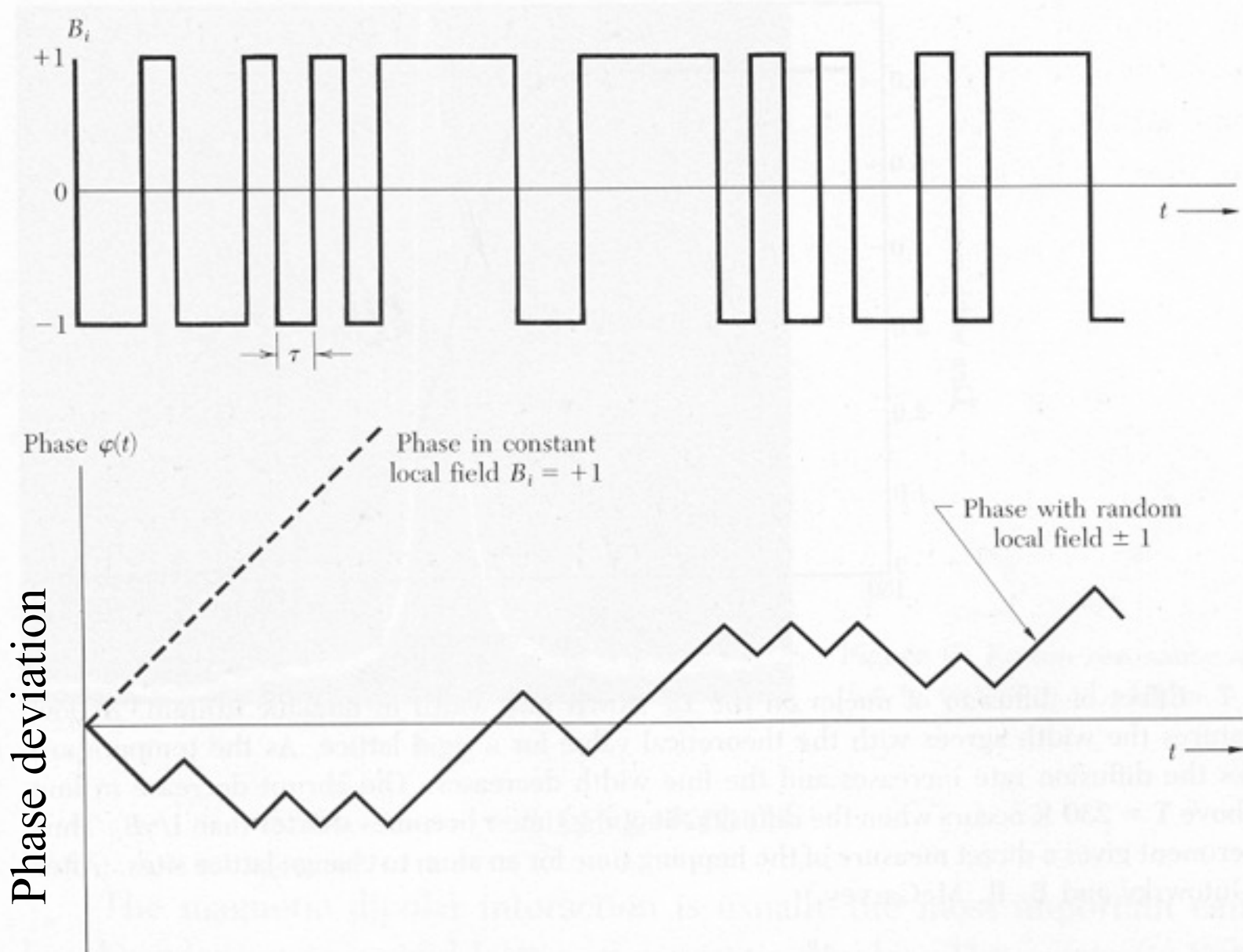
$$\propto \frac{1}{T_1}$$

$$\propto \sqrt{Q_{EA}}$$

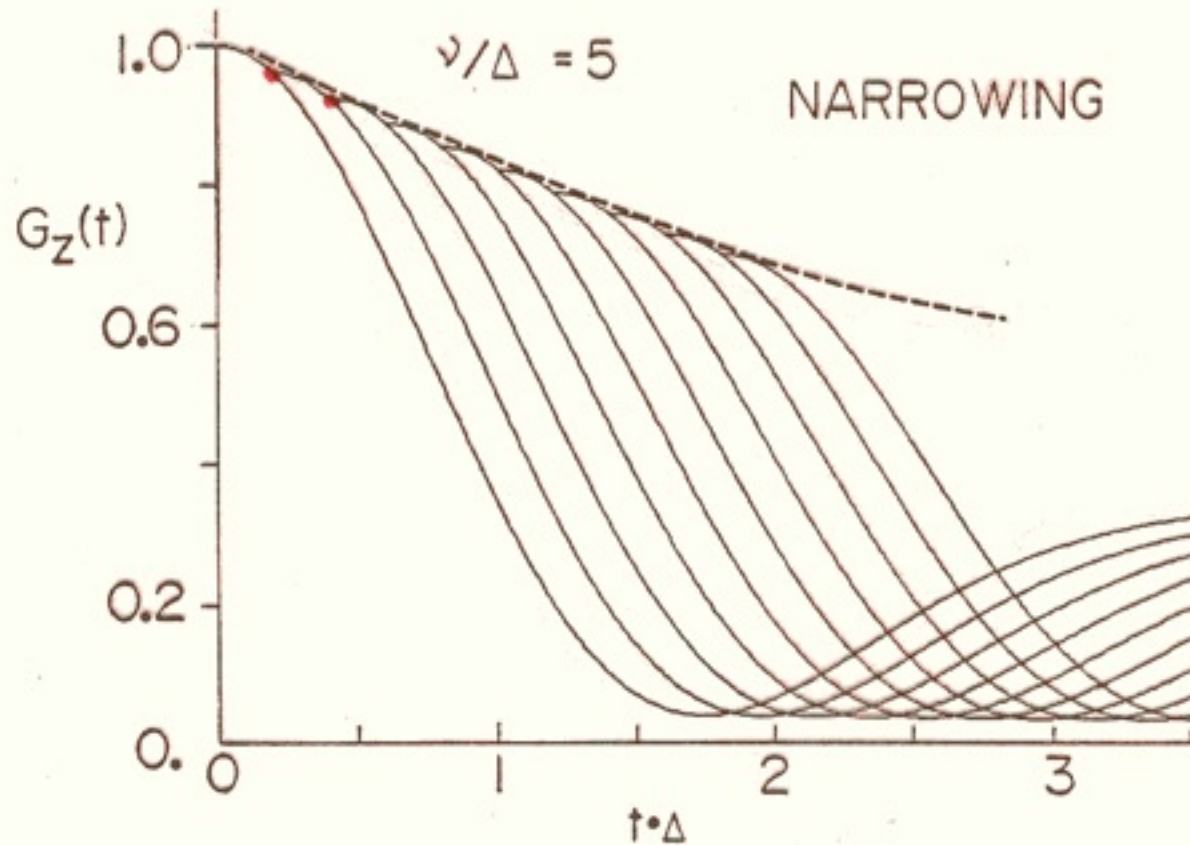


$$1/T_1 \sim a_s^2 / \nu$$

Mn spin fluctuations → Brownian motion of nuclear spin precession



STRONG COLLISION MODEL



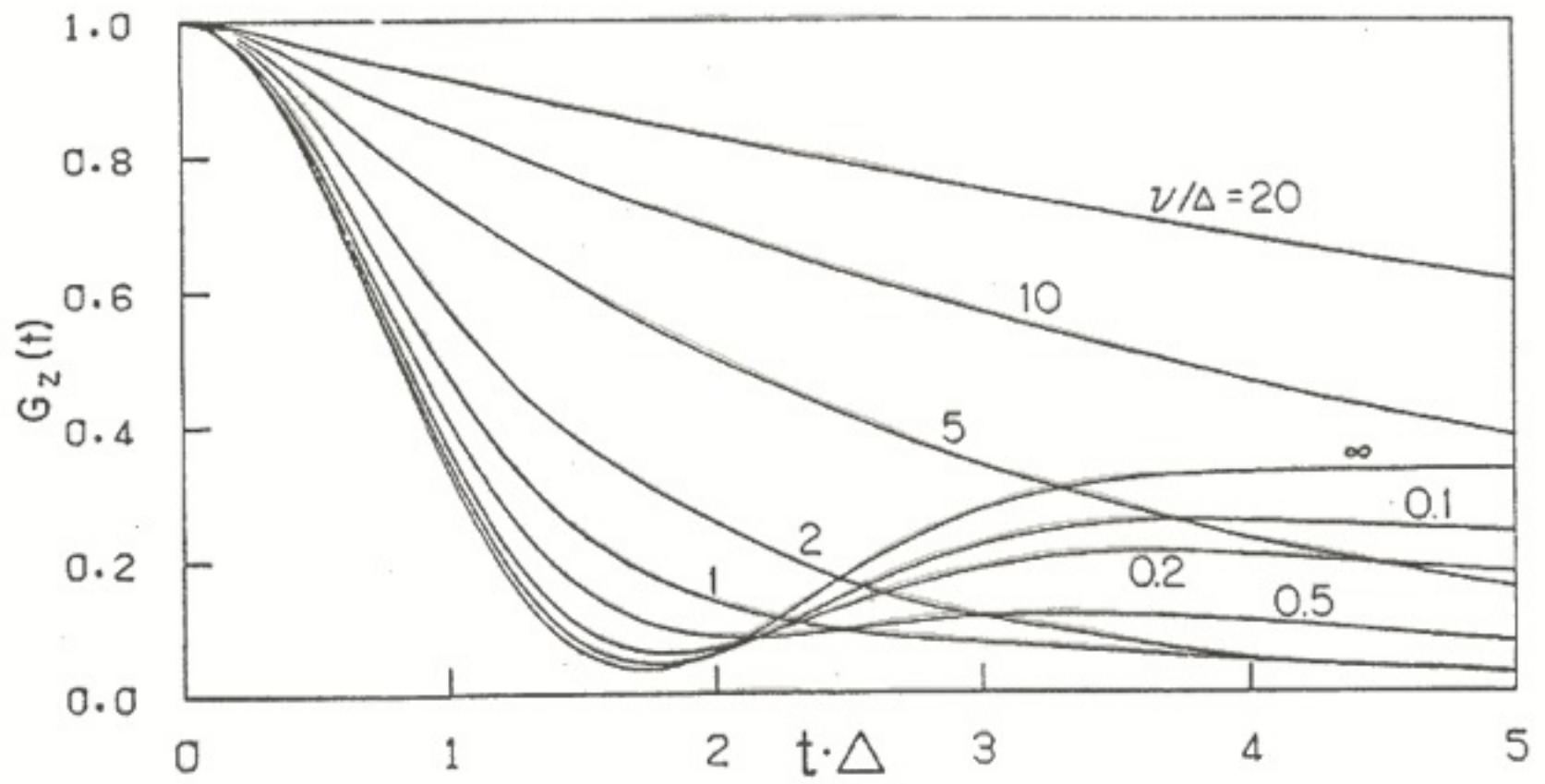
Static Gaussian Field

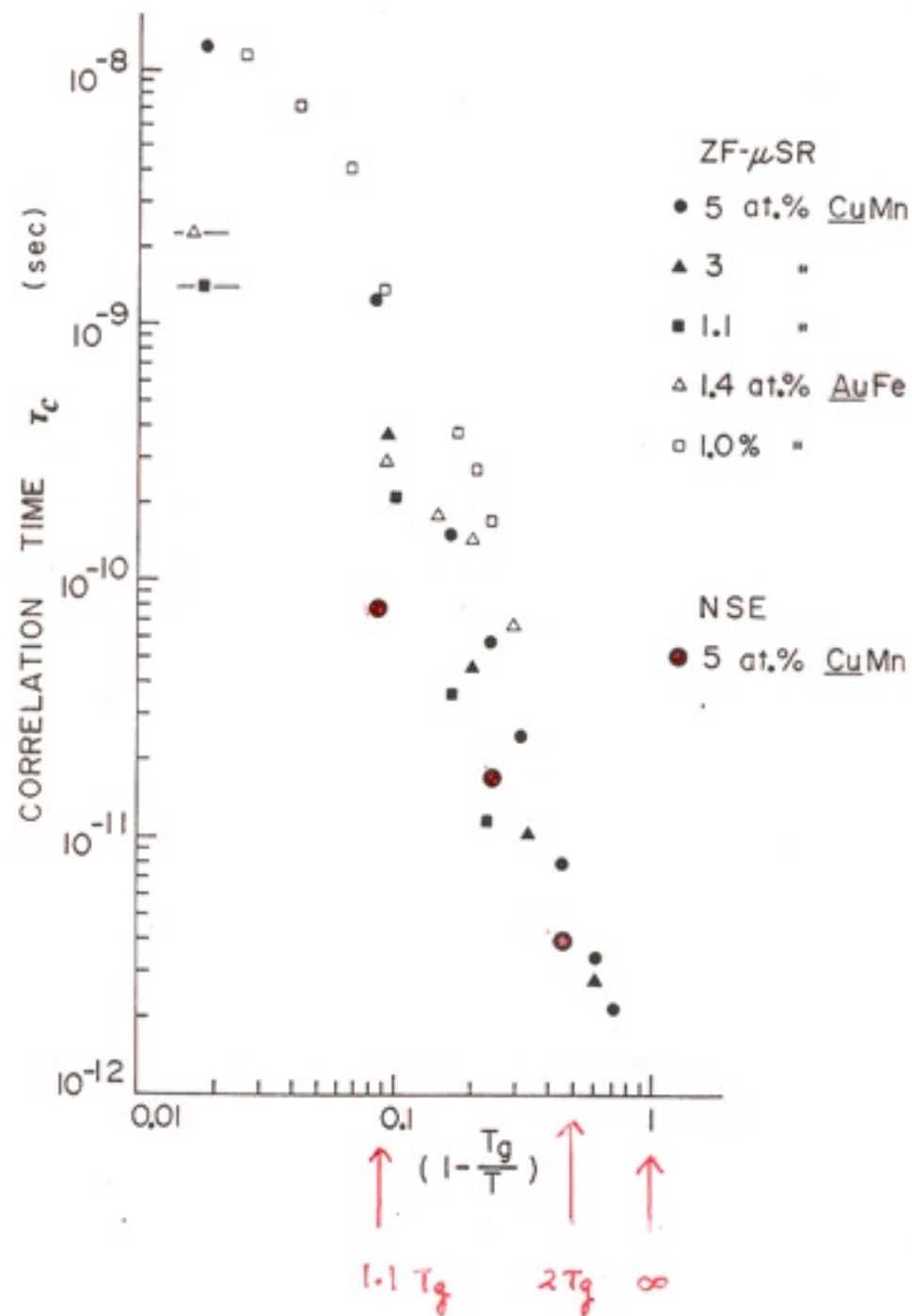
→ $G_z(t) \sim \exp(-\Delta^2 t^2)$
near $t \sim 0$

Dynamic field makes
it into

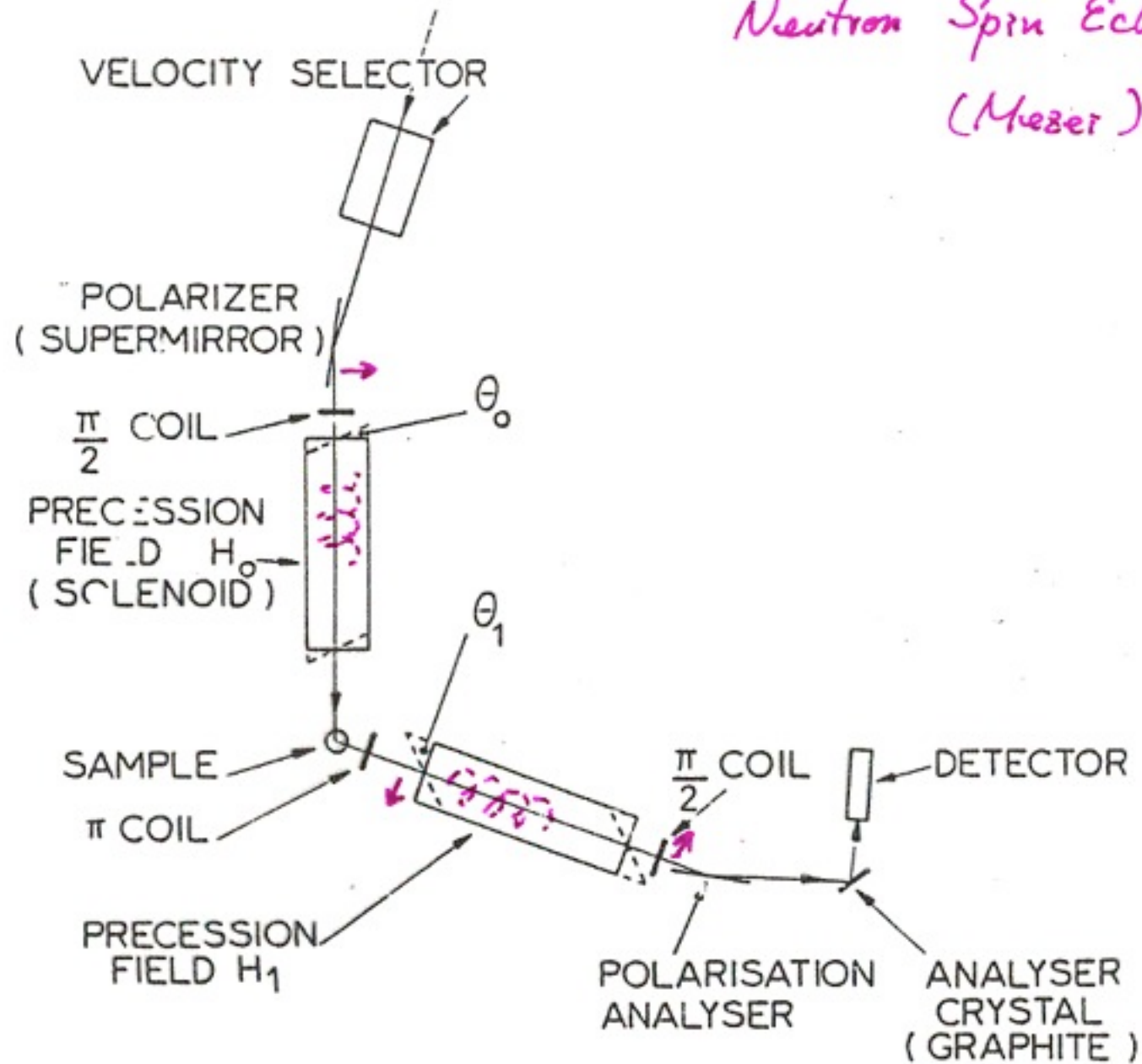
$G_z(t) \sim \exp(-t/T_1)$

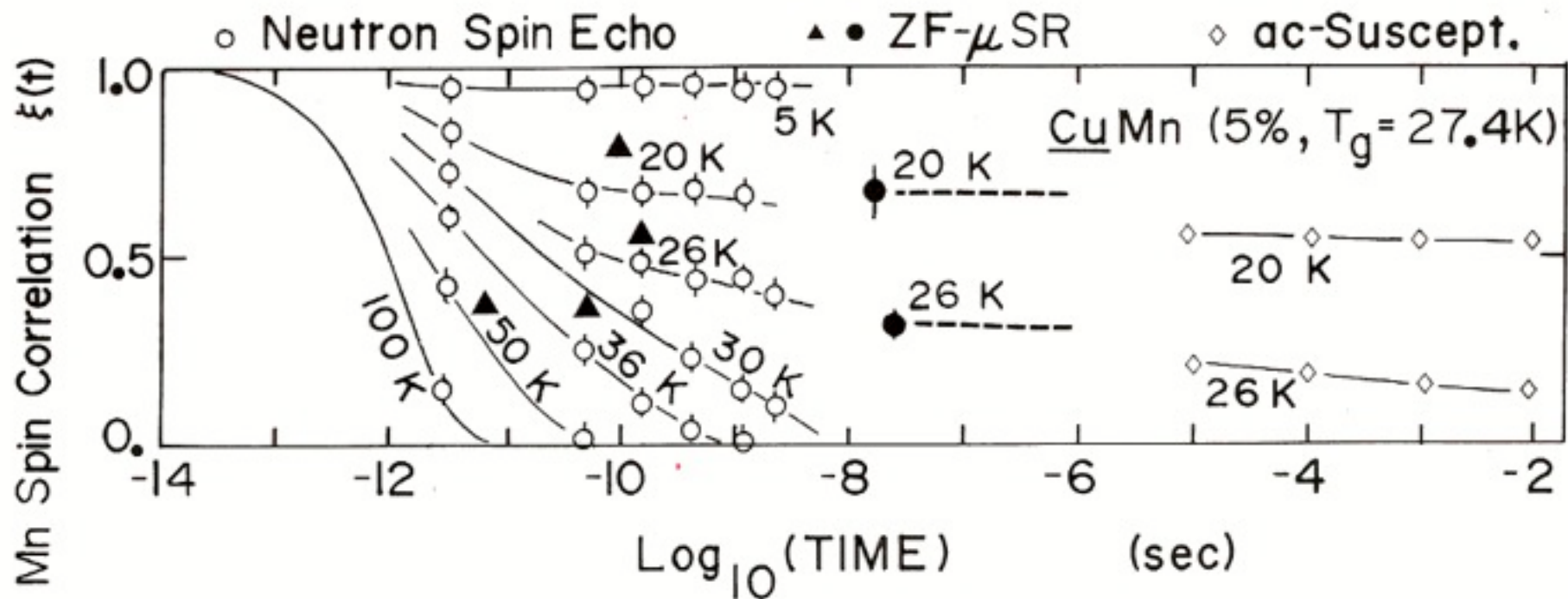
$$G_z(t, \nu) = \exp(-\nu t) \left\{ g_z(t) + \nu \int_0^t g_z(t_1) g_z(t-t_1) dt_1 + \nu^2 \int_0^t \int_0^{t_1} g_z(t_1) g_z(t_2-t_1) g_z(t-t_2) dt_1 dt_2 + \dots \right\}$$





Neutron Spin Echo (Mezer)





**Muon spin relaxation studies of incommensurate magnetism and superconductivity
in stage-4 $\text{La}_2\text{CuO}_{4.11}$ and $\text{La}_{1.88}\text{Sr}_{0.12}\text{CuO}_4$**

A. T. Savici, Y. Fudamoto, I. M. Gat, T. Ito, M. I. Larkin, and Y. J. Uemura*

Department of Physics, Columbia University, New York, New York 10027

G. M. Luke

Department of Physics and Astronomy, McMaster University, Hamilton, Ontario, Canada L8P 4N3

K. M. Kojima

Department of Superconductivity, Faculty of Engineering, University of Tokyo, 7-3-1 Hongo, Tokyo 113-8656, Japan

Y. S. Lee and M. A. Kastner

Department of Physics, MIT, Cambridge, Massachusetts 02139

R. J. Birgeneau

Department of Physics, MIT, Cambridge, Massachusetts 02139

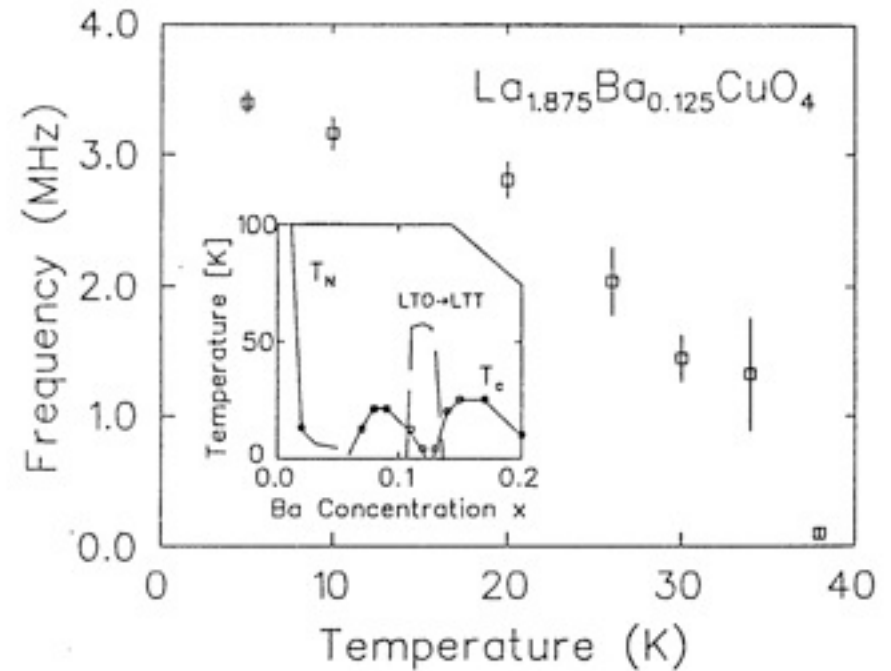
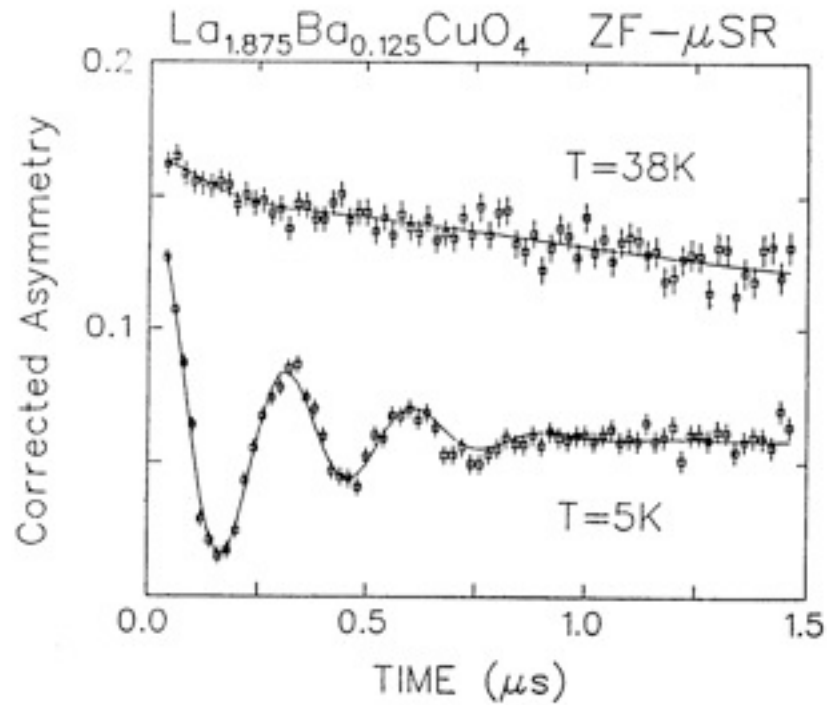
and Department of Physics, University of Toronto, Toronto, Ontario, Canada M5S 1A7

K. Yamada

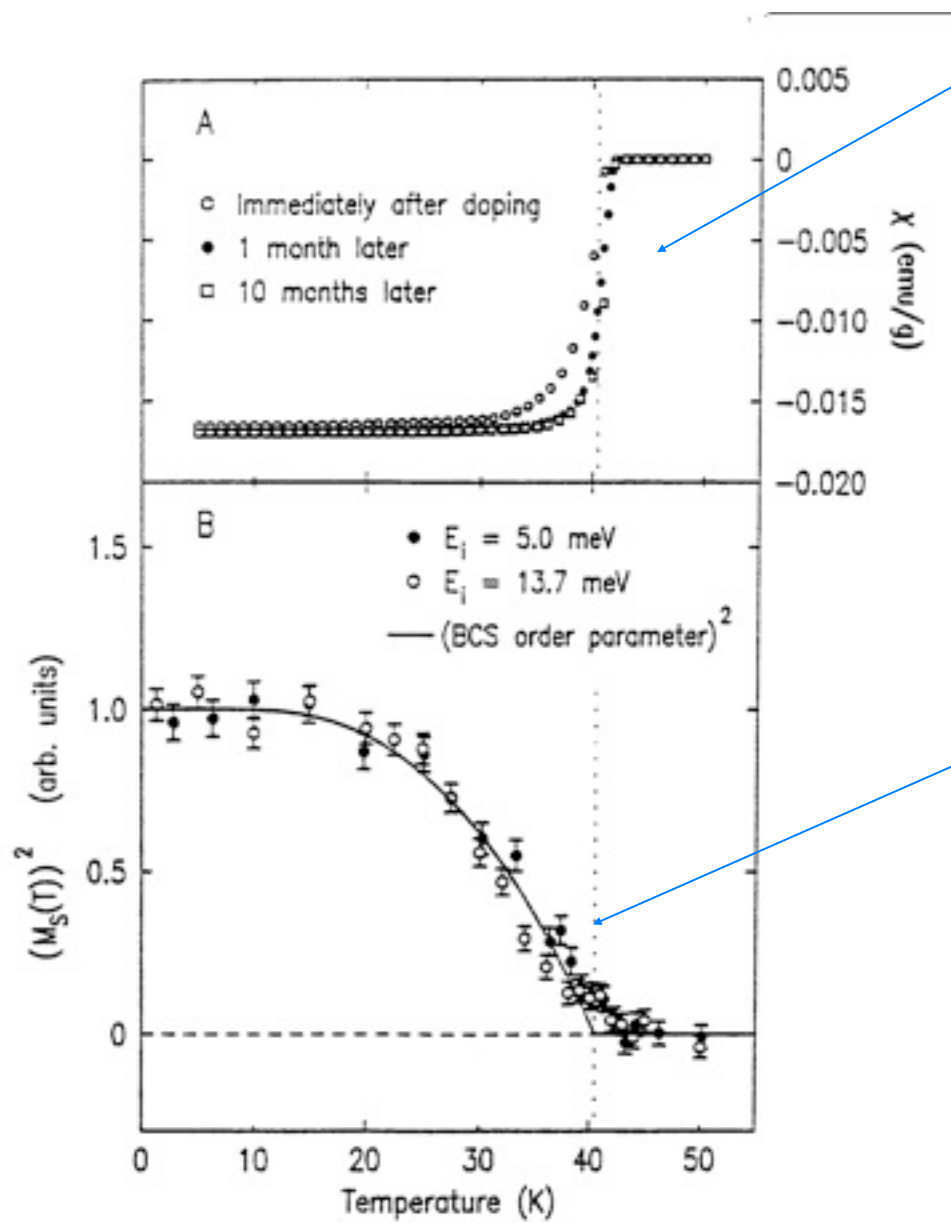
Institute for Chemical Research, Kyoto University, Uji, Kyoto 611-0011, Japan

(Received 1 February 2002; published 16 July 2002)

static magnetism in the stripe : 1/8 systems ZF- μ SR



Luke et al., 1991



$T_C = 42$ K

Stage-4 $\text{La}_2\text{CuO}_{4.11}$

from MIT

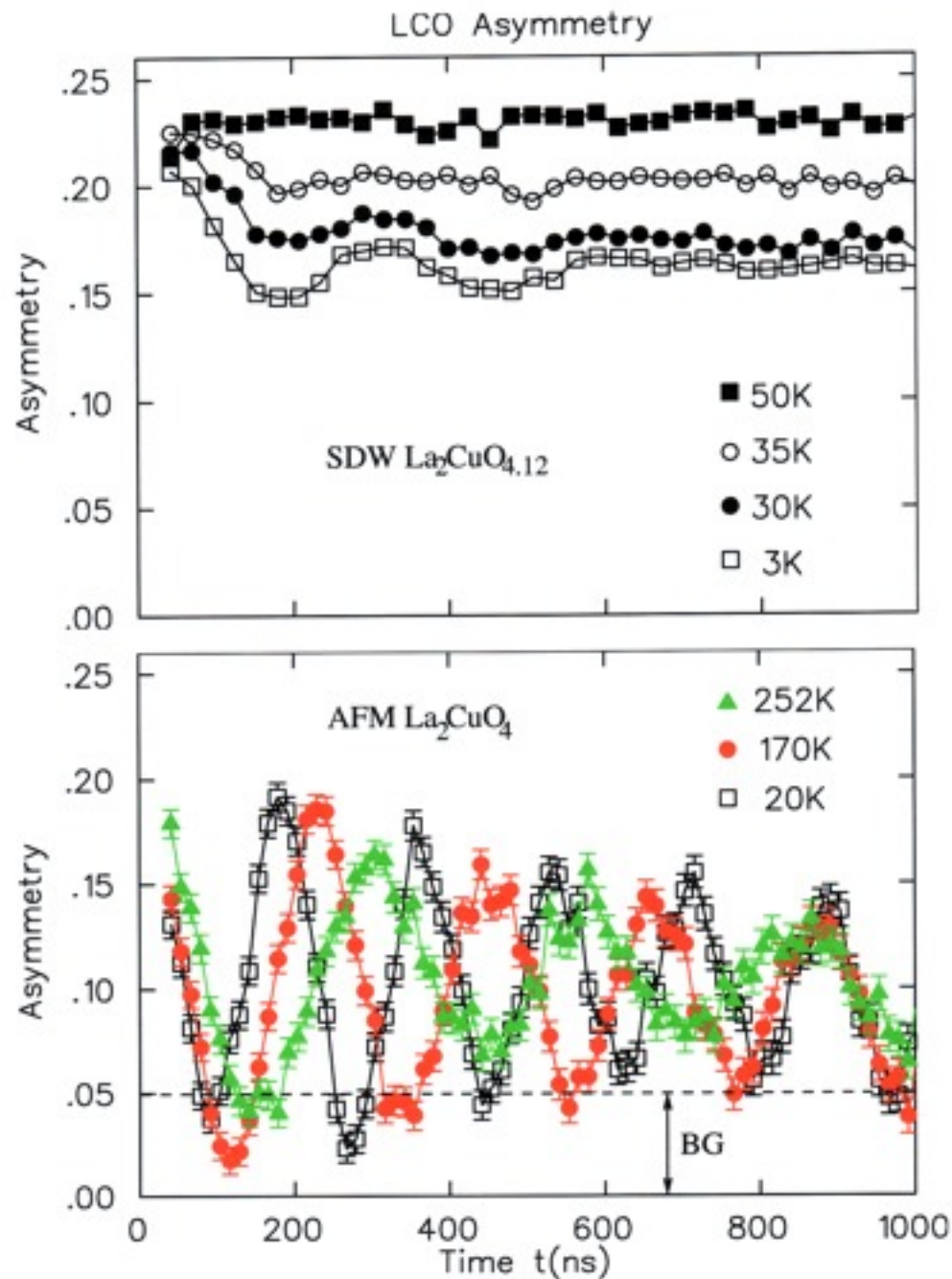
$T_N = 42$ K

sharp satellite Bragg peak
long range spin correlations

ZF- μ SR

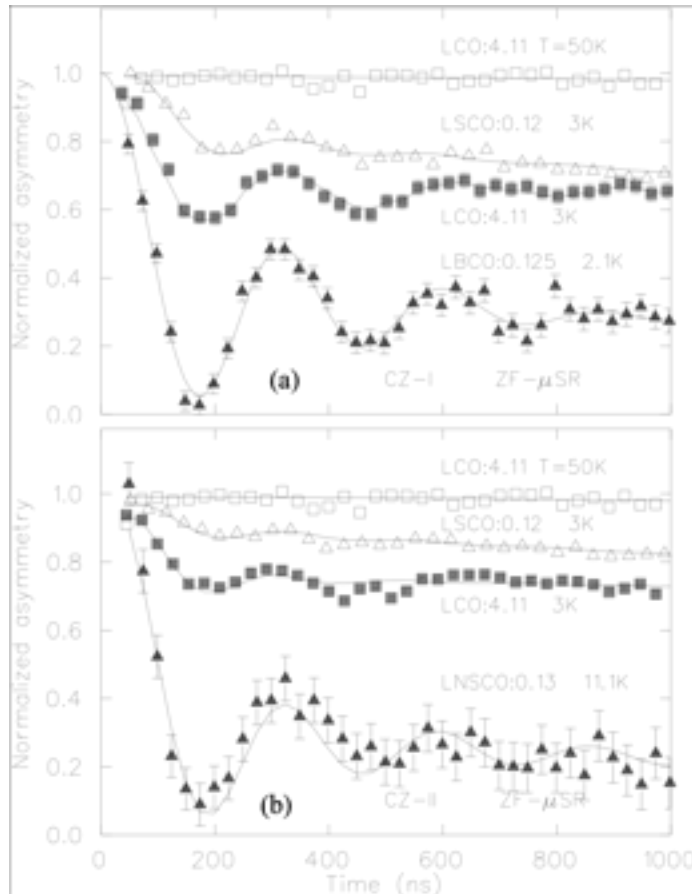
Finite Volume Fraction

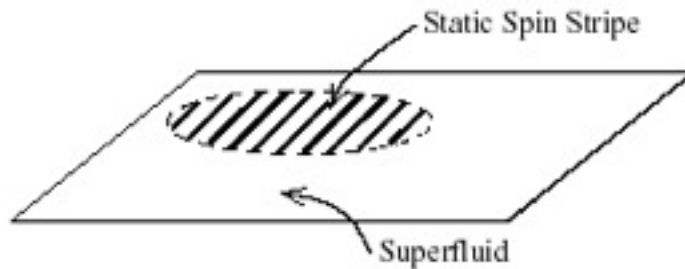
Full Volume Fraction



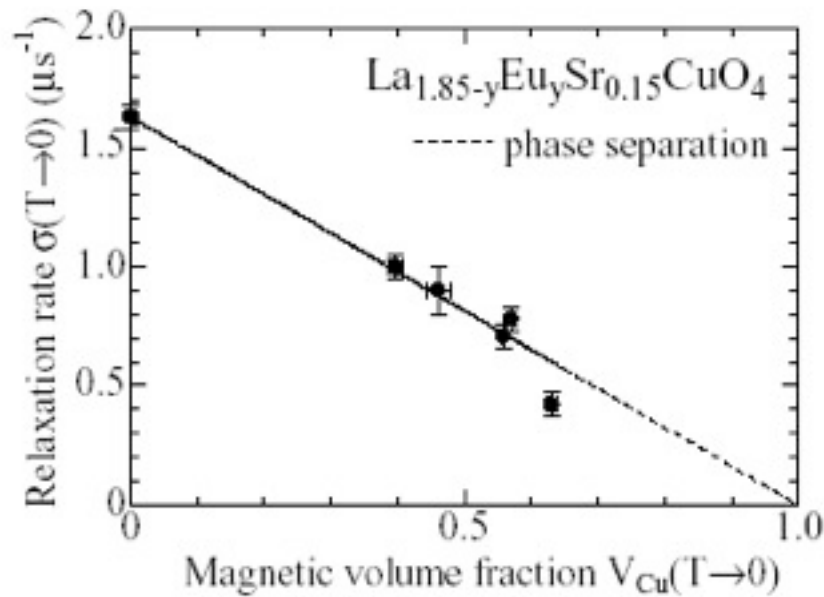
Stripe systems: ZF- μ SR

in LCO:4.11, LSCO:0.12





Trade-off between magnetic volume and superfluid

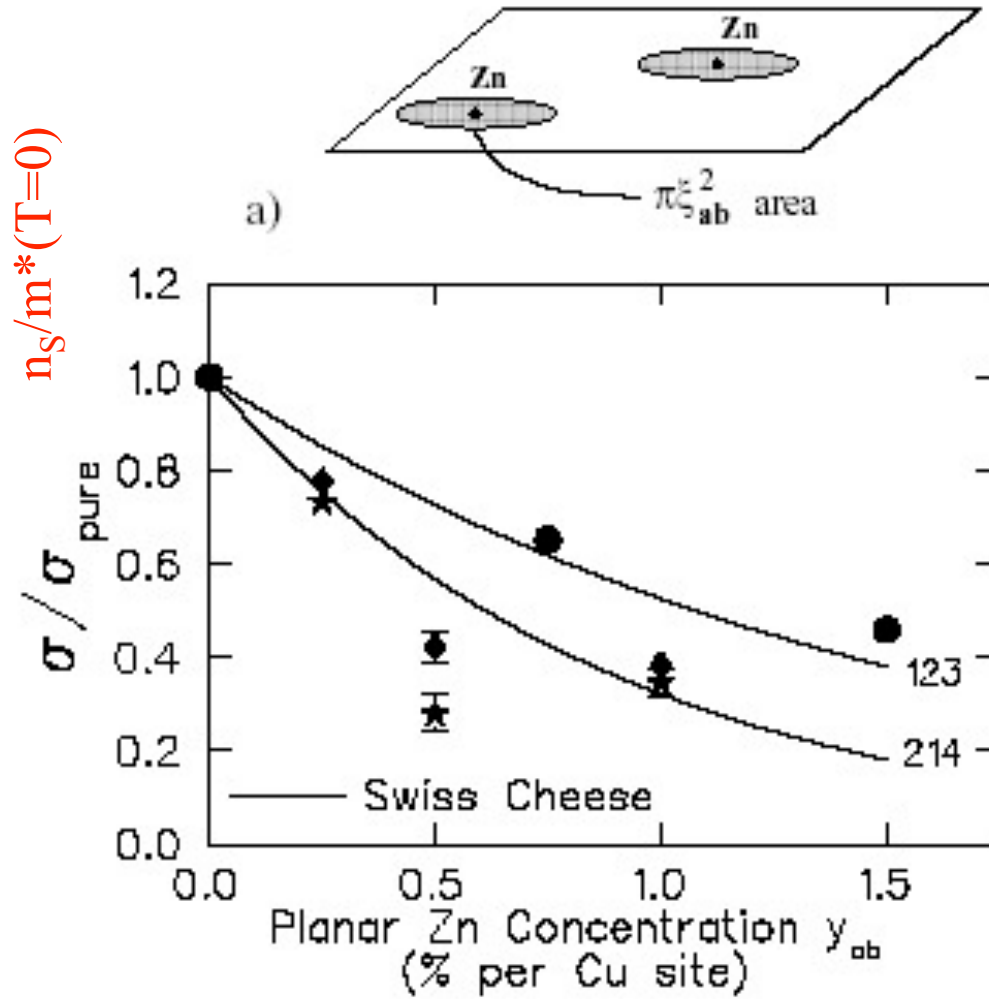


No superfluid on SDW island

with K.M. Kojima, S,Uchida

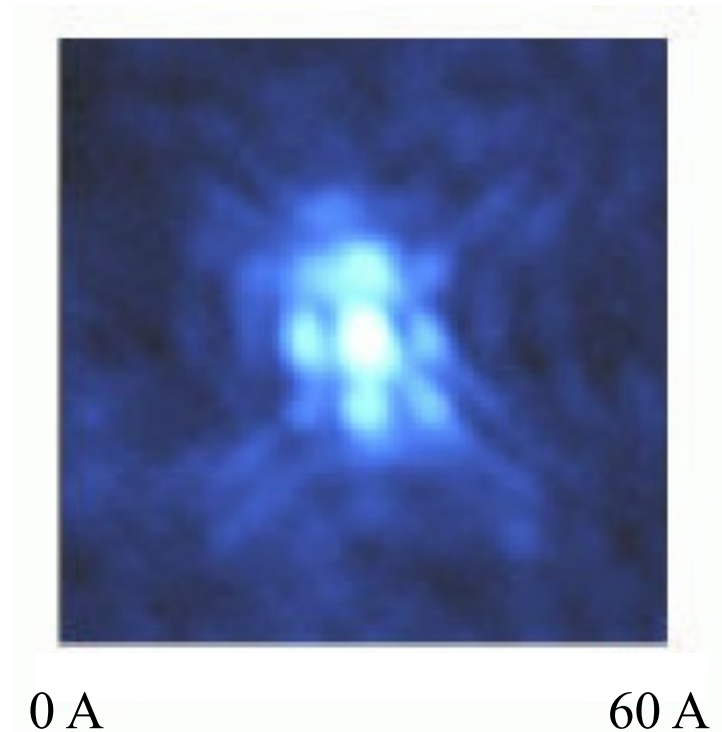
Zn-doped cuprates

TF- μ SR: Superfluid density



PRL 1996

STM (Davis)



Static magnetic order of $\text{Sr}_4\text{A}_2\text{O}_6\text{Fe}_2\text{As}_2$ ($\text{A} = \text{Sc}$ and V) revealed by Mössbauer and muon spin relaxation spectroscopies

J. Munevar,¹ D. R. Sánchez,^{2,1} M. Alzamora,¹ E. Baggio-Saitovitch,¹ J. P. Carlo,³ T. Goko,^{3,4,*} A. A. Aczel,⁵
T. J. Williams,⁵ G. M. Luke,^{5,6} Hai-Hu Wen,⁷ Xiyu Zhu,⁷ Fei Han,⁷ and Y. J. Uemura^{3,†}

¹*Centro Brasileiro de Pesquisas Físicas, Rua Xavier Sigaud 150, Rio de Janeiro, Brazil*

²*Instituto de Física, Universidade Federal Fluminense, 24210-346 Niterói, RJ, Brazil*

³*Department of Physics, Columbia University, New York, New York 10027, USA*

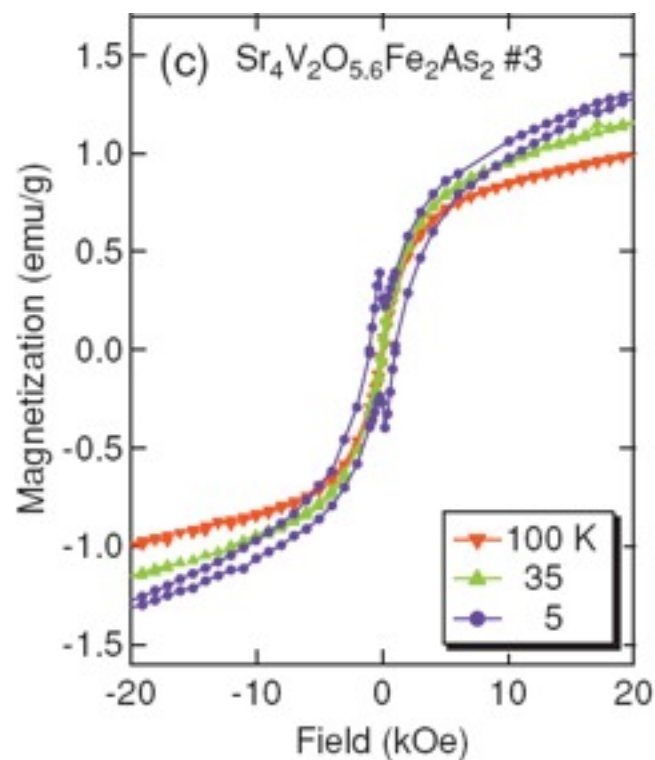
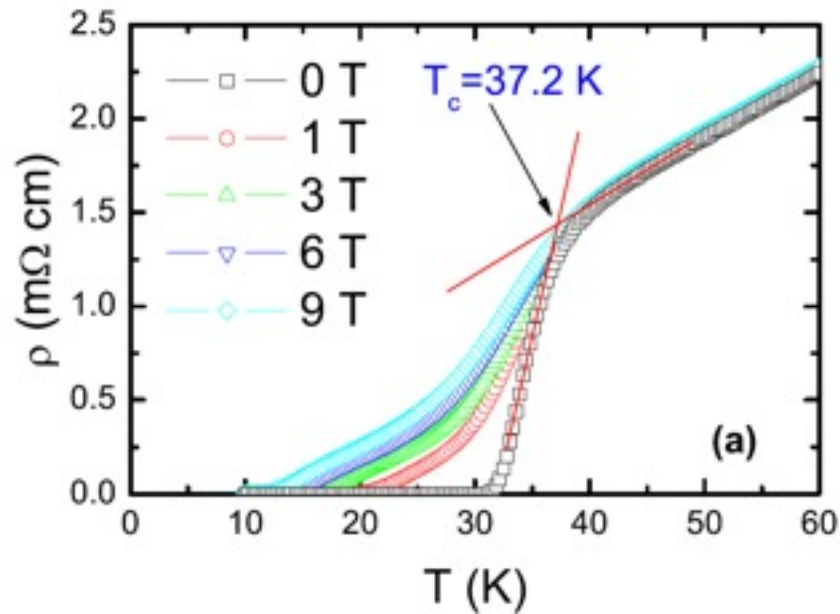
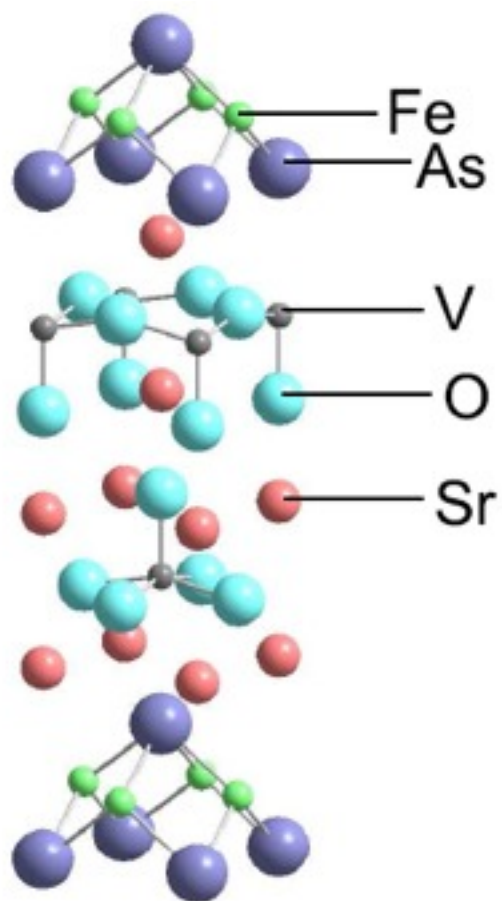
⁴*TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada*

⁵*Department of Physics and Astronomy, McMaster University, Hamilton, Ontario L8S 4M1, Canada*

⁶*Canadian Institute of Advanced Research, Toronto, Ontario M5G 1Z8, Canada*

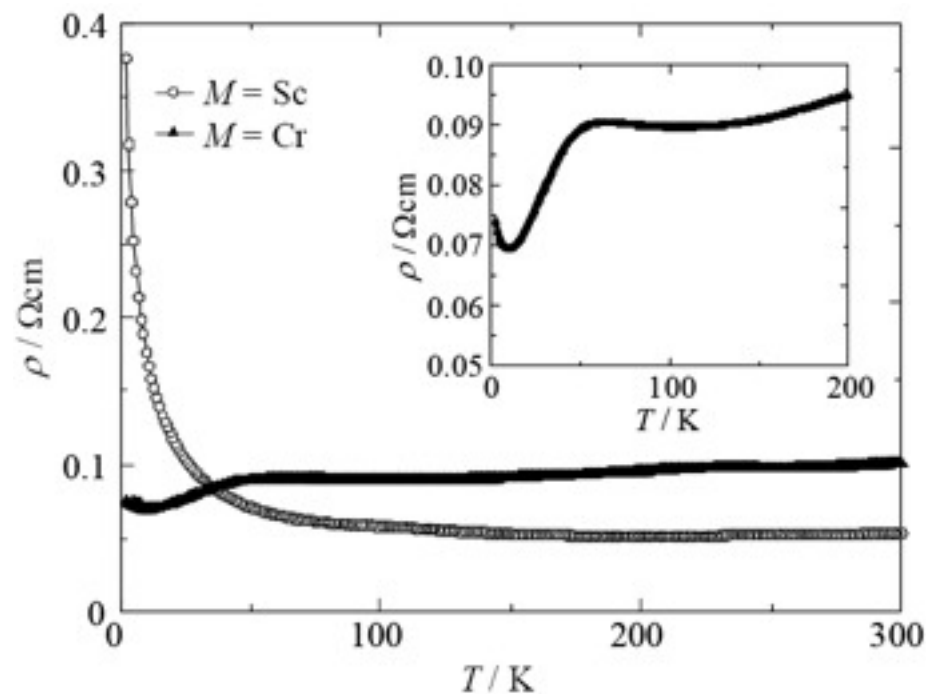
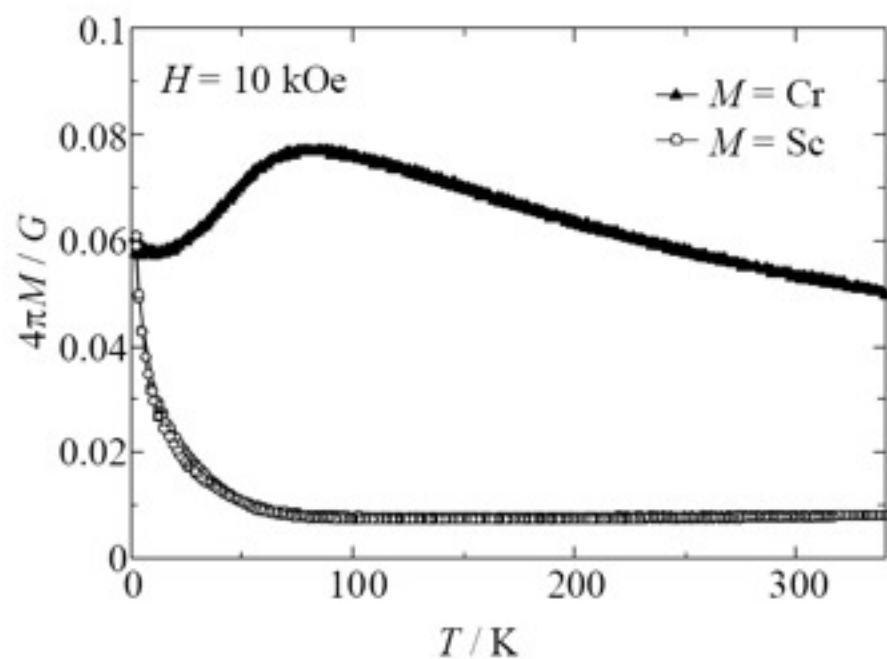
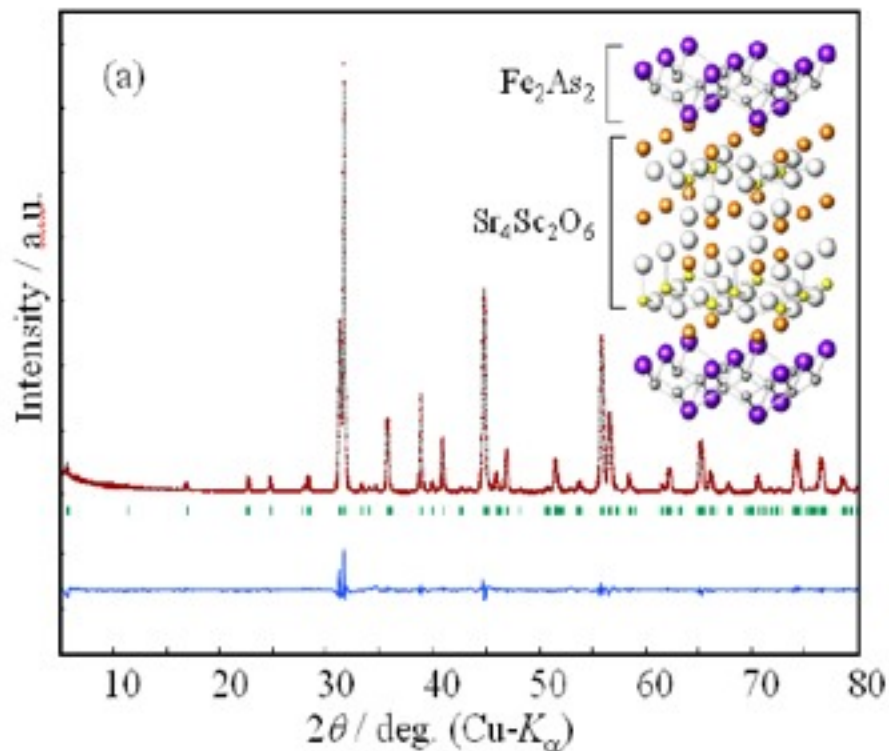
⁷*National Laboratory for Superconductivity, Institute of Physics and Beijing National Laboratory for Condensed Matter Physics,
Chinese Academy of Sciences, P.O. Box 603, Beijing 100190, People's Republic of China*

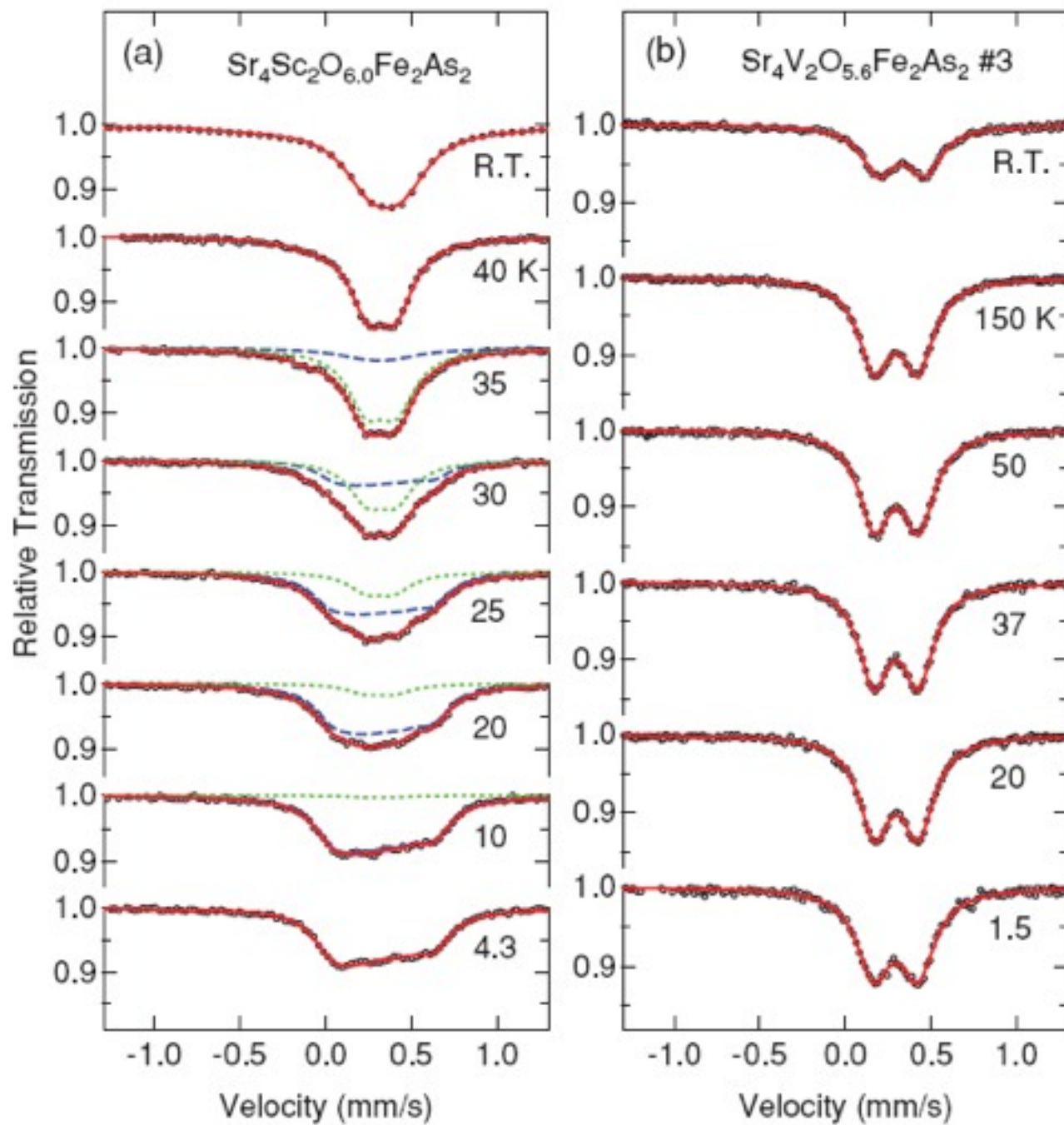
(Received 8 November 2010; revised manuscript received 30 March 2011; published 22 July 2011)

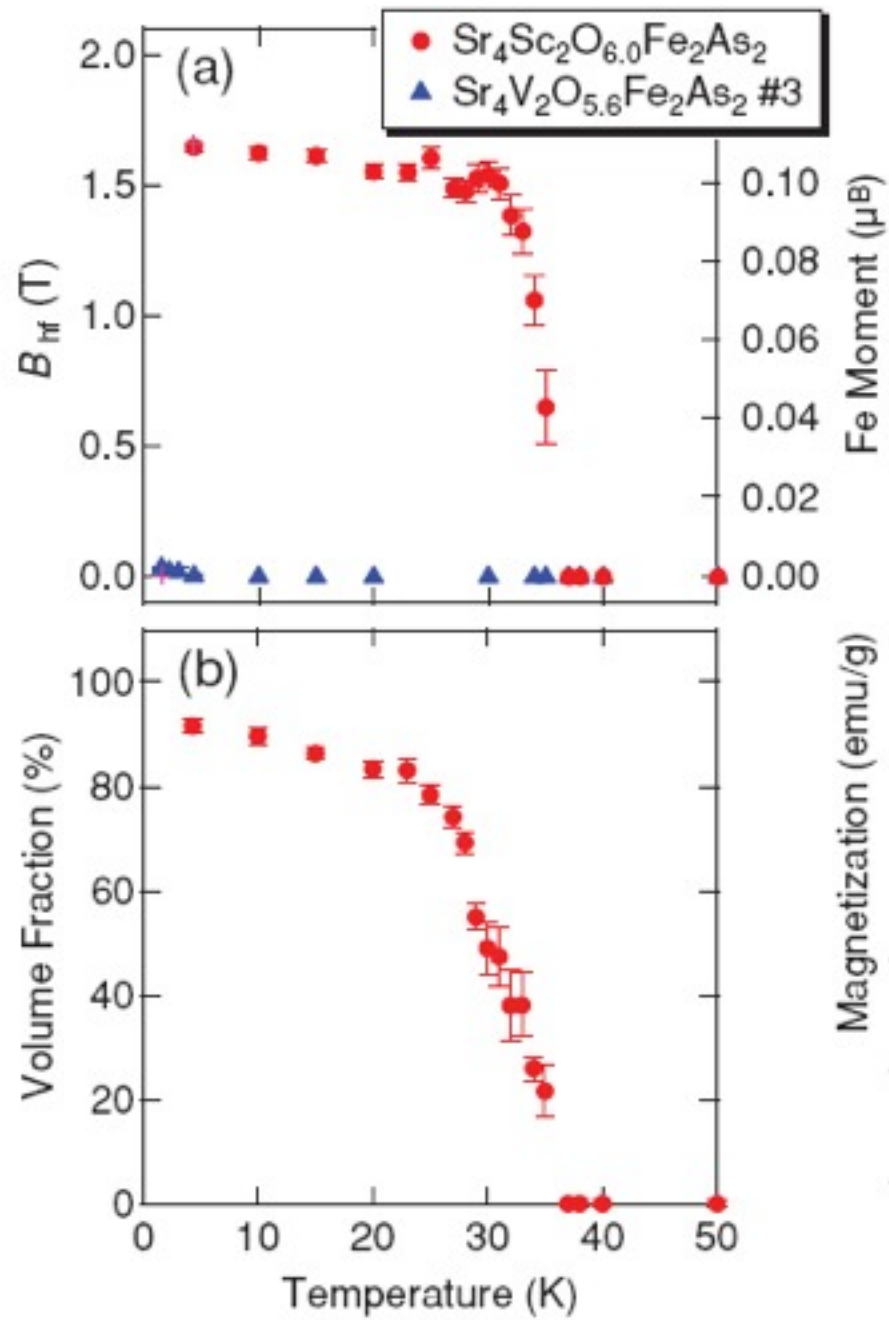


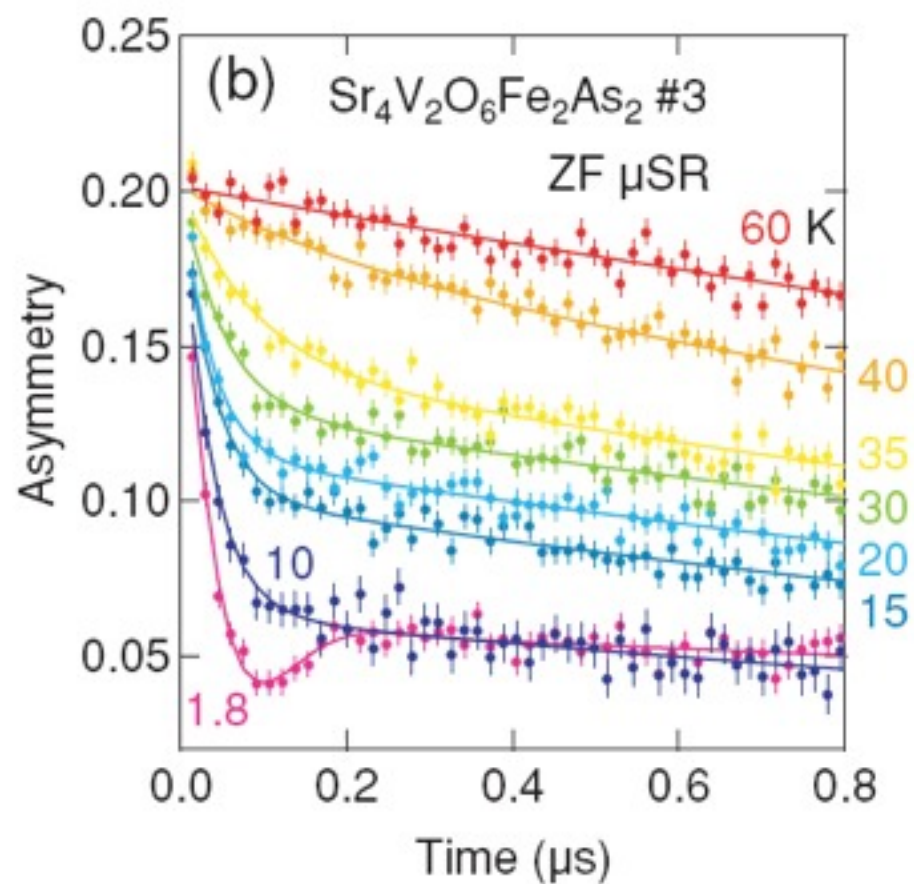
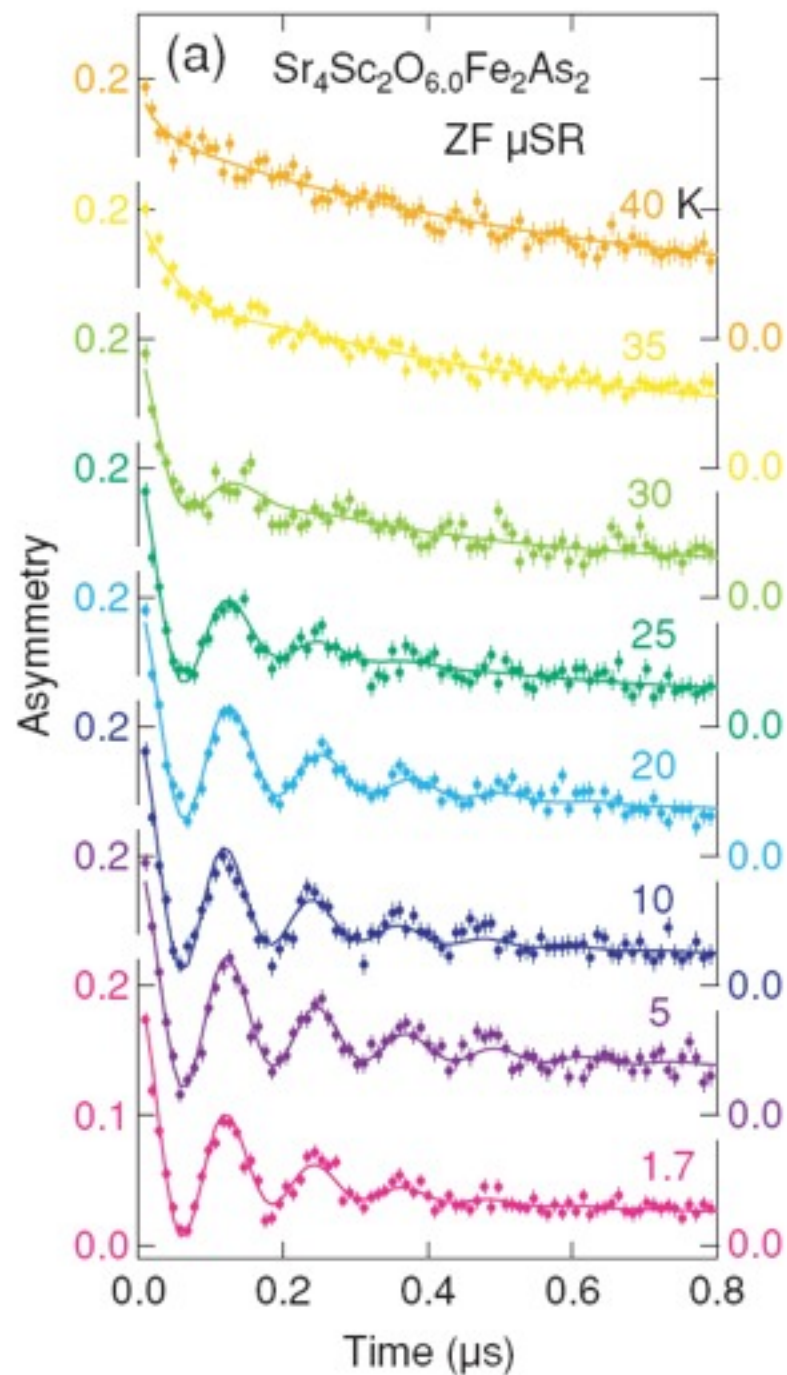


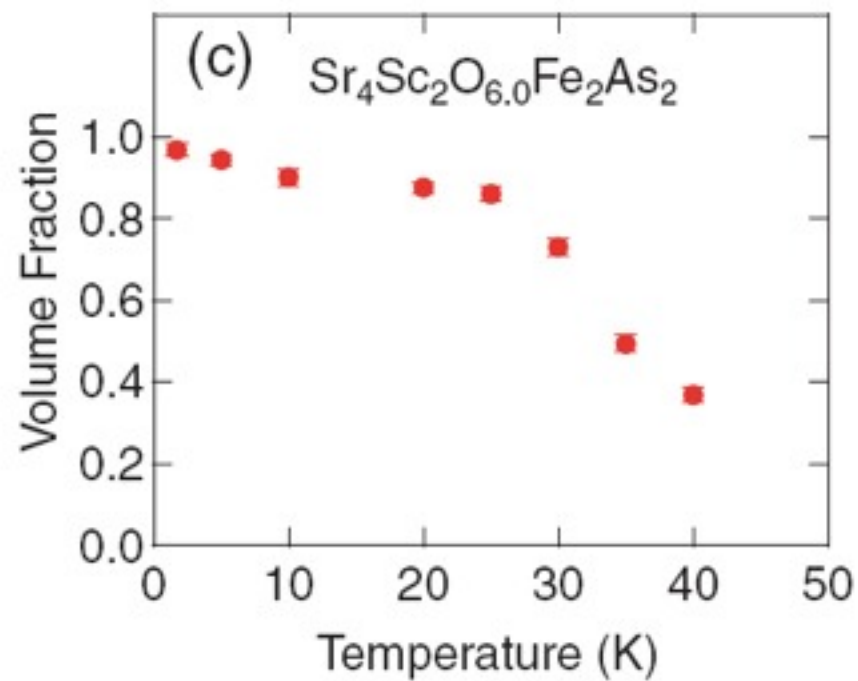
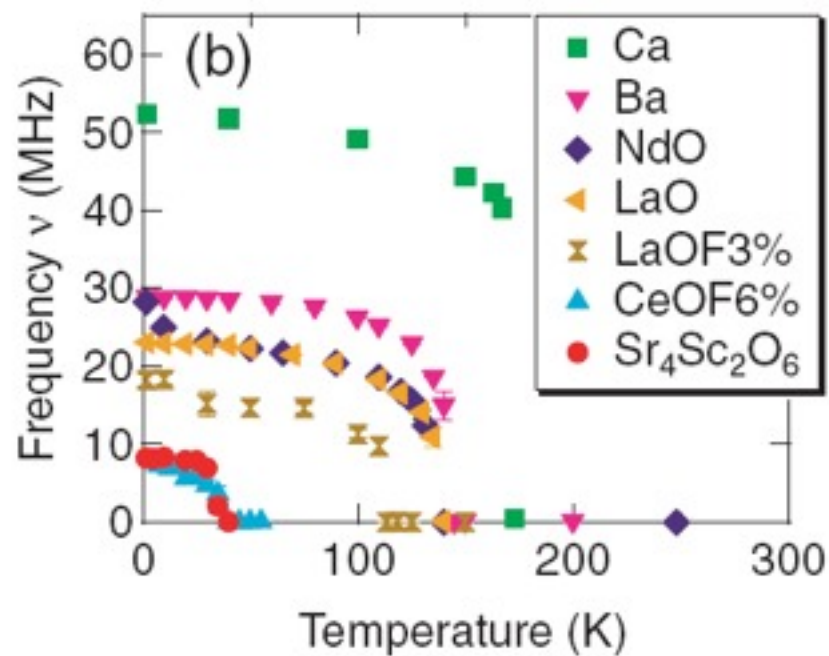
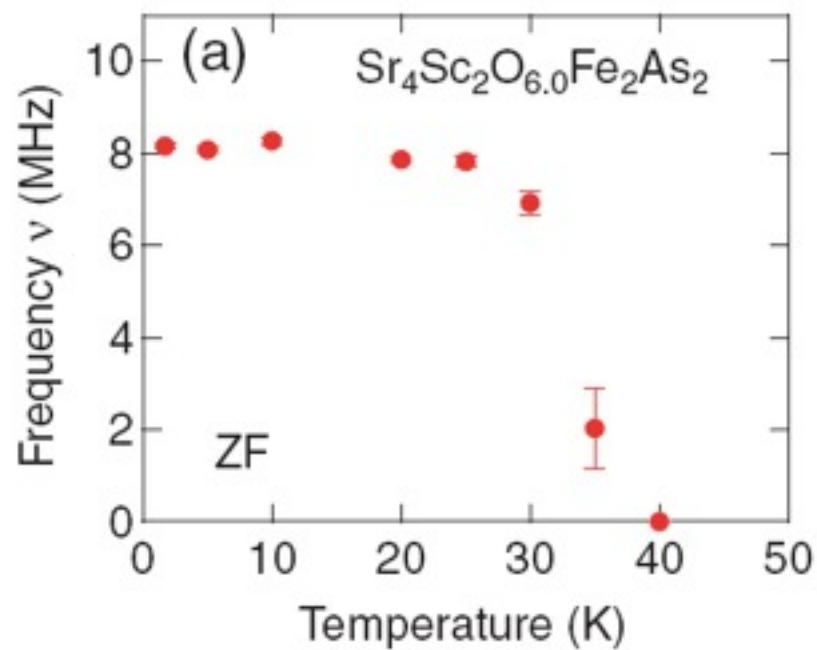
$$M = \text{Sc}$$

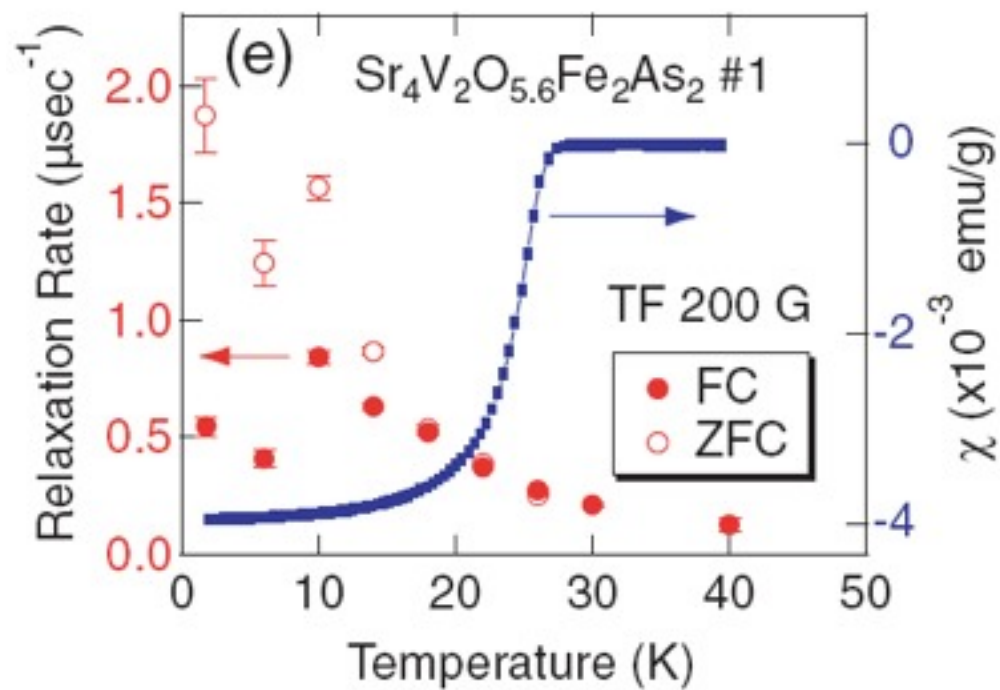
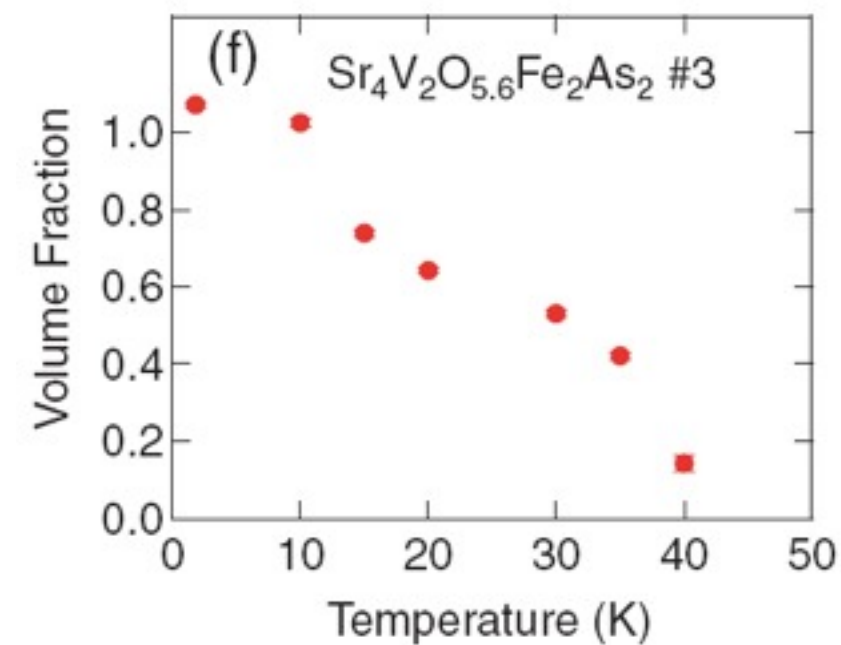
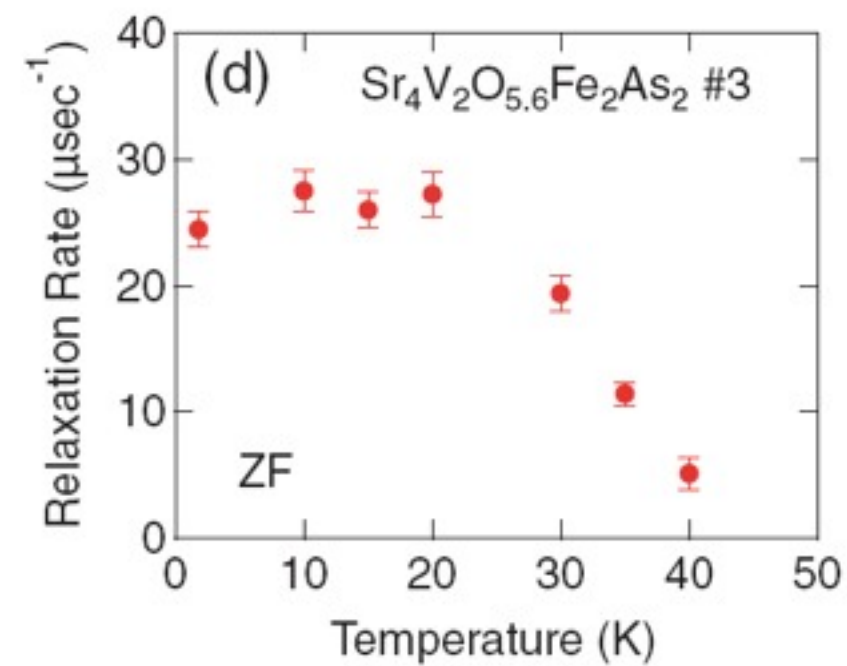












Static magnetic order of quasi-two-dimensional FeAs compounds $\text{Sr}_4\text{A}_2\text{O}_{6-x}\text{Fe}_2\text{As}_2$, with $A = \text{Sc}$ and V , has been detected by ^{57}Fe Mössbauer and muon spin relaxation (μSR) spectroscopies. The nonsuperconducting stoichiometric ($x = 0$) $A = \text{Sc}$ system exhibits a static internal/hyperfine magnetic field both at the ^{57}Fe and μ^+ sites, indicating antiferromagnetic order of Fe moments below $T_N = 35$ K with ~ 0.1 bohr magneton per Fe at $T = 2$ K. The superconducting and oxygen deficient ($x = 0.4$) $A = \text{V}$ system exhibits a static internal field only at the μ^+ site below $T_N \sim 40$ K, indicating static magnetic order of V moments coexisting with superconductivity without freezing of Fe moments. These results suggest that the 42622 FeAs systems belong to the same paradigm with the 1111 and 122 FeAs systems with respect to magnetic behavior of Fe moments.

Phase separation and suppression of critical dynamics at quantum phase transitions of MnSi and $(\text{Sr}_{1-x}\text{Ca}_x)\text{RuO}_3$

Y. J. UEMURA^{1*}, T. GOKO^{1,2}, I. M. GAT-MALUREANU^{1,3}, J. P. CARLO¹, P. L. RUSSO¹, A. T. SAVICI¹, A. ACZEL⁴, G. J. MACDOUGALL⁴, J. A. RODRIGUEZ⁴, G. M. LUKE⁴, S. R. DUNSIGER⁴, A. MCCOLLAM⁵, J. ARAI², CH. PFLEIDERER⁶, P. BÖNI⁶, K. YOSHIMURA⁷, E. BAGGIO-SAITOVITCH⁸, M. B. FONTES⁸, J. LARREA⁸, Y. V. SUSHKO⁹ AND J. SERENI¹⁰

Nature Physics 3 (2007) 29 - 35

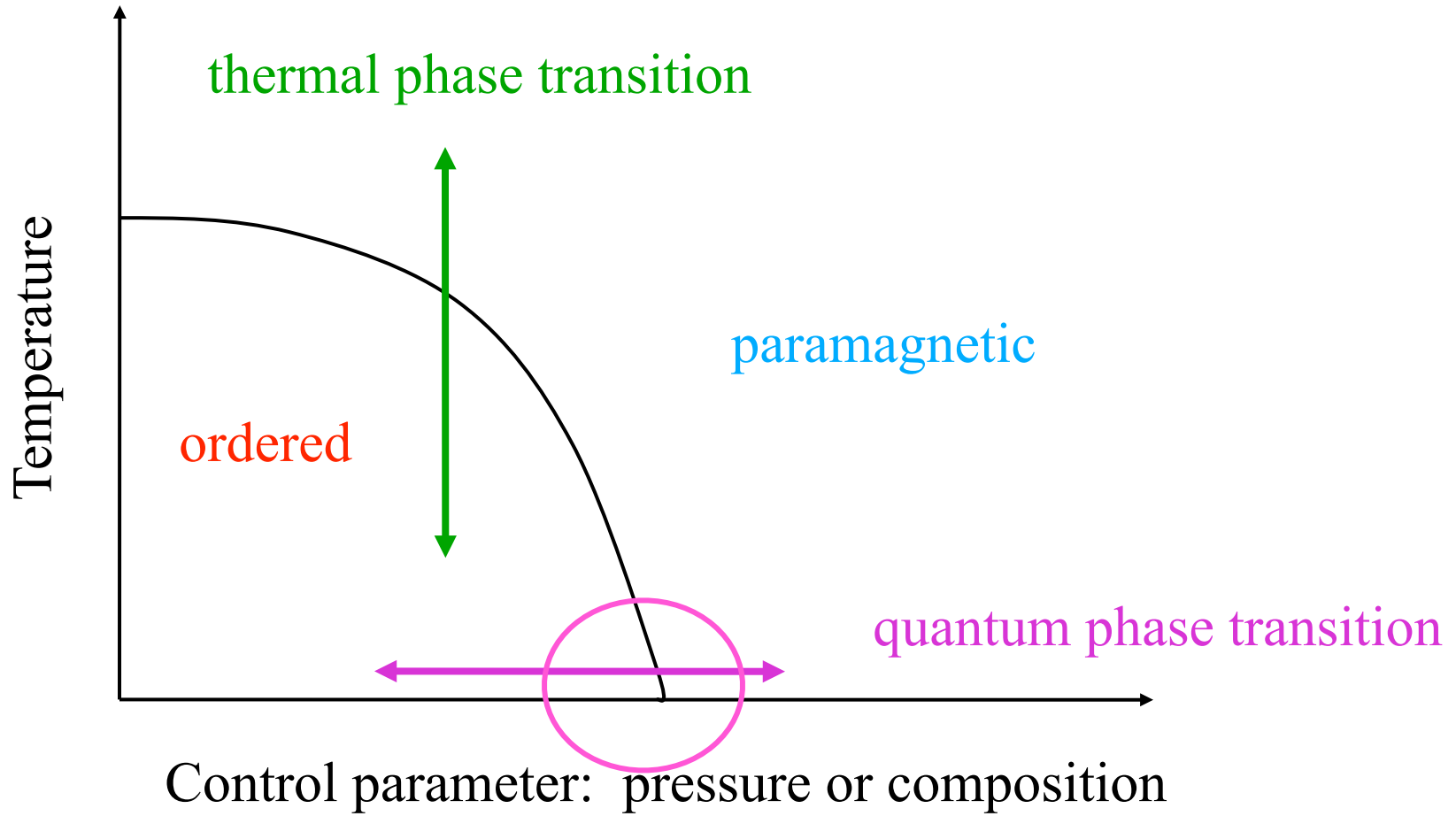


Table 1. T_c versus Spin-wave Stiffness in Ferromagnets

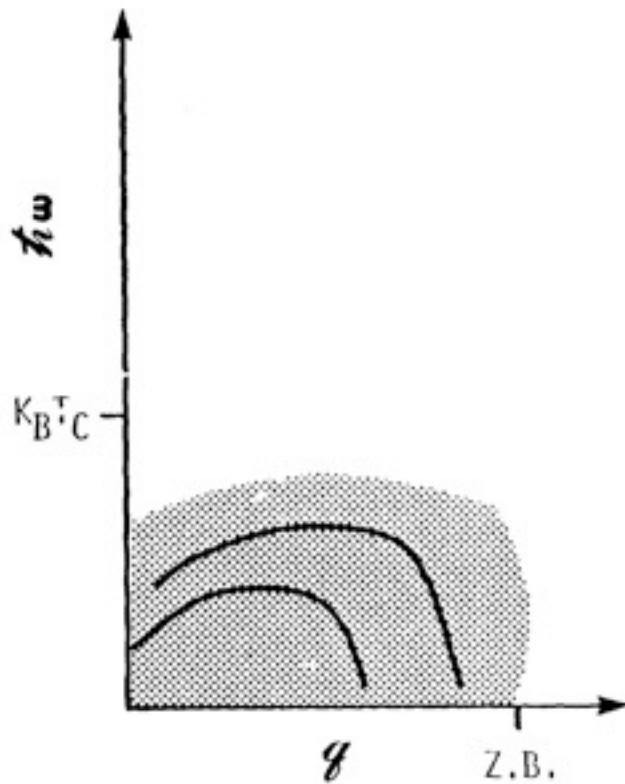
	MnSi	Ni	Fe	Pd ₂ MnSn	EuO
T_c [K]	29	630	1020	193	69
Spin-wave Stiffness D [meV Å ²]	50	400	320	110	13.5
E_{sw}^{zb} at zone boundary [meV]	37	496	373	42	7.9
E_{sw}^{zb}/kT_c (measured)	15	9.1	4.2	2.5	1.3
E_{sw}^{zb}/kT_c (NN Heisenberg)	5	4.6	2.9	2.0	1.3
Ordered Moment $S(T \rightarrow 0)$	0.18	0.3	1.1	2.0	3.5
P_{para}/P_{ord} *	4.1	1.5	1.05	1.0	1.0

* Rhodes-Wohlfarth Ratio

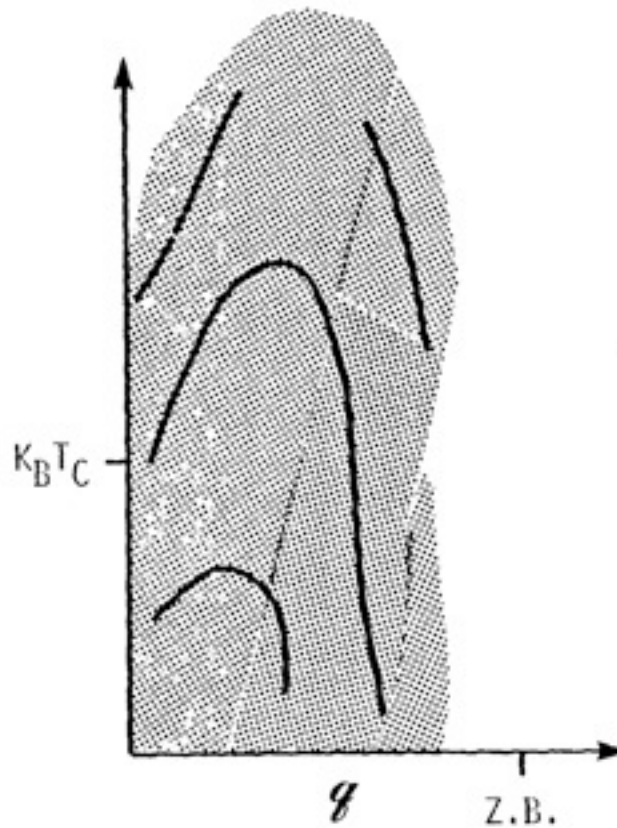
← **itinerant**

localized →

LOCALIZED MOMENT



ITINERANT-ELECTRON



In both cases,

$$\chi \propto \frac{1}{T - T_C}$$

Heisenberg

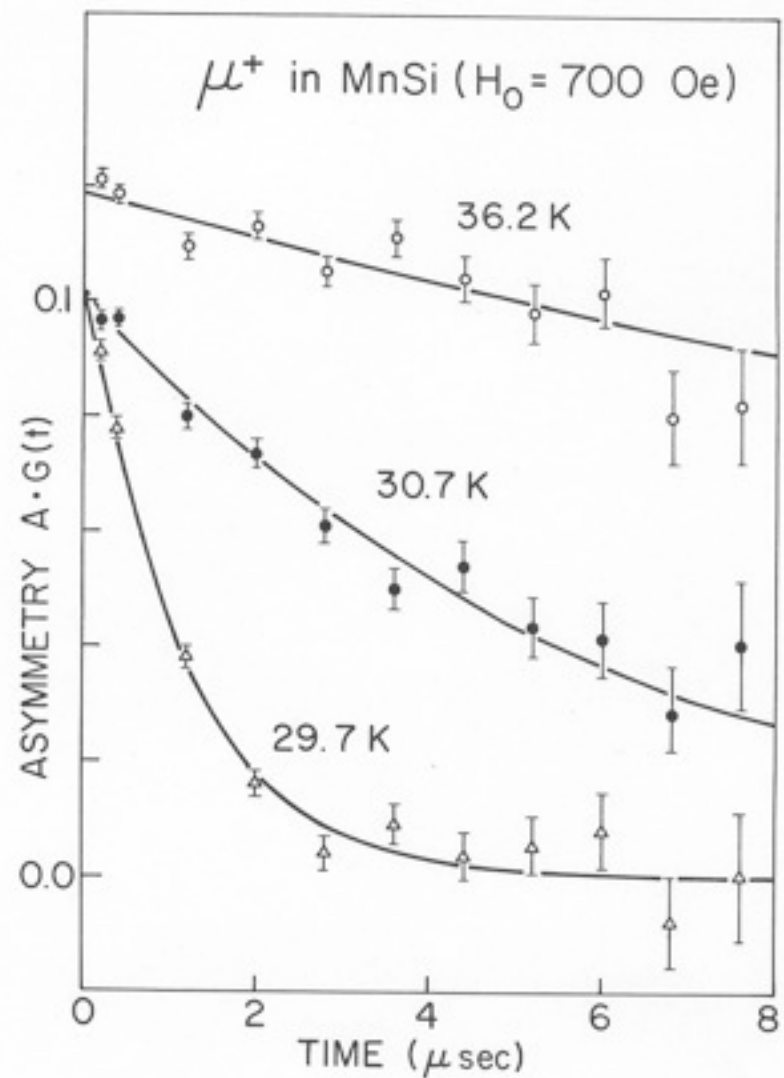
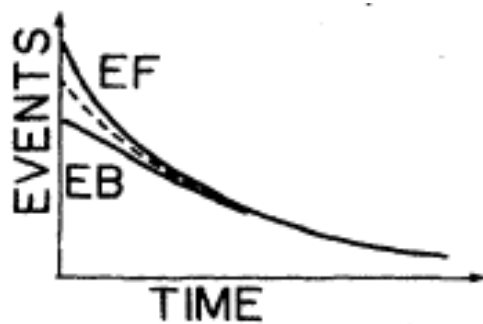
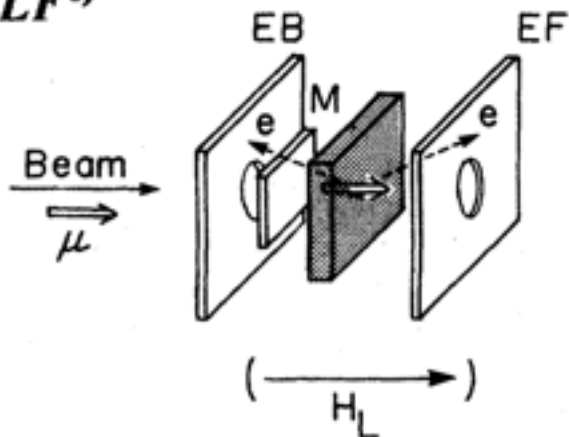
Slater

Stoner

Doniach

Moriya

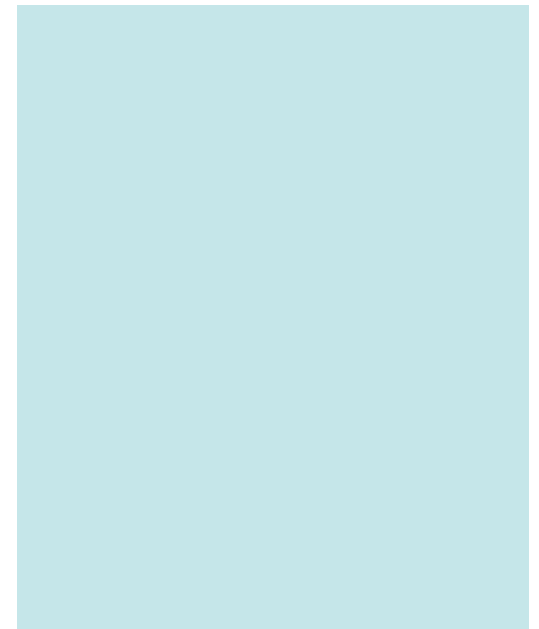
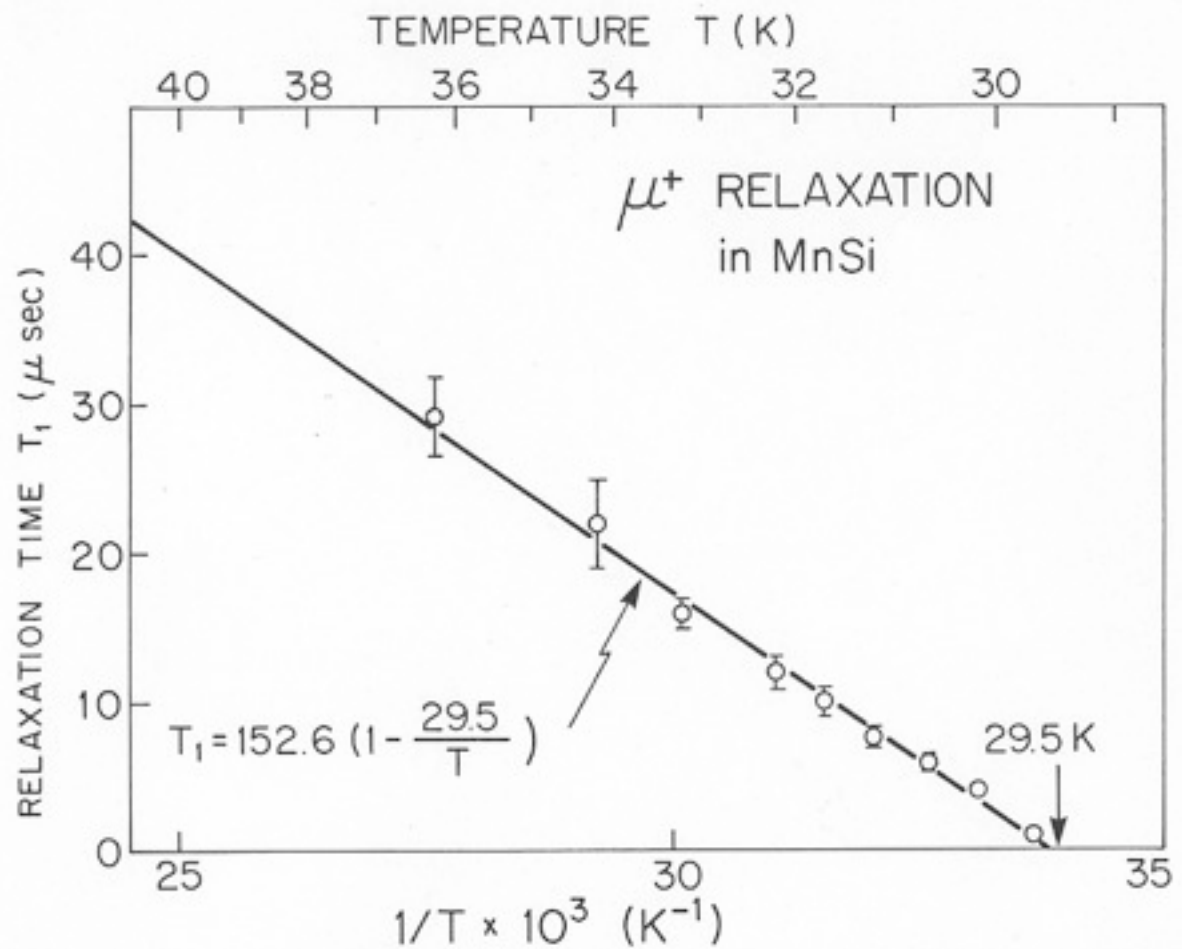
ZF- μ SR
LF- μ SR

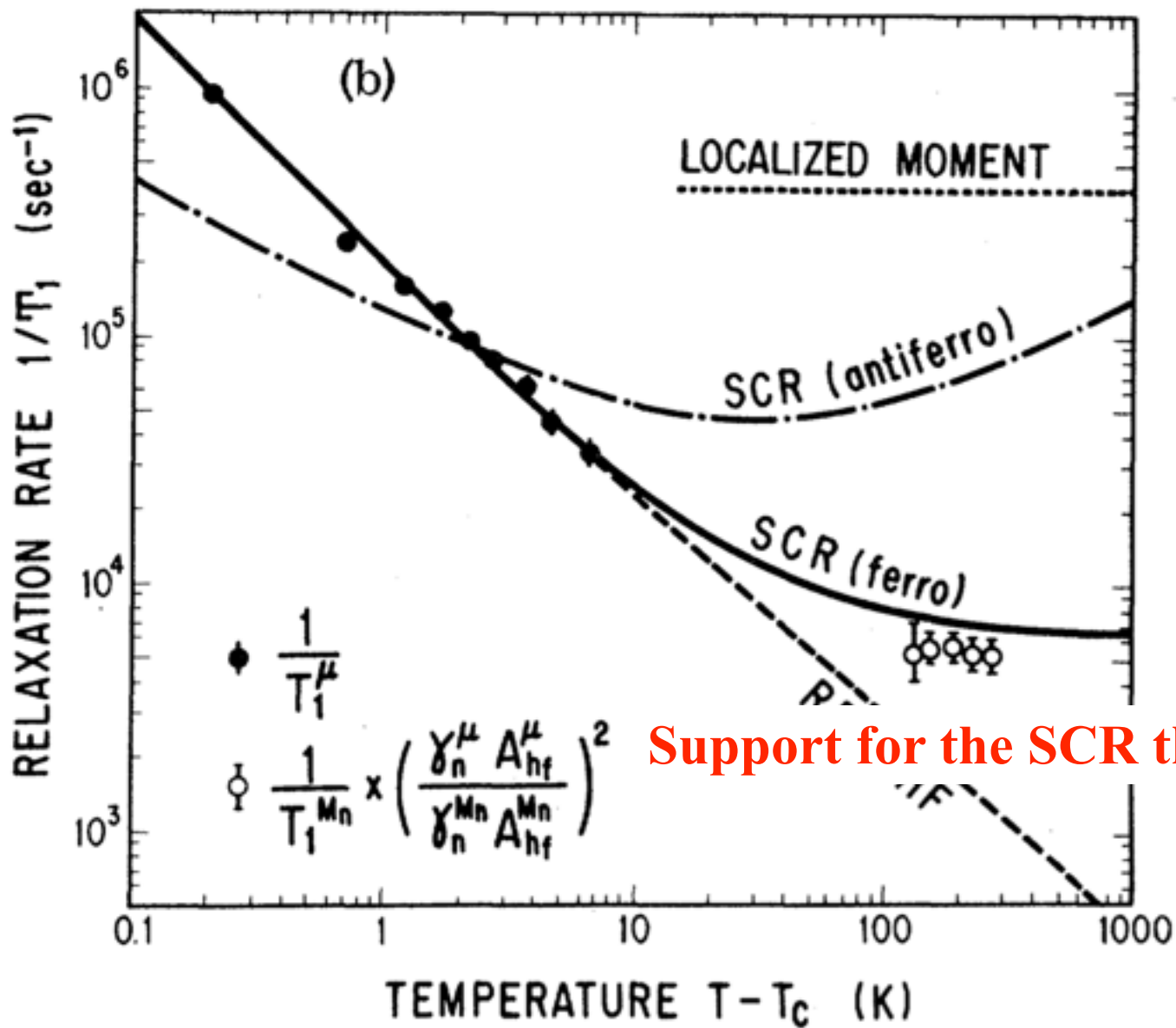


1979 PRL

μ SR in MnSi: PRL 1978

$$H_{LF} = 700 \text{ G}$$

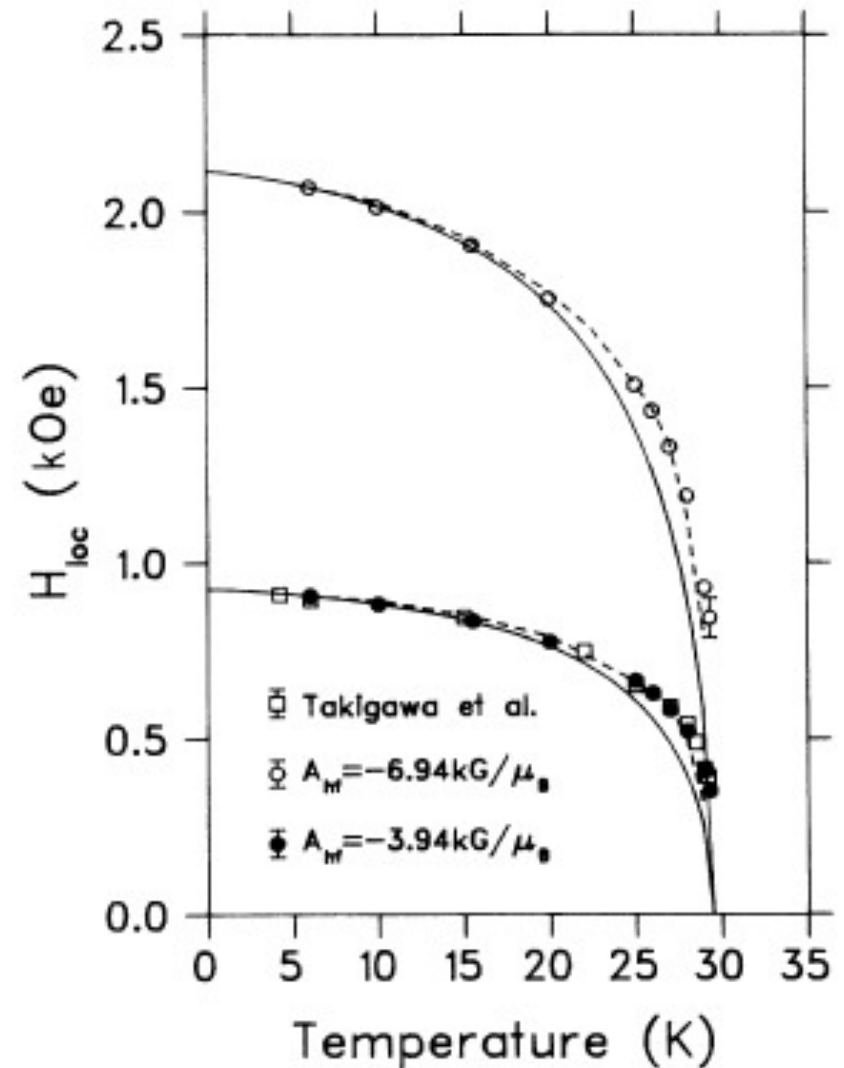
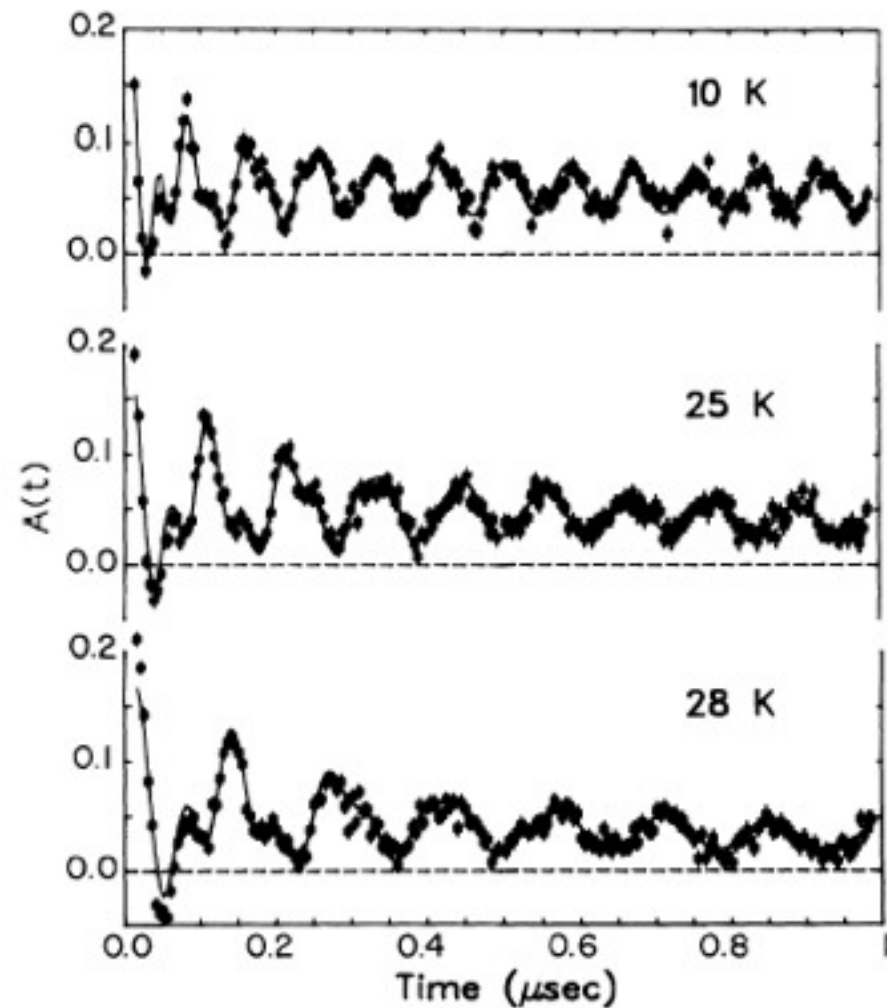


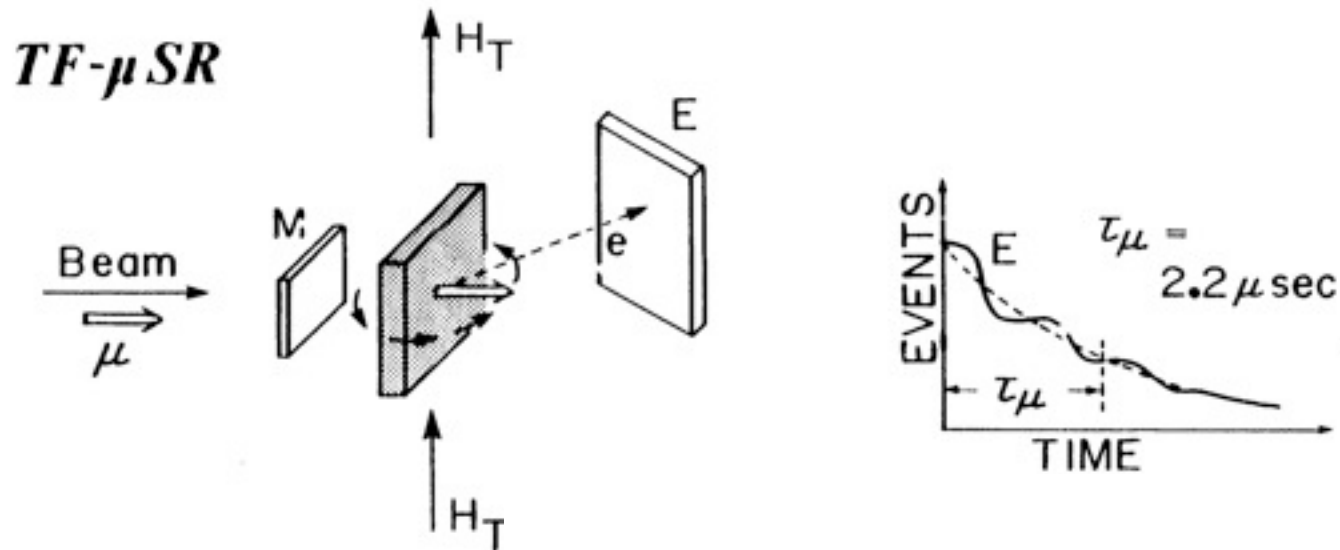


Support for the SCR theory of Moriya

μ SR covers wide temperature region, complementary to NMR

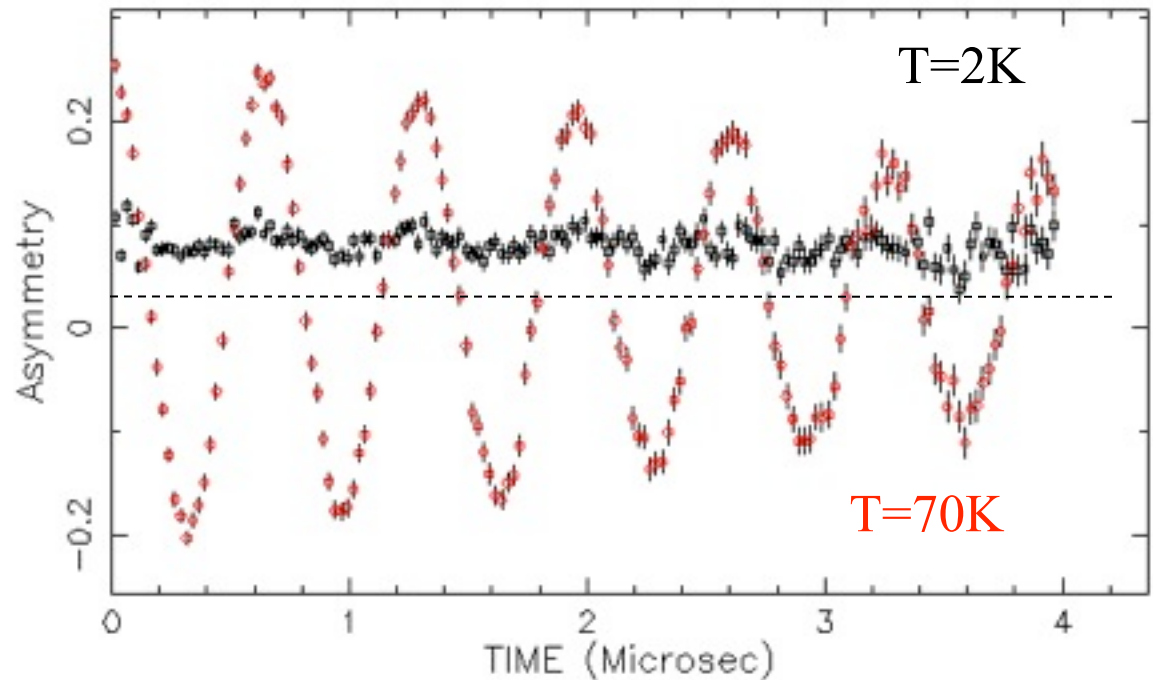
ZF precession in ordered state:
frequency scales with ordered moment



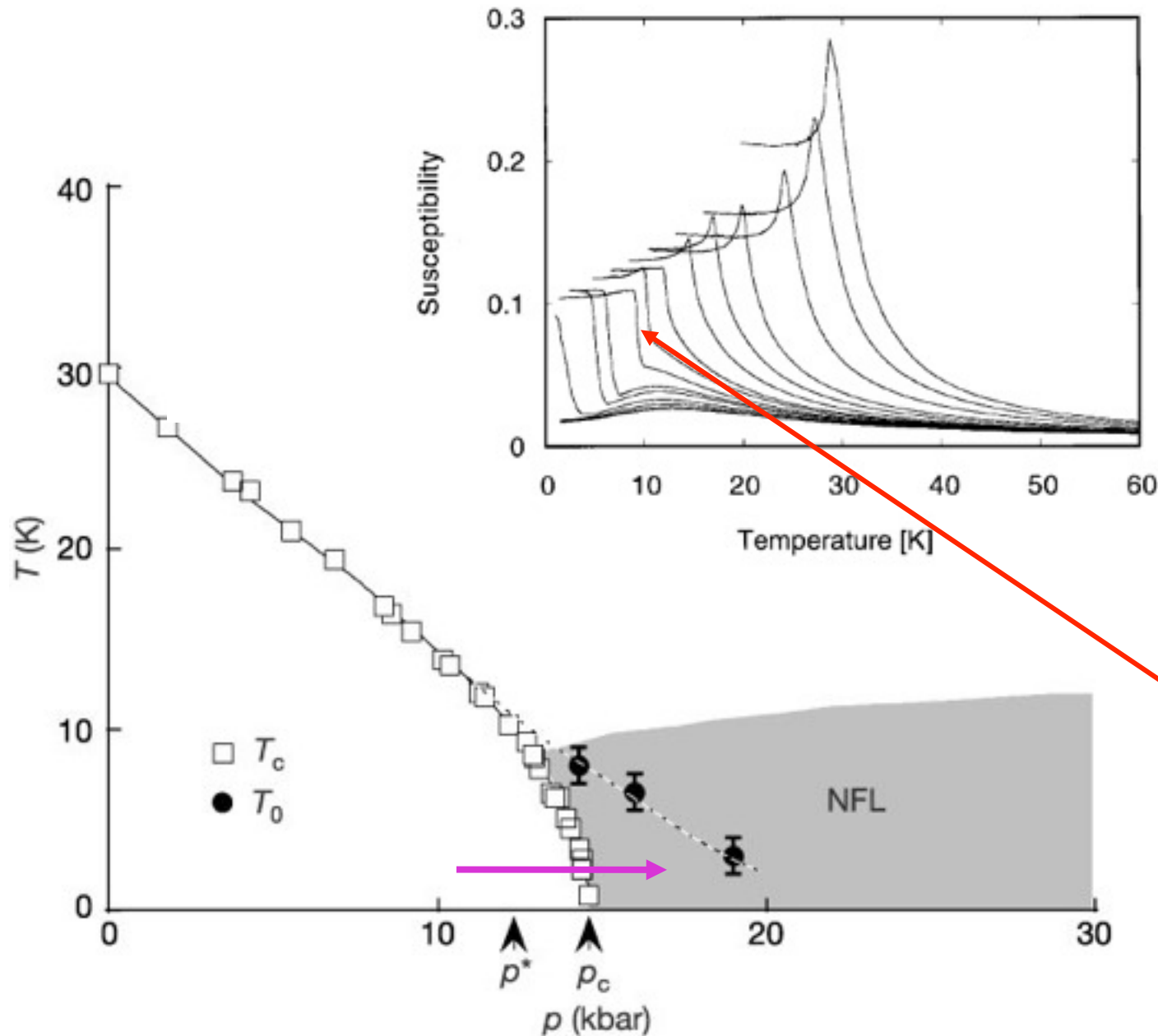


Weak TF 100 G

**Precession amplitude
represents para- /
non-magnetic volume**



Pfleiderer et al., PRB1997; Nature2004



on scatt.

anomalous short-range correlations
 $p^* > p$

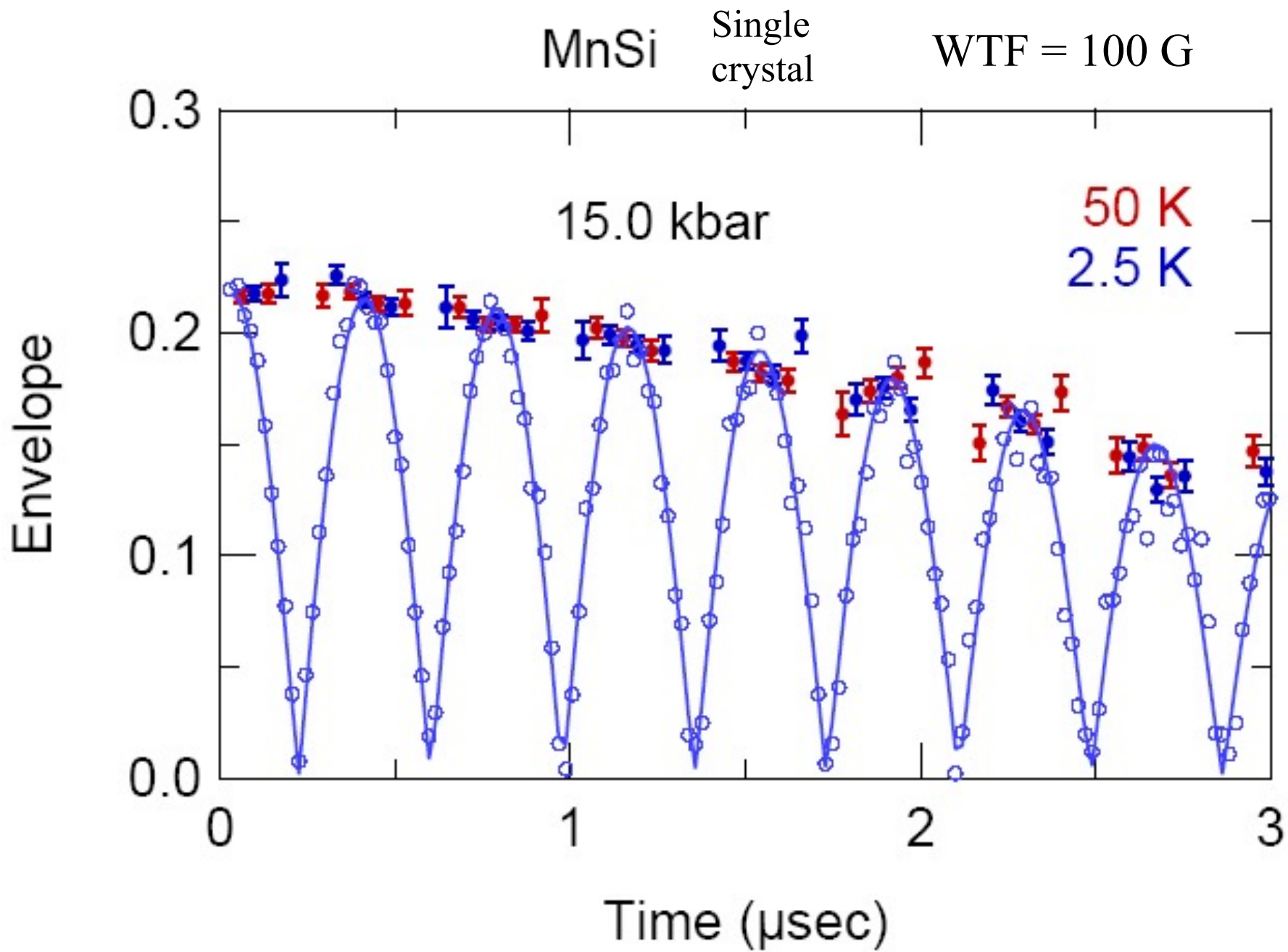
Transport /
 suscepti.
 weakly
 first order
 transition
 above
 $p^* \sim 12$ kbar

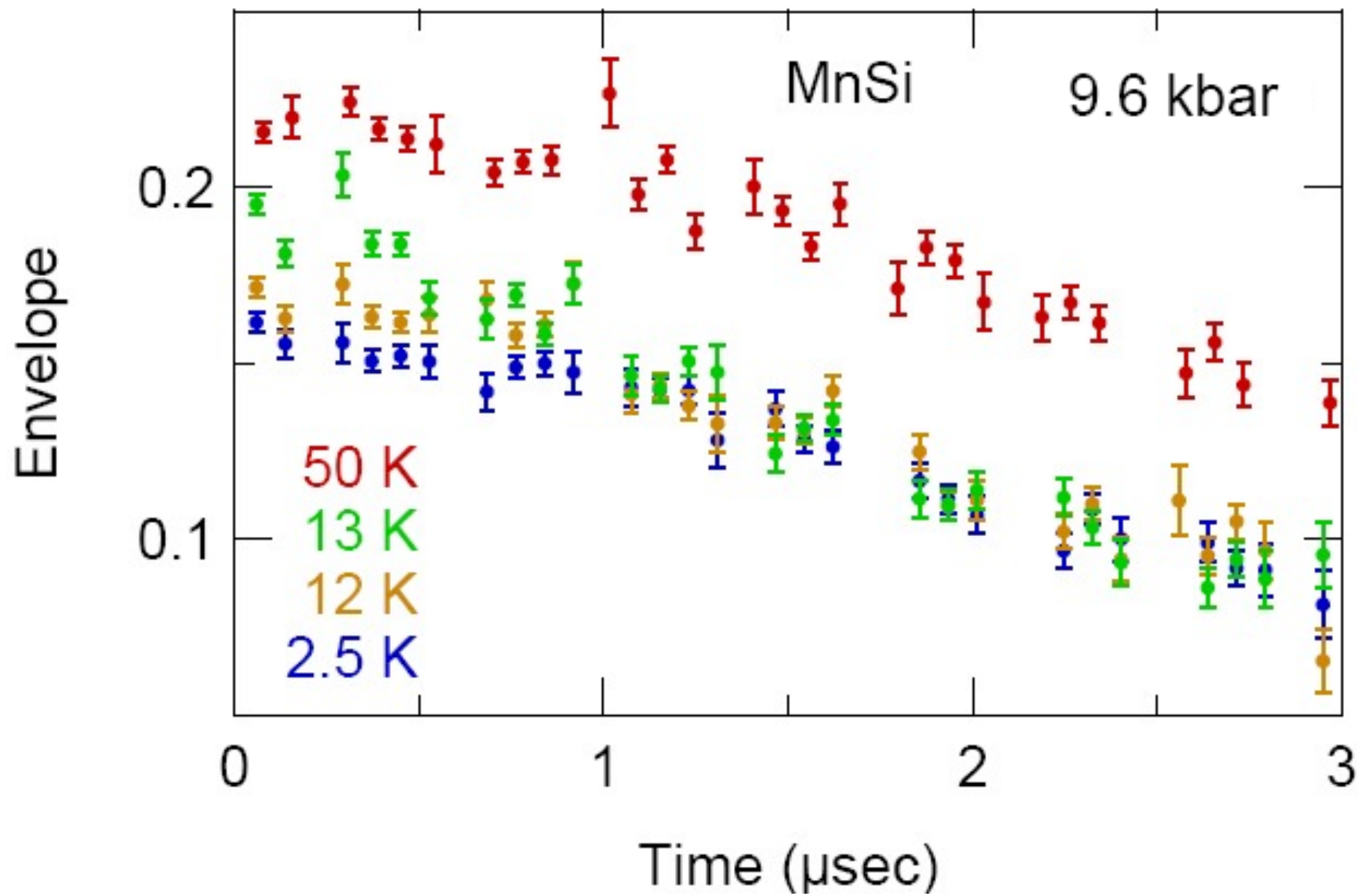
1998 - MuSR in MnSi under applied pressure

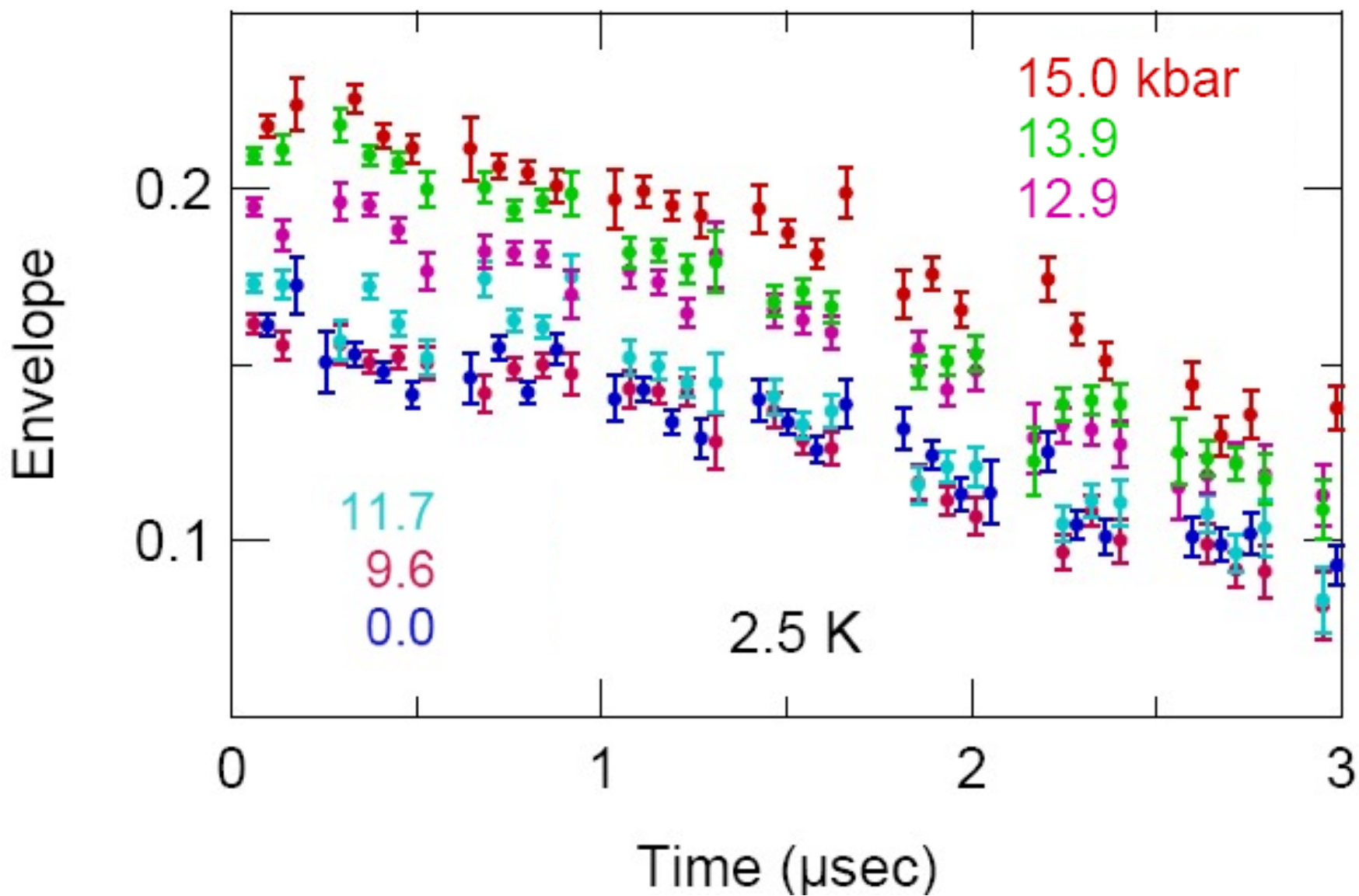
---- difficulty in large background from cell
and limited accessible pressure

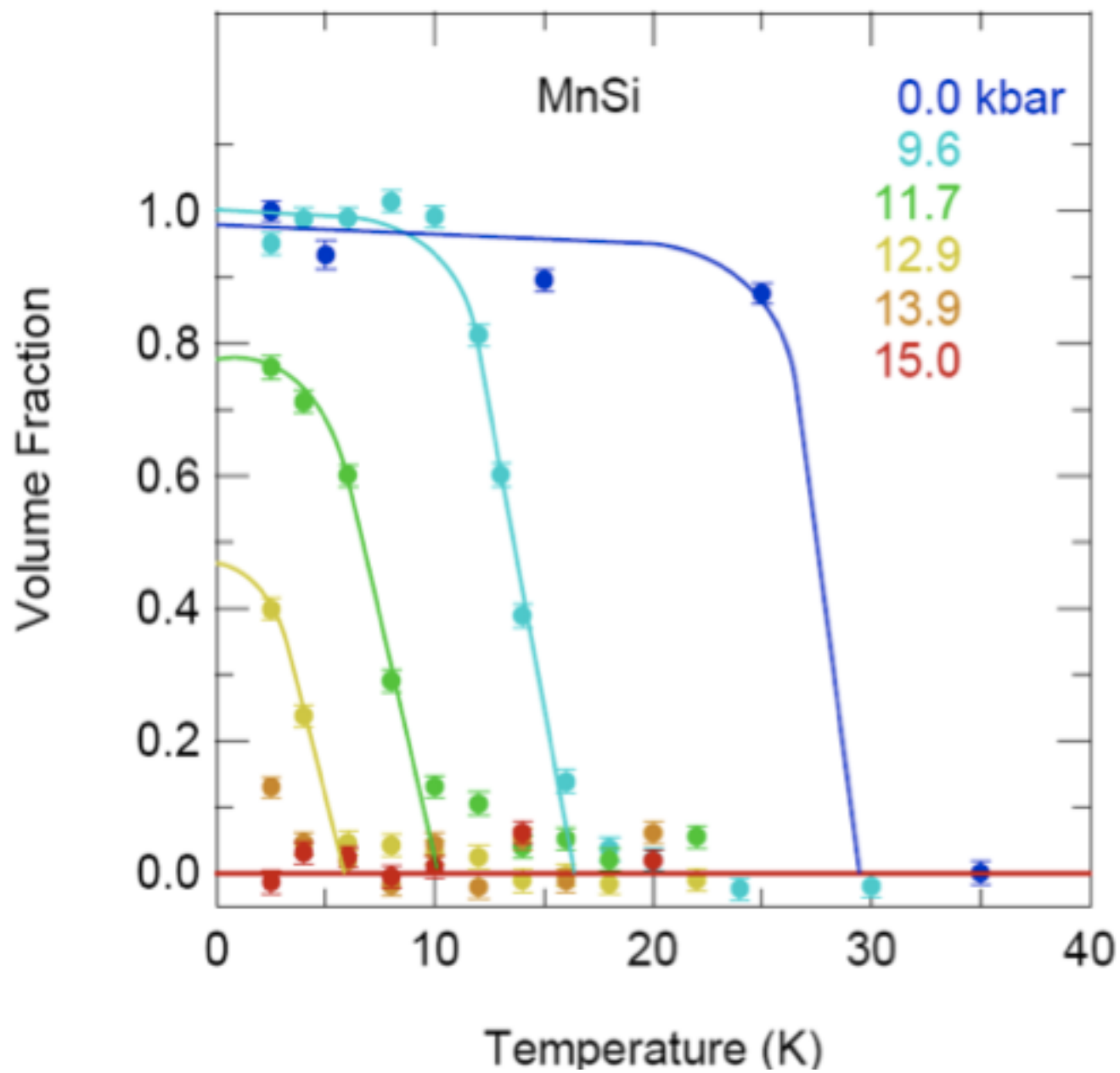
2004 Summer and November: major progress with T. Goko
MuSR in Transeverse Field of 100 G.

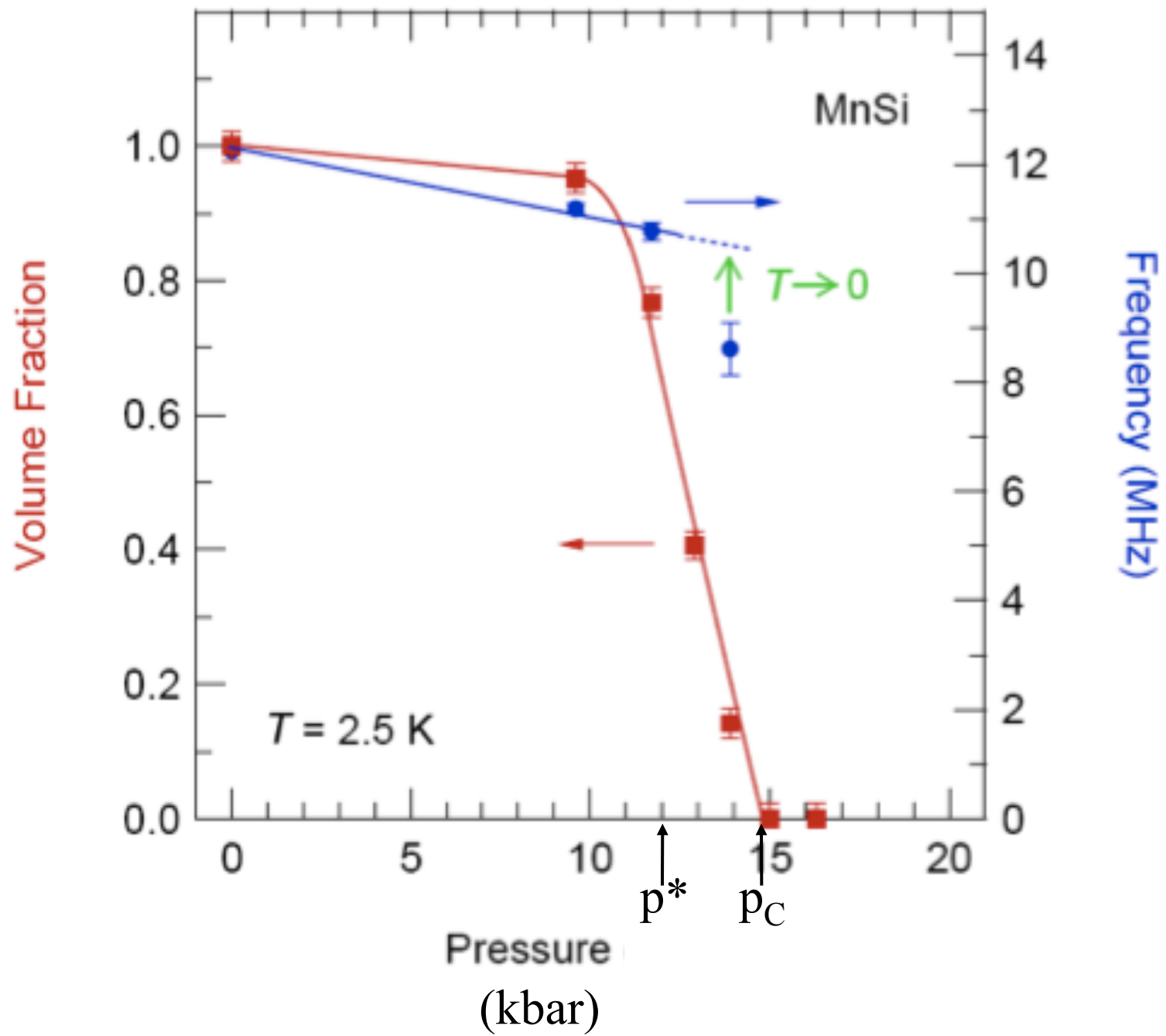
Single crystal specimen from Pfleiderer (TU Munich)

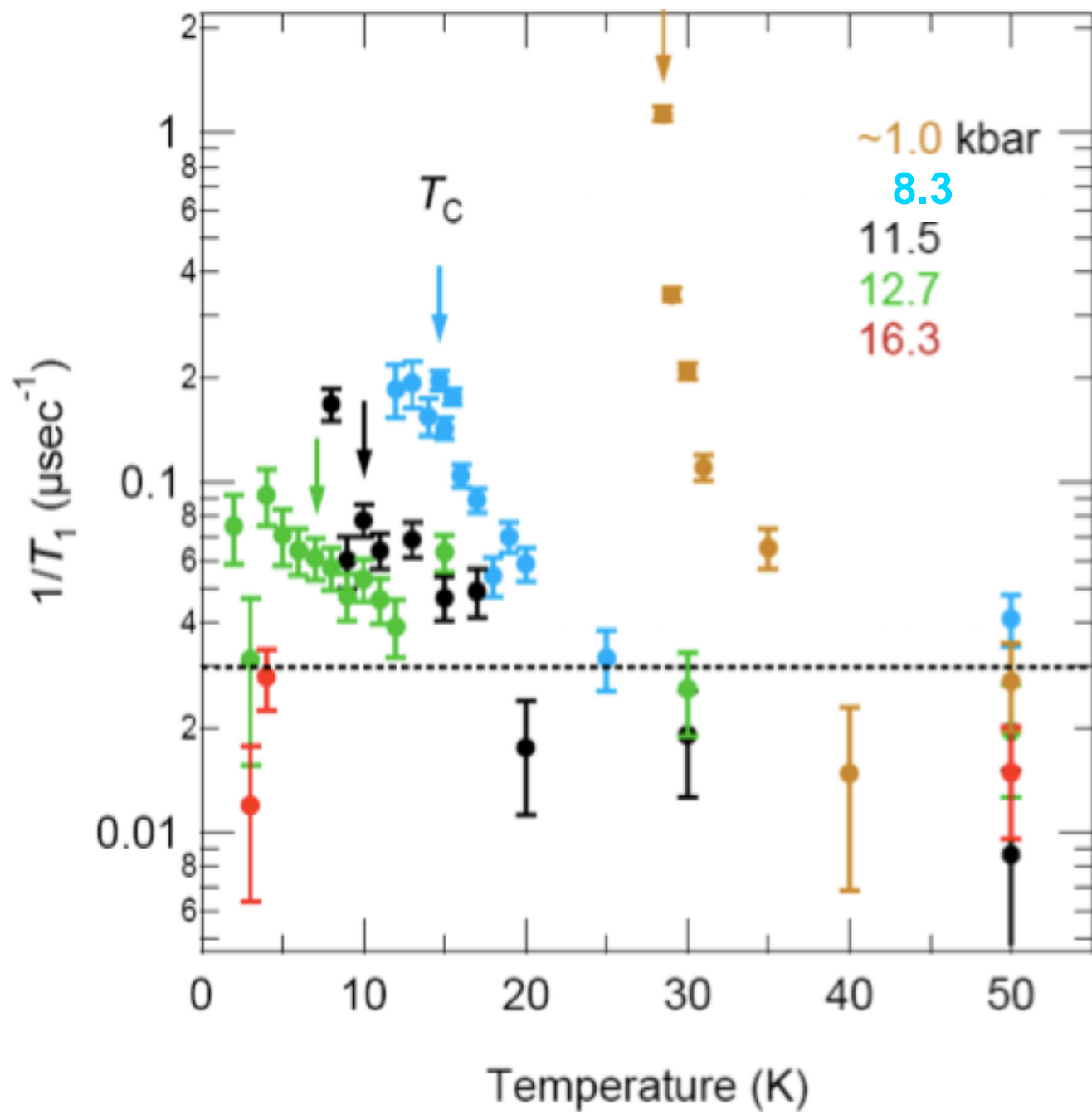












New Information from MuSR

p^* p_c



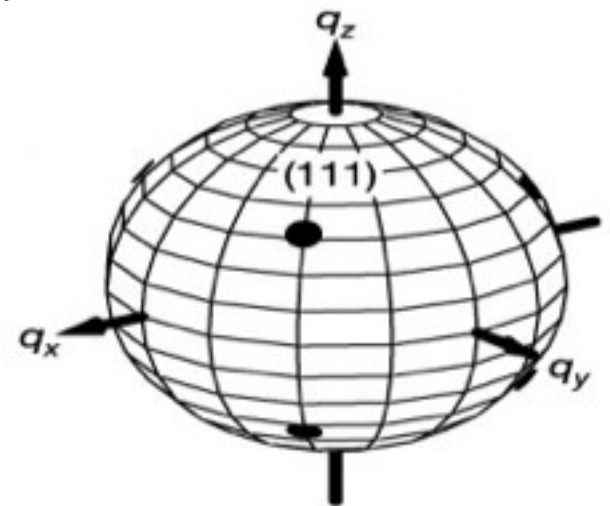
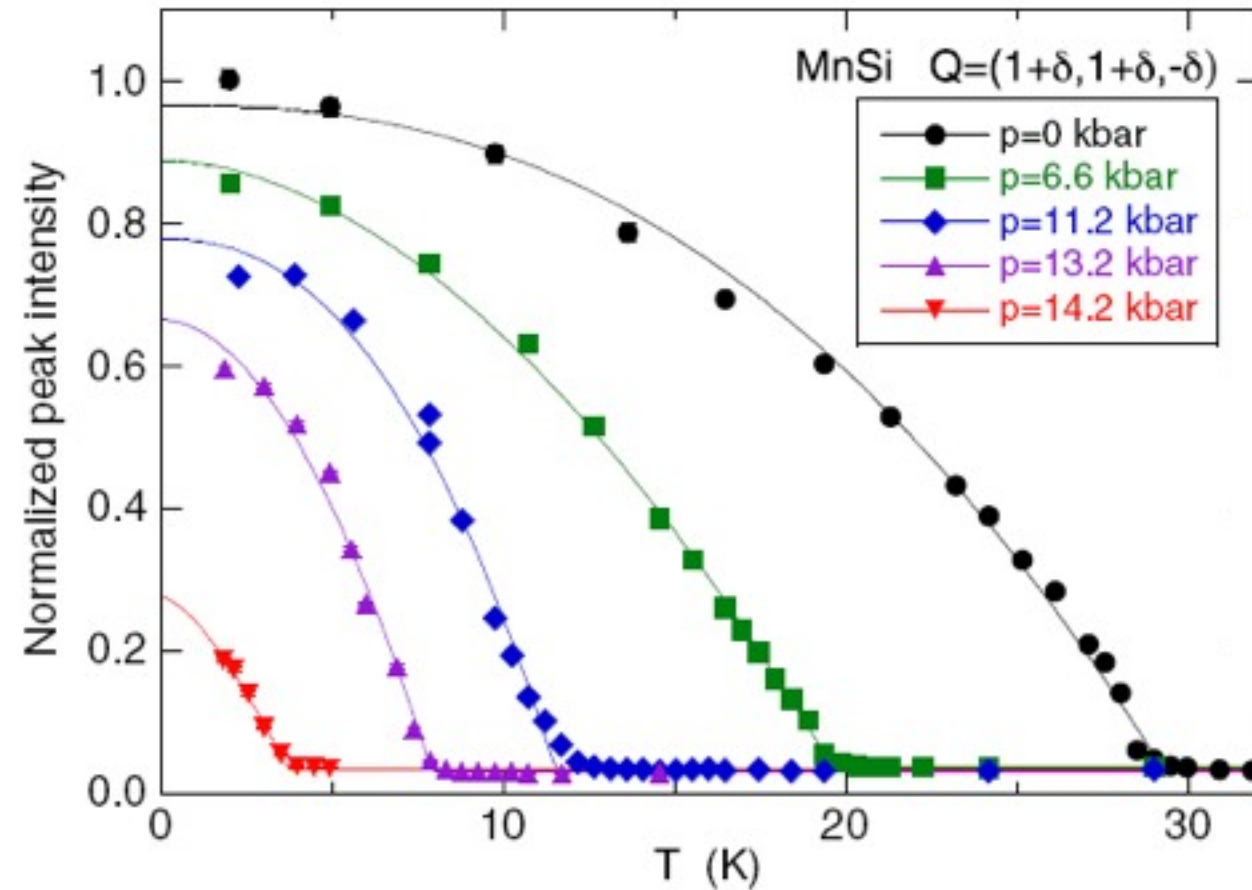
1. Finite Static Volume Fraction between 12– 15 kbar
----- **Spontaneous Phase Separation**
2. No static component above 15 kbar
3. No dynamic critical behavior above p^*

Also: Little temperature dependence of ordered moment size
(ZF- μ SR frequency) --- confirming NMR ---

➔ **First-order QPT**

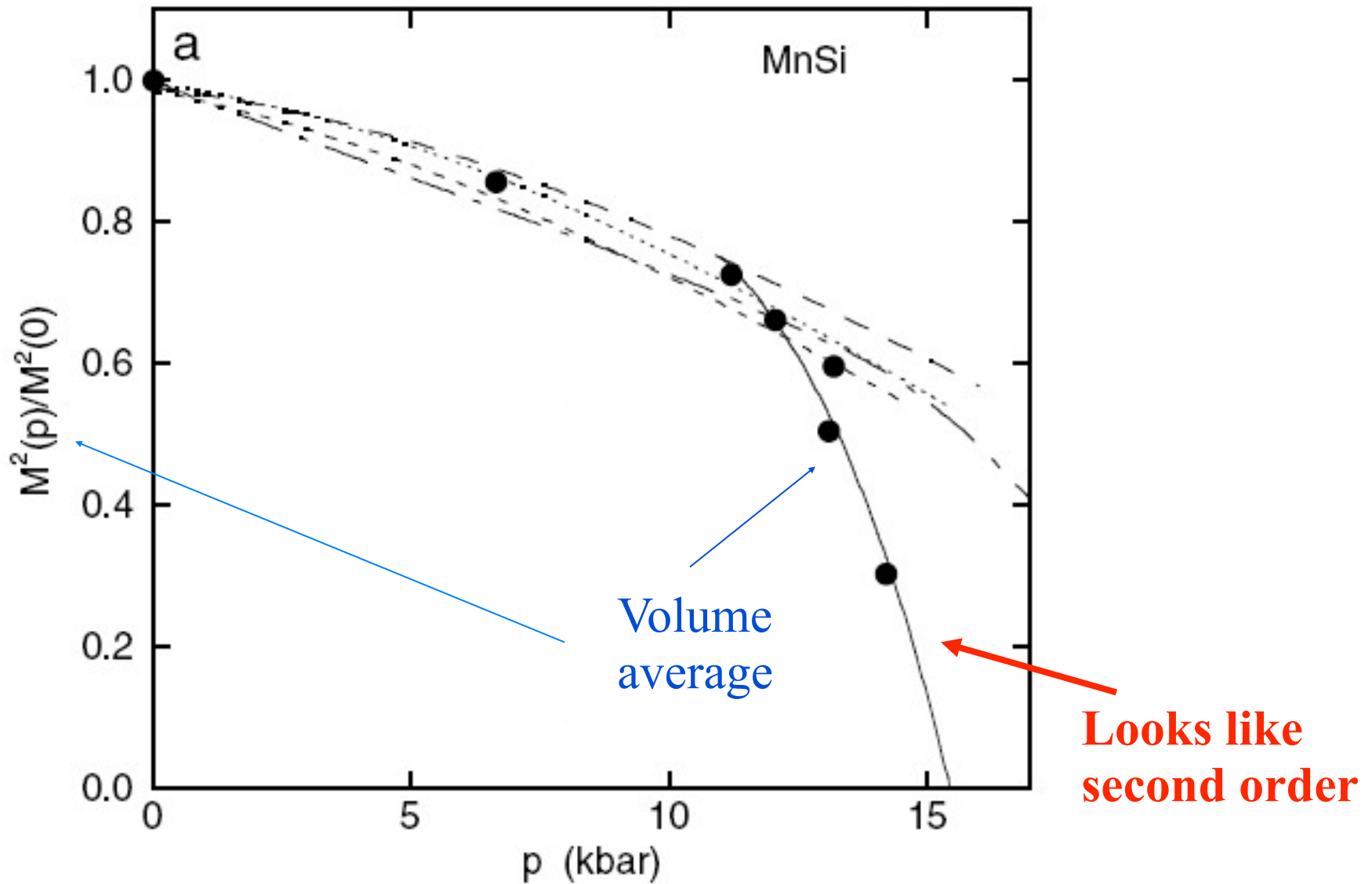
Pressure dependence of the magnetic structure of the itinerant electron magnet MnSi

B Fåk¹, R A Sadykov², J Flouquet¹ and G Lapertot¹

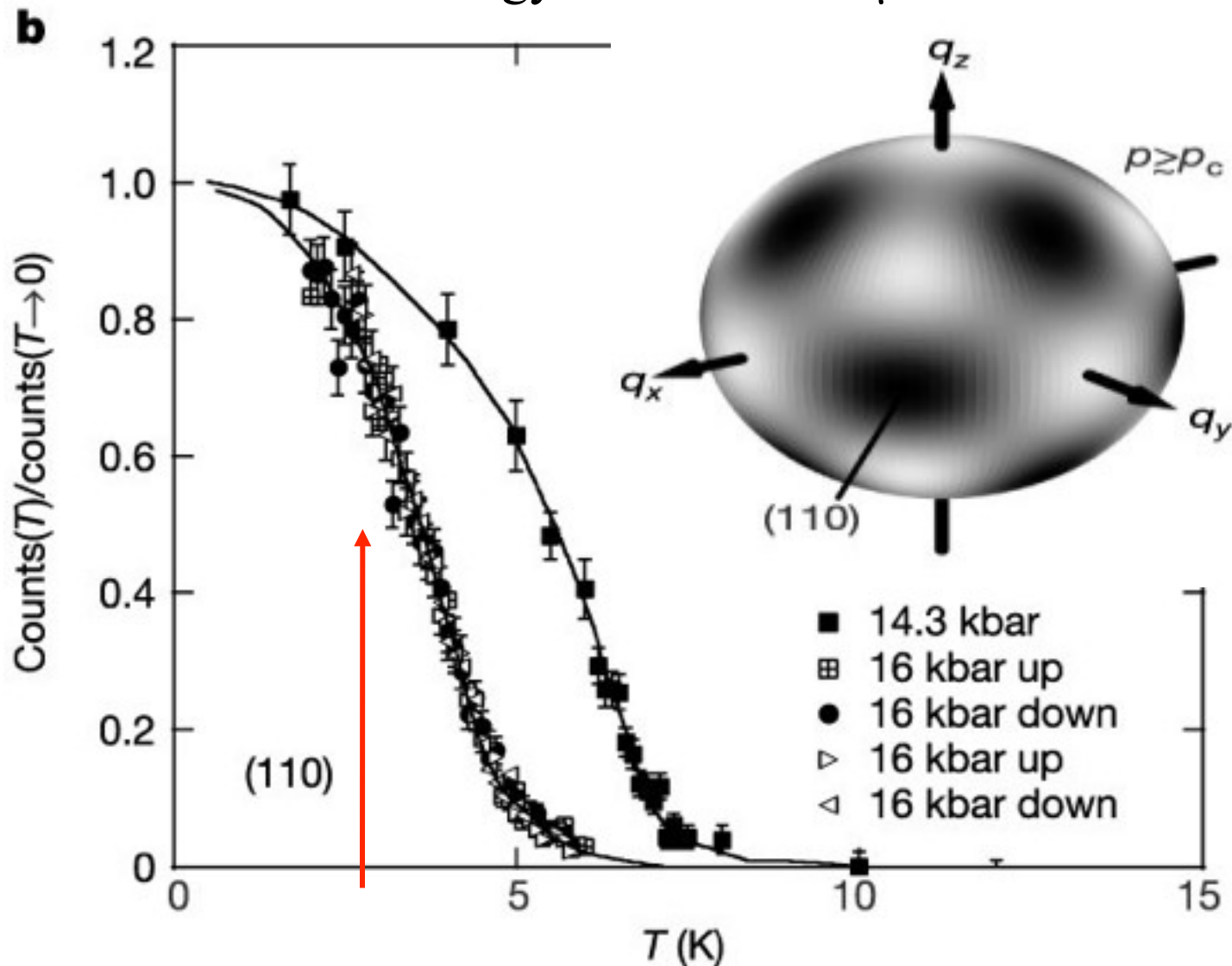


Neutron scattering

Neutron intensity: S^2 times Volume fraction



Neutron energy resolution $50 \mu\text{ eV}$



Mn spin fluctuation rate $\nu < 10^{11} /s$ at 16 kbar

Mn spin fluctuation rate ν at 16 kbar ($p_C < p$) at $T = 2.5$ K

MuSR: $\nu > 10^{10}$ /s, if instantaneous moment size $\sim 0.2 \mu_B$

Neutron: $\nu < 10^{11}$ /s

$$10^{10} < \nu < 10^{11} \text{ /s}$$

➔ Very slow but definitely dynamic fluctuations of the diffusive spin correlations

➔ In para/non mag state, very slow soft mode towards competing magnetic state

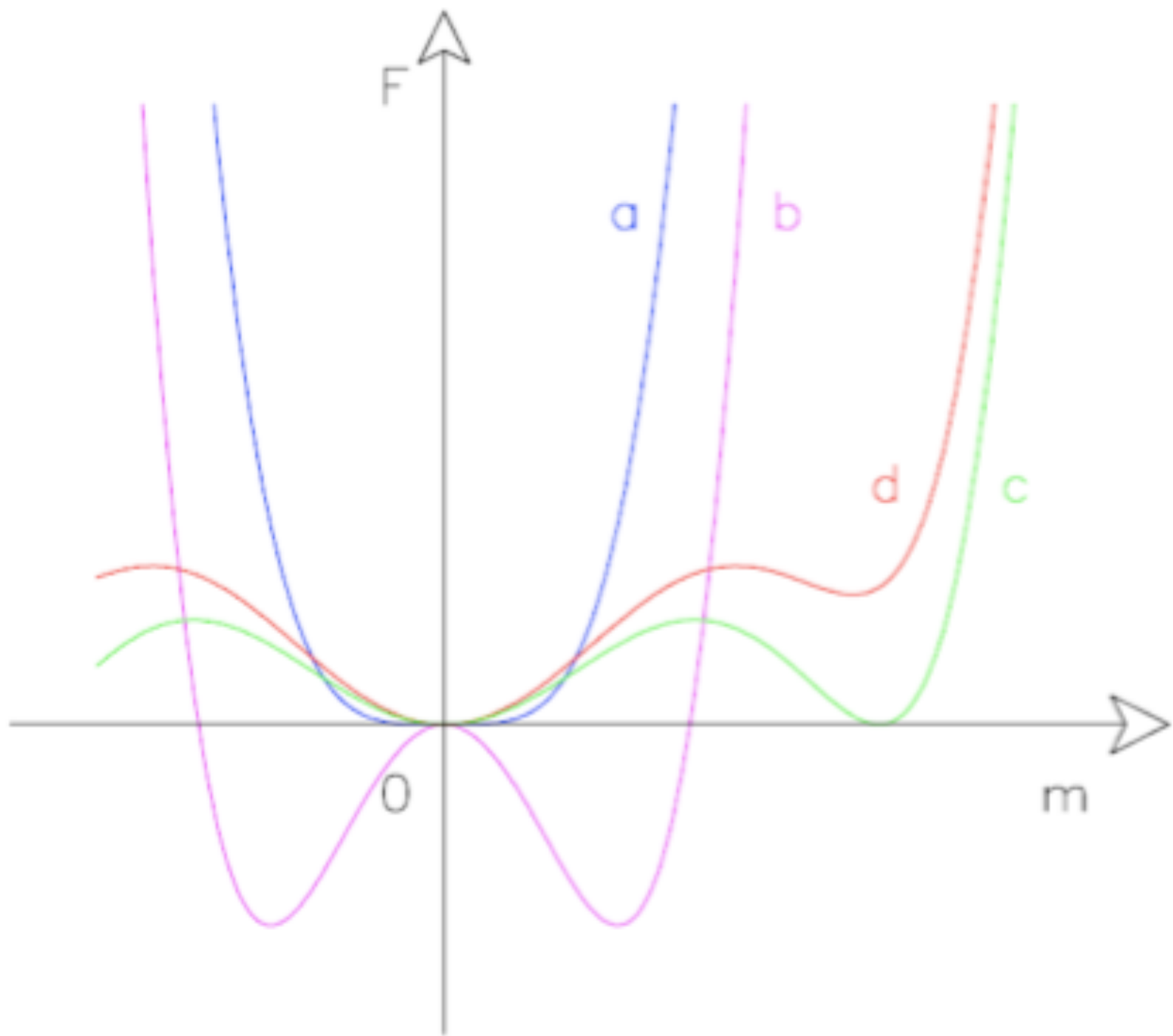


Table 1 Phase separation (PS)/first-order transition (FOT)/partial-volume (PVF) features detected at QPT.

System	Crossover	Parameter (p in kbar)	FOT/PS/PVF	Method
Itinerant electron magnets				
UGe ₂	FM1–para	$p_c = 16$	FOT PS	Magnetization Ge NQR
ZrZn ₂	FM–para	$p_c = 16.5$	FOT	Magnetization
MnSi	Helical–para	$12 = p^* < p < p_c = 14.6$ $p < p_c$ $p < 18$ $p^* < p < p_c$	FOT FOT PVF PS	Susceptibility Si NMR Si NMR μ SR
(Sr _{1-x} Ca _x)RuO ₃	FM–para	$0.7 < Ca(x) < 0.65$	FOT PS FOT	μ SR
Heavy-femion systems				
CeCu _{2.2} Si ₂	AF(a)–SC	Temp.	PS	μ SR
URu ₂ Si ₂	AF–hidden	$3 < p < 10$ $0 < p < 10$	PVF PVF/FOT	Si NMR μ SR
CeIn ₃	AF–SC	$p_c = 24.3$	FOT	In NQR
High- T_c systems				
(La, Sr) ₂ (Cu _{1-x} Zn _x)O ₄	SC–normal	Zn(x)	PS	μ SR
Bi ₂ Sr ₂ Ca(Cu _{2-x} Zn _x)O ₈	SC–fnormal	Zn(x)	PS	STM
(La _{1.85-y} Sr _{0.15} Eu _y)CuO ₄	Stripe–SC	Eu(y)	PS	μ SR
0-doped (La _{2-x} Sr _x)CuO _{4+y}	Stripe–SC	Temp., Sr(x)	PVF/PS	μ SR
Tl ₂ Ba ₂ CuO _{6+δ}	SC–metal	Overdope $O(\delta)$	PS	μ SR
Bi ₂ Sr ₂ CaCu ₂ O _{8+δ}	SC–metal	Overdope $O(\delta)$	PS	STM